

# CSE 250

## Data Structures

Dr. Eric Mikida  
epmikida@buffalo.edu  
208 Capen Hall

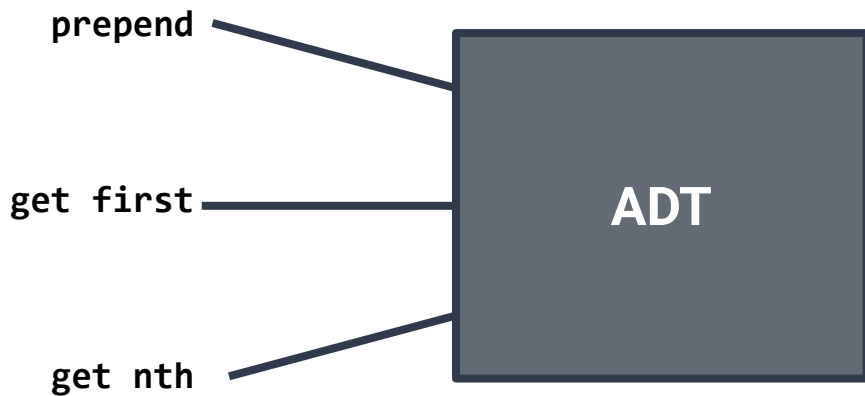
**Lec 04: Intro to Complexity**

# Announcements and Feedback

- Normal recitations (w/attendance) begin next week
- Academic Integrity Quiz due 9/8 @ 11:59PM **(MUST GET 100%)**
- PA0 due 9/8 @ 11:59PM **(MUST GET 100%)**
  - See @38 on Piazza if you ran into server errors
- WA1 due 9/8 @ 11:59PM

# Thought Experiment

An Abstract Data Type is a specification of **what** a data structure can do



# Thought Experiment

Often, many data structures can satisfy a given ADT...how do you choose?



# Thought Experiment

## Data Structure 1

- Very fast `prepend`, `get first`
- Very slow `get nth`

## Data Structure 2

- Very fast `get nth`, `get first`
- Very slow `prepend`

## Data Structure 3

- Very fast `get nth`, `get first`
- Occasionally slow `prepend`

**Which is better?**

# Thought Experiment

## Data Structure 1 (LinkedList)

- Very fast prepend, get first
- Very slow get nth

## Data Structure 2 (Array)

- Very fast get nth, get first
- Very slow prepend

## Data Structure 3 (ArrayList...in reverse)

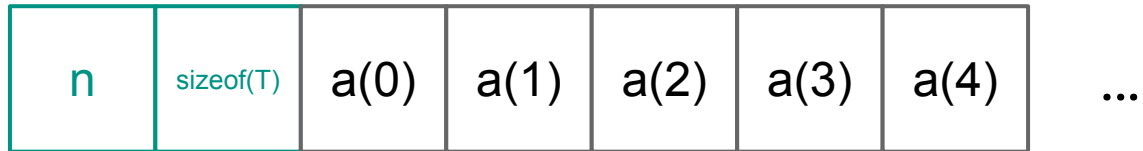
- Very fast get nth, get first
- Occasionally slow prepend

Which is better?

**IT DEPENDS!**

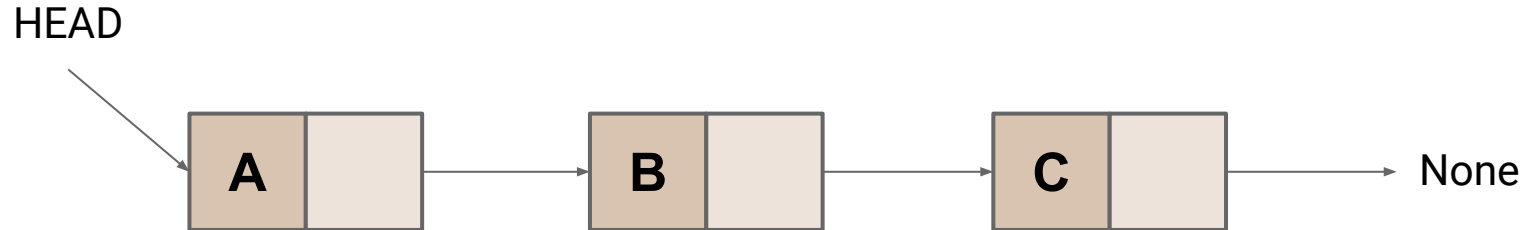
# A (very) Brief Refresher: Array

- An array is an ordered container (elements stored one after another)
- Array elements are all stored in a contiguous block of memory



