

# CSE 250 Recitation

September 8- 9: Summation, PA1 Testing



# Welcome

## Introductions

- SAs: Who are we?
- Class: Who are you?

## Participation

- Written exercises during recitation
- Not about getting it right...it's about gaining hands on experience\*
- Good opportunity to ask questions
- **Turned in with your name and UBIT for attendance** (see syllabus)

\* we reserve the right to not count participation with no effort

# PA1: Getting Started

- **PA1** revolves around linked lists and how to implement them
- All PAs this semester start by writing tests
- Why Test Driven Development?
  - Deepens your understanding of the problem
  - Enables you to test your code without submitting to Autolab
  - Writing code before thinking about the problem will lead to disaster

# PA1: Getting Started

- Remember when writing tests, **understanding the expected behavior** of each method is more important than how to make your implementation
- Some of the best tests are going to be written by asking “what situations could break my code”
- Let's try to come up with some good linked lists for testing
  - **Side note:** how can we make these lists without relying on methods like insert

# PA1: SortedList Exercise

**Discussion:** What are the features of `SortedList` in PA1 that make it different from a vanilla `LinkedList`?

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**Discussion:** What are the features of `SortedList` in PA1 that make it different from a vanilla `LinkedList`?

- Doubly Linked
- Sorted
- Duplicate values are stored in a single linked list node
  - Each node therefore stores the **value** AND the **count**
- Some methods take a node reference as a hint

# PA1: SortedList Exercise