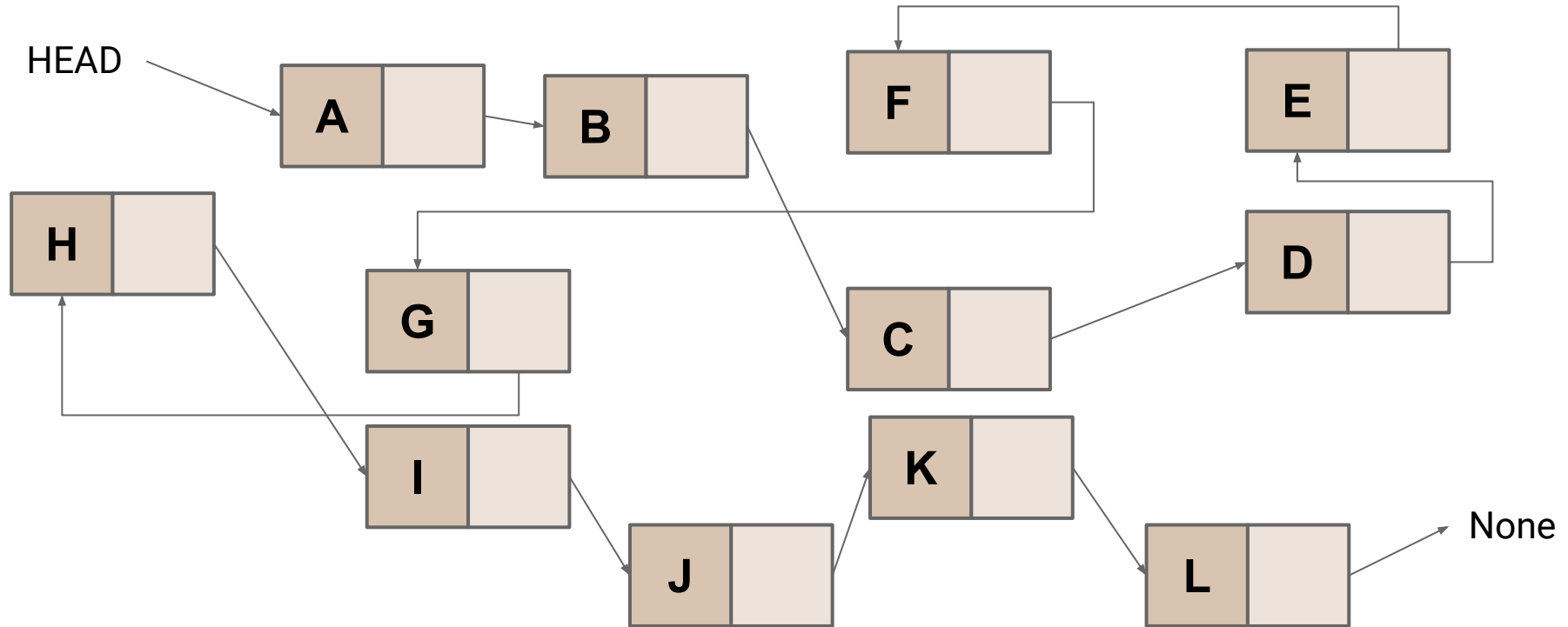
# A (very) Brief Refresher: Linked Lists

- Also an ordered container
- Each element stores a pointer to the next element
  - ...not necessarily in a contiguous block of memory



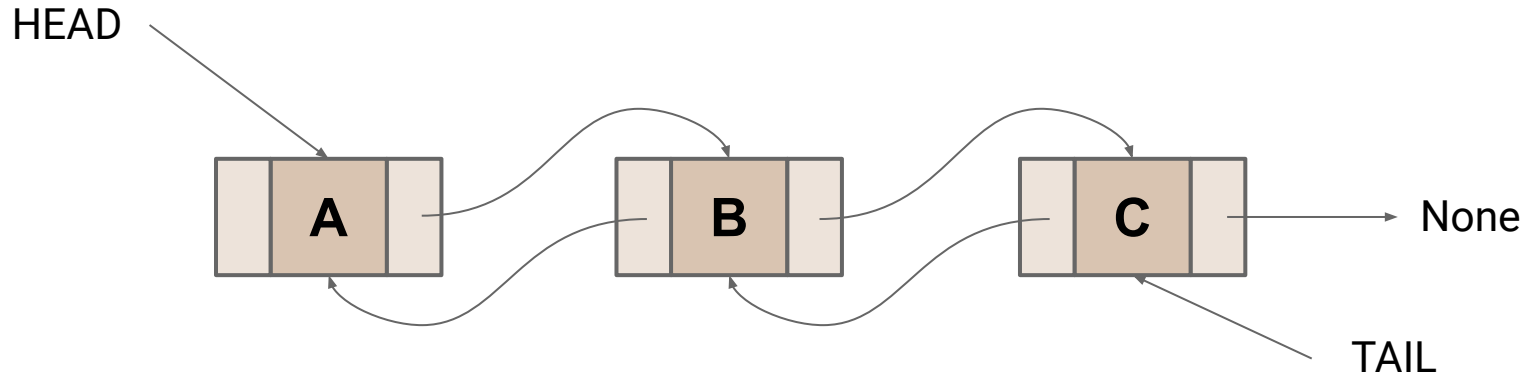


# A (very) Brief Refresher: Linked Lists



# A (very) Brief Refresher: Linked Lists

- Can also be doubly linked (a next AND a prev pointer per node)
- PA1 will have you implementing a **Sorted Doubly Linked List** with some minor twists



# Thought Experiment

## Data Structure 1 (LinkedList)

- Very **fast** prepend, get first
- Very **slow** get nth

## Data Structure 2 (ArrayList)

- Very **fast** get nth, get first
- Very **slow** prepend

## Data Structure 3 (ArrayList...in reverse)

- Very **fast** get nth, get first
- Occasionally **slow** prepend

What is "fast"? "slow"?

# Attempt #1: Wall-clock time?

- What is fast?
  - 10s? 100ms? 10ns?
  - ...it depends on the task
- Algorithm vs Implementation
  - Compare Grace Hopper's implementation to yours
- What machine are you running on?
  - Your old laptop? A lab machine? The newest, shiniest processor on the market?
- What bottlenecks exist? CPU vs IO vs Memory vs Network...

# Attempt #1: Wall-clock time?

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**Wall-clock time is not terribly useful...** <sup>13</sup>

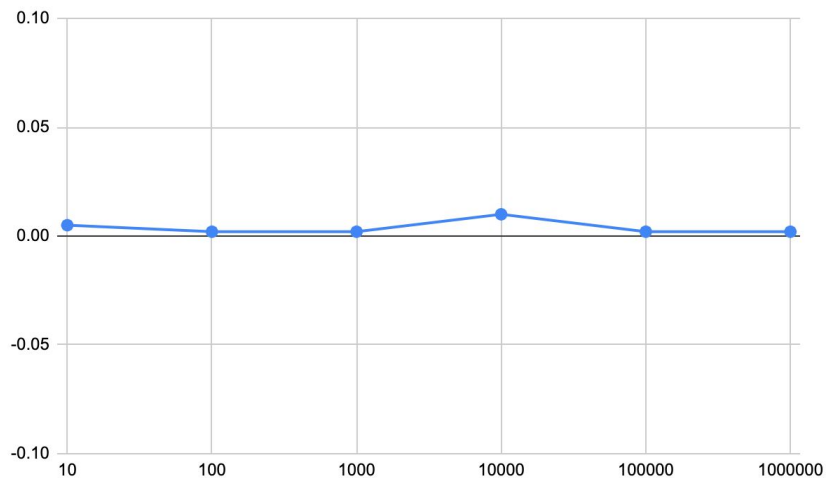
# Analysis Checklist

1. Don't think in terms of wall-time, think in terms of “number of steps”

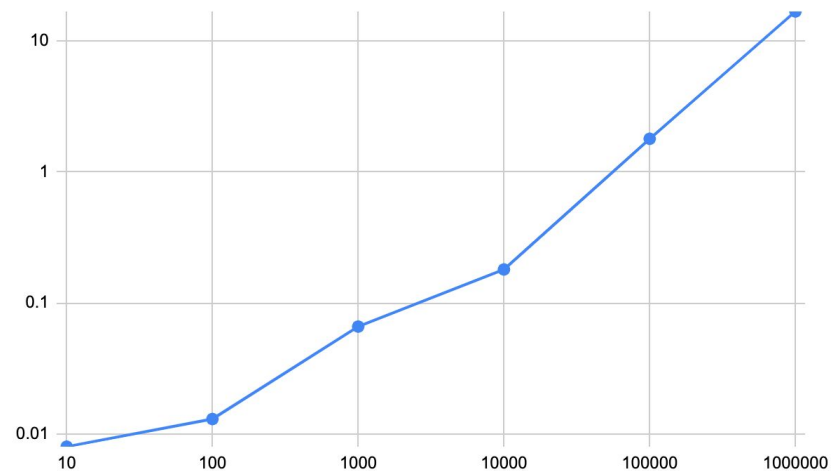
**Let's do a quick demo...**

# Comparing Random Access for Array vs List

## Array



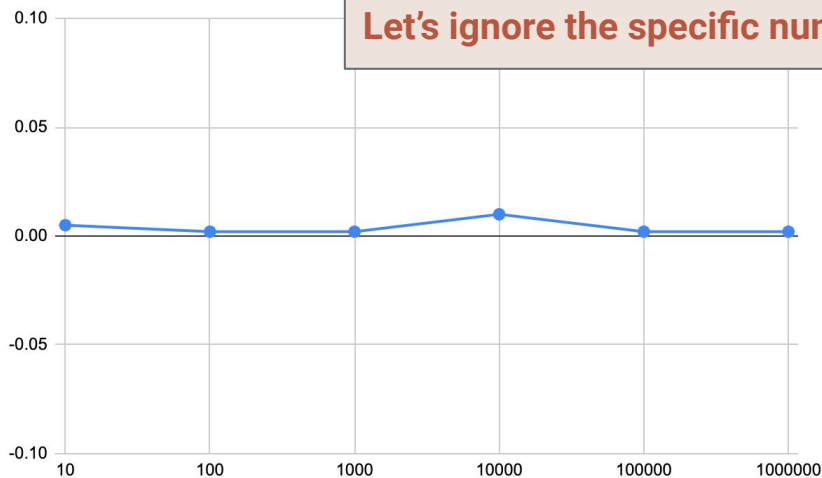
## List



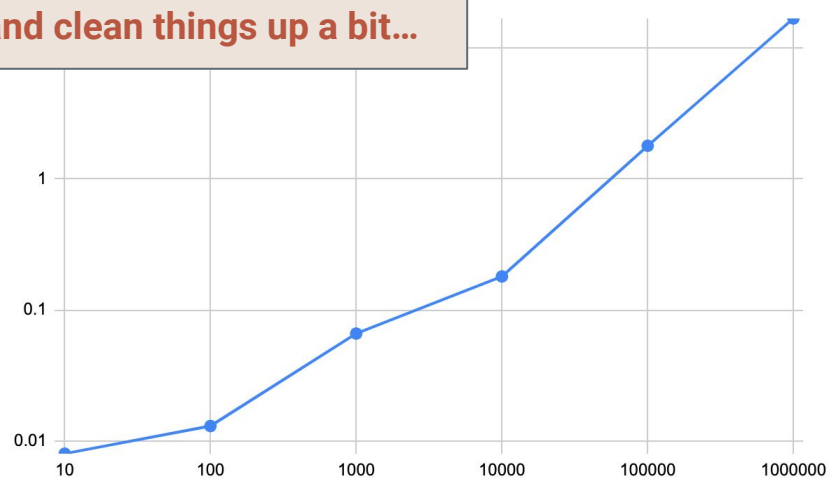


# Comparing Random Access for Array vs List

## Array



## List



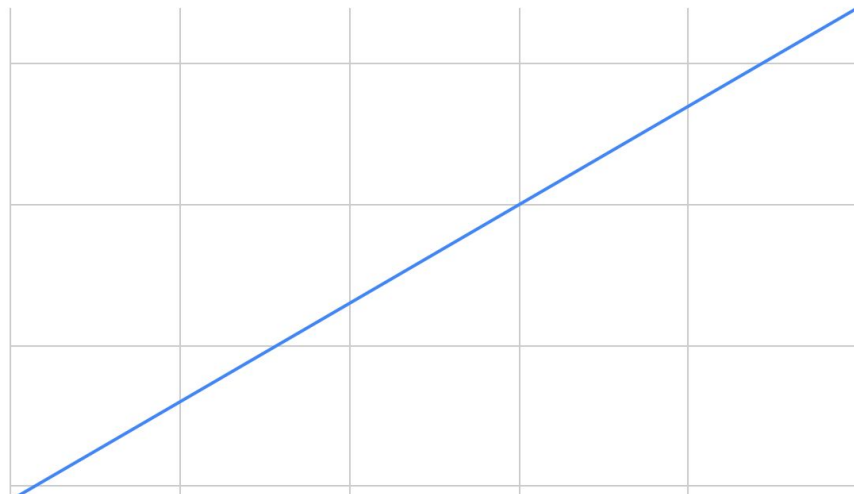
Let's ignore the specific numbers and clean things up a bit...

# Comparing Random Access for Array vs List

**Array**



**List**

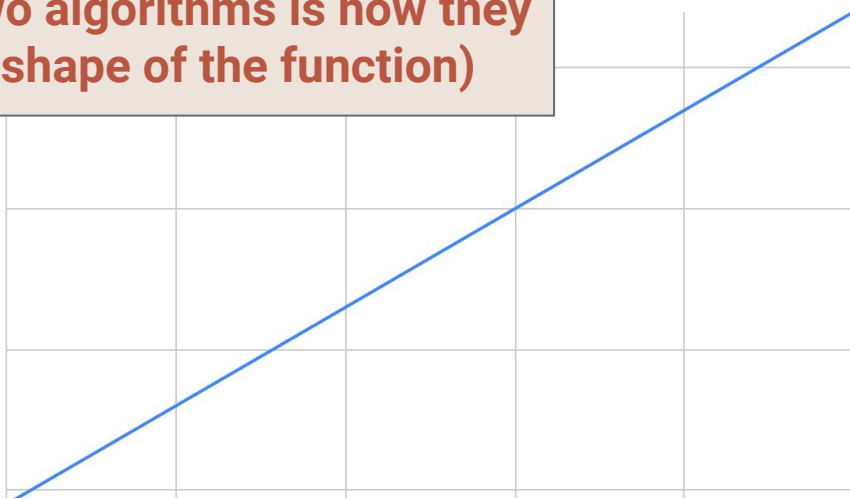
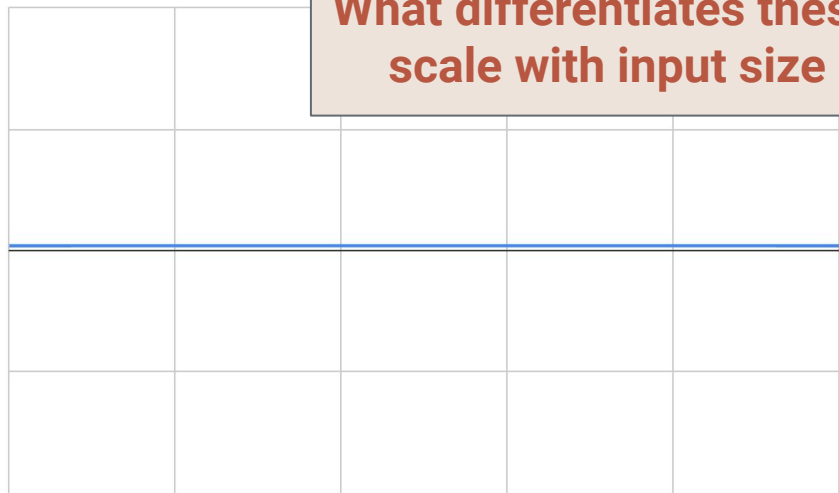


# Comparing Random Access for Array vs List

Array

List

What differentiates these two algorithms is how they scale with input size (the shape of the function)



# Analysis Checklist

1. Don't think in terms of wall-time, think in terms of “number of steps”
2. **To give a useful solution, we should take “scale” into account**
  - **How does the runtime change as we change the size of the input?**

# Counting Steps

```
1 public void userFullName(User[] users, int id) {  
2     User user = users[id];  
3     String fullName = user.firstName + user.lastName;  
4     return fullName;  
5 }
```

# Counting Steps

```
1 public void userFullName(User[] users, int id) {  
2     User user = users[id];  
3     String fullName = user.firstName + user.lastName;  
4     return fullName;  
5 }
```

How many steps does this function take?

# Counting Steps

```
1 public void userFullName(User[] users, int id) {  
2     User user = users[id];  
3     String fullName = user.firstName + user.lastName;  
4     return fullName;  
5 }
```

7 steps...ish? Maybe? What the heck is a step?

# Counting Steps

```
1 public void updateUsers(User[] users) {  
2     x = 1;  
3     for(user : users) {  
4         user.id = x;  
5         x = x + 1;  
6     }  
7 }
```



# Counting Steps

```
1 public void updateUsers(User[] users) {  
2     x = 1; ←  
3     for(user : users) {  
4         user.id = x;  
5         x = x + 1;  
6     }  
7 }
```

1

# Counting Steps

```
1 public void updateUsers(User[] users) {  
2     x = 1;  
3     for(User user : users) { ←  
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7 }
```

$$1 + \sum_{user \in users}$$

# Counting Steps

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1 public void updateUsers(User[] users) {  
2     x = 1;  
3     for(User user : users) {  
4         user.id = x; } ←  
5         x = x + 1;  
6     }  
7 }
```

$$1 + \sum_{user \in users} 4$$

# Counting Steps

```
1 public void updateUsers(User[] users) {  
2     x = 1;  
3     for(User user : users) {  
4         user.id = x;  
5         x = x + 1;  
6     }  
7 }
```

$$1 + \sum_{user \in users} 4 = 1 + 4 \cdot |users|$$

# Counting Steps

```
1 public void totalReads(User[] users, Post[] posts) {  
2     int totalReads = 0;  
3     for(Post post : posts) {  
4         int userReads = 0;  
5         for(User user : users) {  
6             if(user.readPost(post)){ userReads += 1; }  
7         }  
8         totalReads += userReads;  
9     }  
10 }
```

# Counting Steps

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1 public void totalReads(User[] users, Post[] posts) {  
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```

1.

# Counting Steps

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9     }  
10 }
```

$$1 + \sum_{post \in posts}$$

# Counting Steps

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1 public void totalReads(User[] users, Post[] posts) {  
2     int totalReads = 0;  
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5         for(User user : users) {  
6             if(user.readPost(post)){ userReads += 1; }  
7         }  
8         totalReads += userReads; ←  
9     }  
10 }
```

$$1 + \sum_{post \in posts} (3)$$



# Counting Steps

```
1 public void totalReads(User[] users, Post[] posts) {  
2     int totalReads = 0;  
3     for(Post post : posts) {  
4         int userReads = 0;  
5         for(User user : users) { ←  
6             if(user.readPost(post)){ userReads += 1; }  
7         }  
8         totalReads += userReads;  
9     }  
10 }
```

$$1 + \sum_{post \in posts} \left( 3 + \sum_{user \in users} \dots \right)$$

# Counting Steps

```
1 public void totalReads(User[] users, Post[] posts) {  
2     int totalReads = 0;  
3     for(Post post : posts) {  
4         int userReads = 0;  
5         for(User user : users) {  
6             if(user.readPost(post)){ userReads += 1; } ←  
7         }  
8         totalReads += userReads;  
9     }  
10 }
```

$$1 + \sum_{post \in posts} \left( 3 + \sum_{user \in users} 2 \right)$$

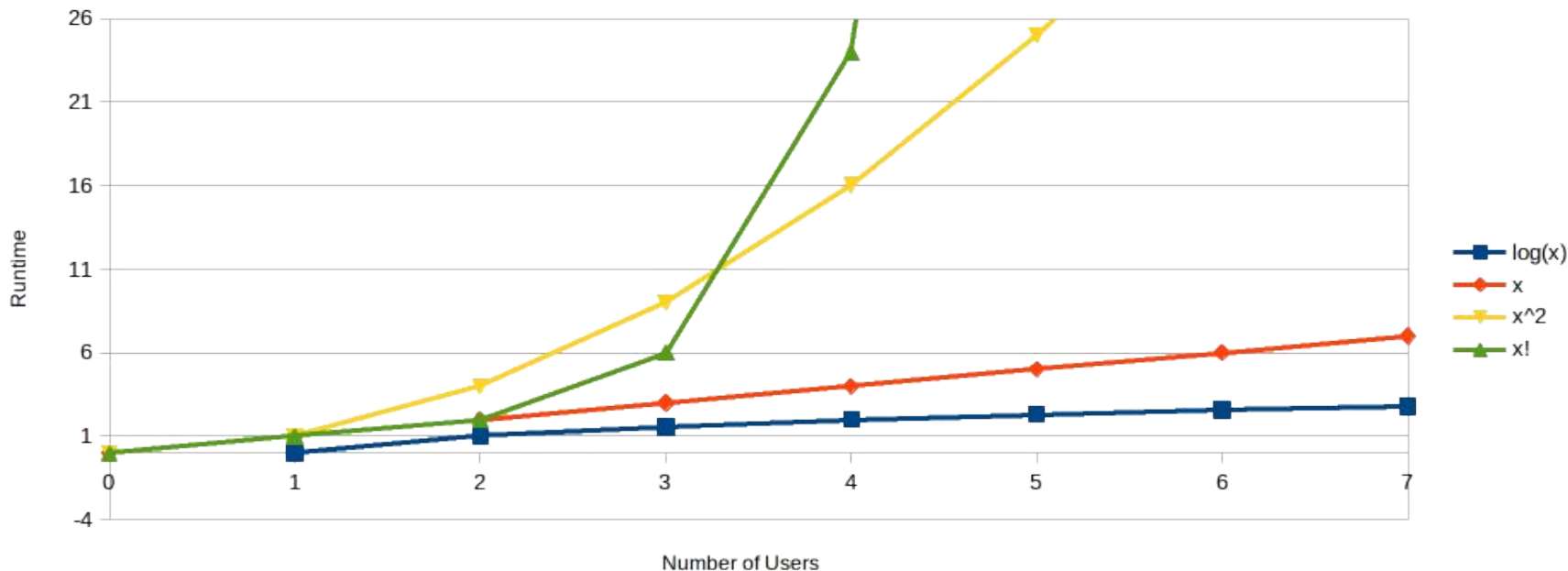
# Steps to "Functions"

Now that we have number of steps\* in terms of summations...  
...which we can simplify (like in WA1) into mathematical functions...

We can start analyzing runtime as a function

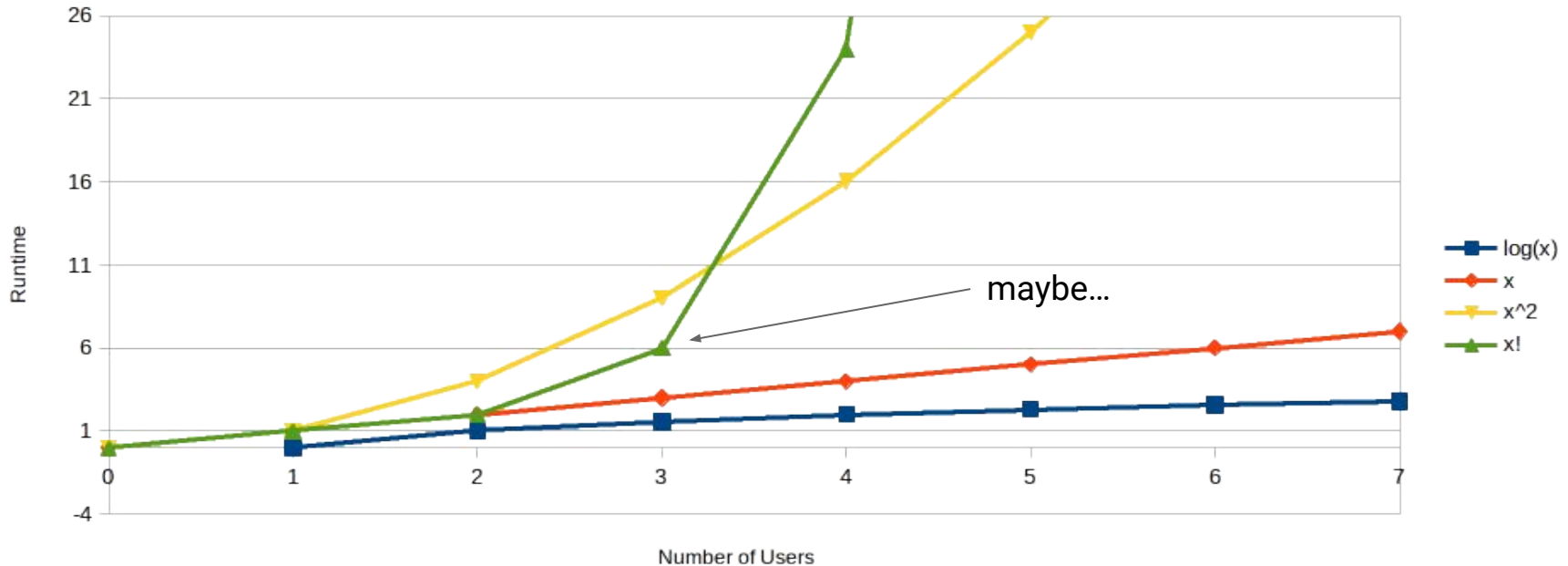
*\* we'll give a better definition of what a "step" is later*

# Runtime as a Function



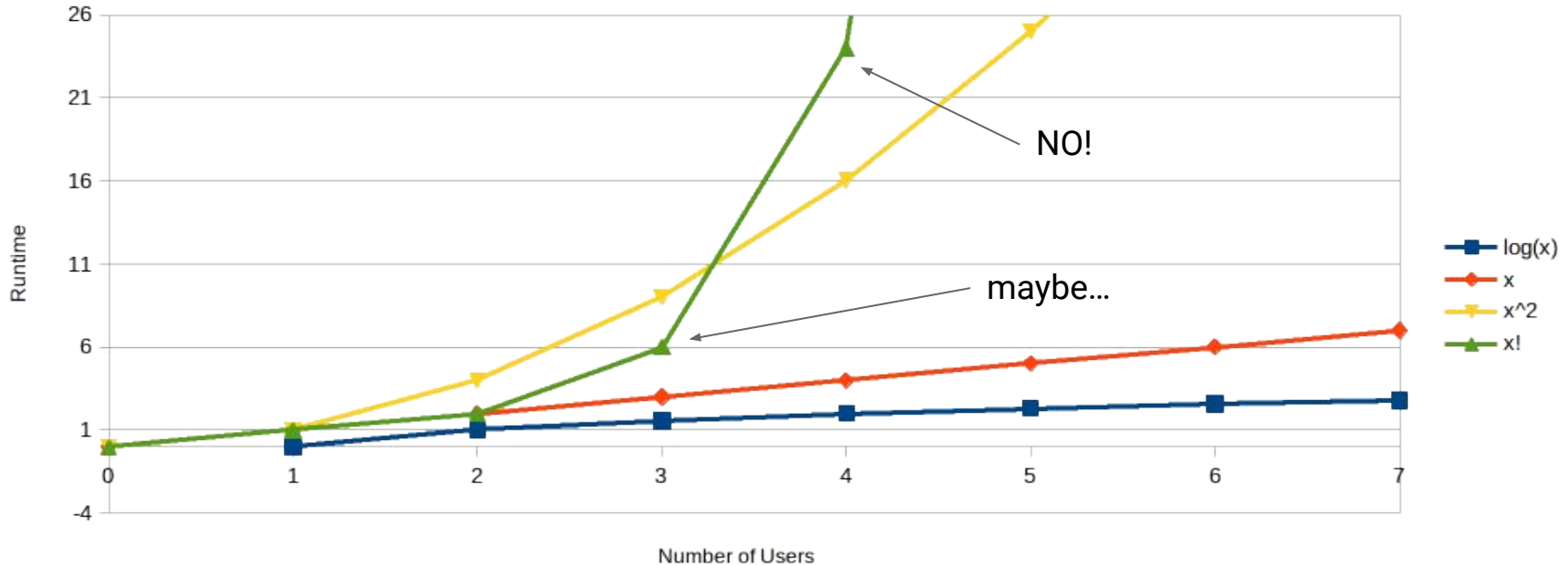
**Would you consider an algorithm that takes  $|\text{Users}|!$  number of steps?**

# Runtime as a Function



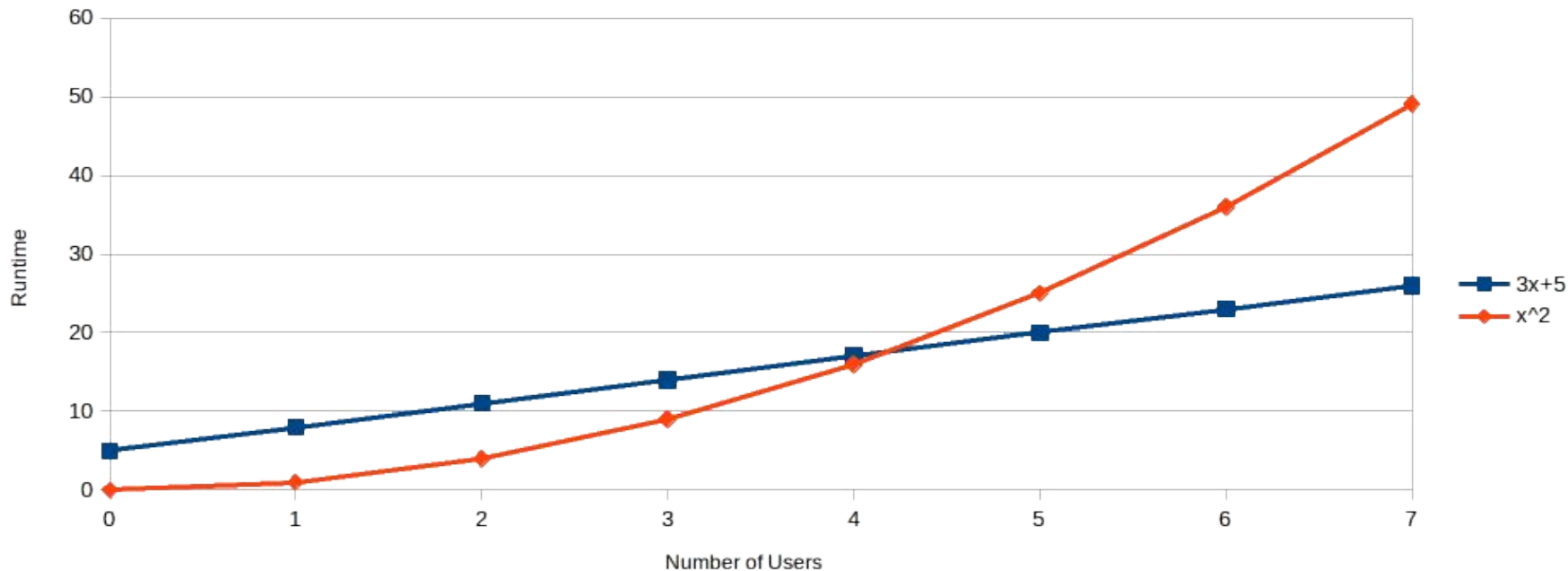
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# Runtime as a Function



**Would you consider an algorithm that takes  $|\text{Users}|!$  number of steps?**

# Runtime as a Function



Which is better?  $3x|\text{Users}|+5$  or  $|\text{Users}|^2$

# Analysis Checklist

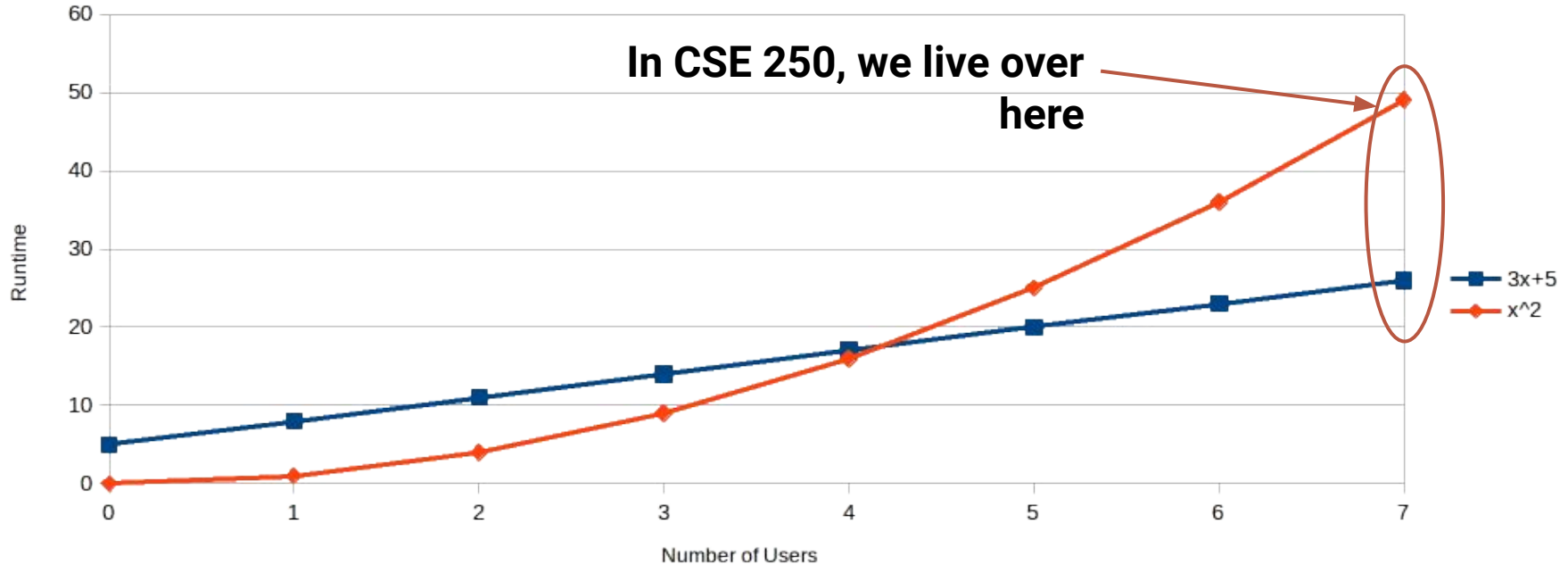
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  - How does the runtime change as we change the size of the input?



# Analysis Checklist

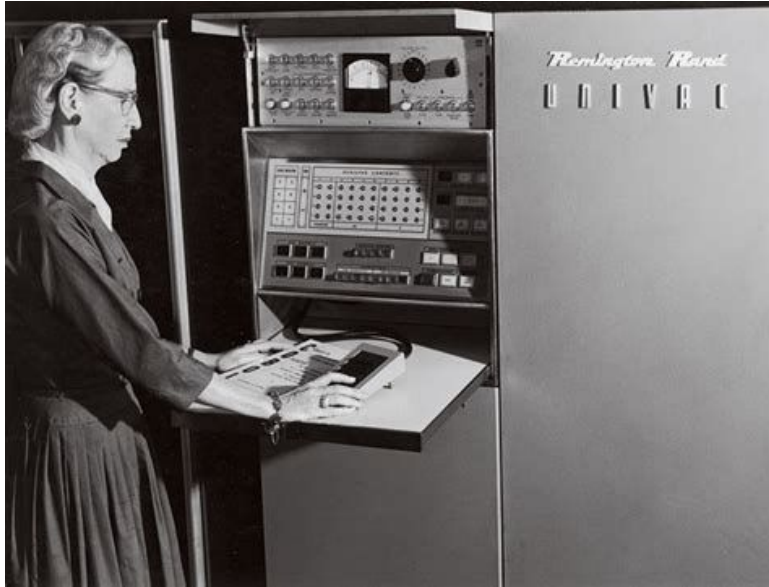
1. Don't think in terms of wall-time, think in terms of “number of steps”
2. To give a useful solution, we should take “scale” into account
  - How does the runtime change as we change the size of the input?
3. **Focus on “large” inputs**
  - **Rank functions based on how they behave at large scales**

# Runtime as a Function



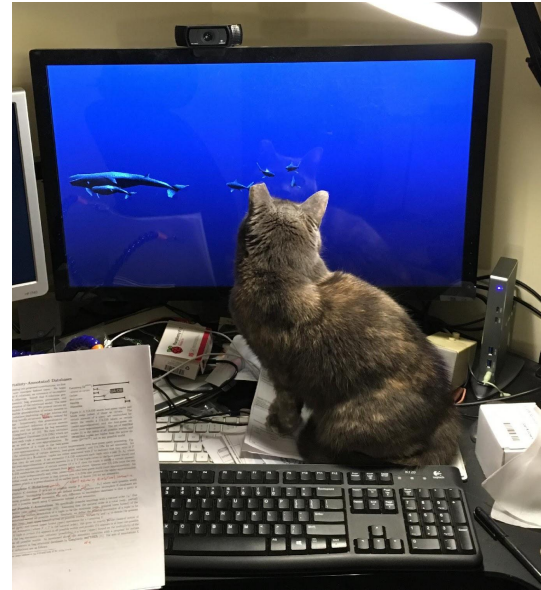
Which is better?  $3x|\text{Users}|+5$  or  $|\text{Users}|^2$

# Goal: Ignore implementation details



**Seasoned Pro Implementation**

**VS**



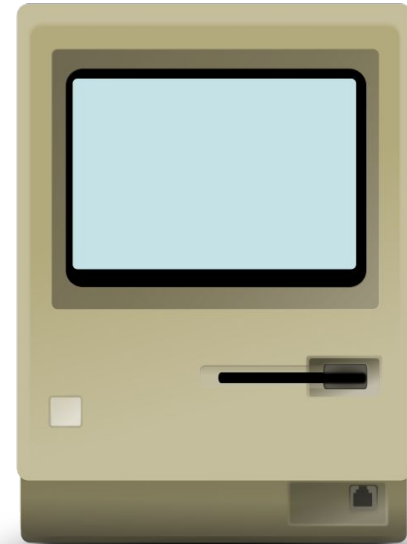
**Error 23: Cat on Keyboard**

# Goal: Ignore execution environment



**Intel i9**

**VS**



**Motorola 68000**

# Goal: Judge the Algorithm Itself

- How fast is a step? Don't care
  - Only count number of steps
- Can this be done in two steps instead of one?
  - “3 steps per user” vs “some number of steps per user”
  - Sometimes we don't care...sometimes we do

# Analysis Checklist

1. Don't think in terms of wall-time, think in terms of "number of steps"
2. To give a useful solution, we should take "scale" into account
  - How does the runtime change as we change the size of the input?
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# Analysis Checklist

1. Don't think in terms of wall-time, think in terms of “number of steps”
2. To give a useful solution, we should take “scale” into account
  - How does the runtime change as we change the size of the input?
3. Focus on “large” inputs
  - Rank functions based on how they behave at large scales
4. **Decouple algorithm from infrastructure/implementation**
  - **Asymptotic notation...?**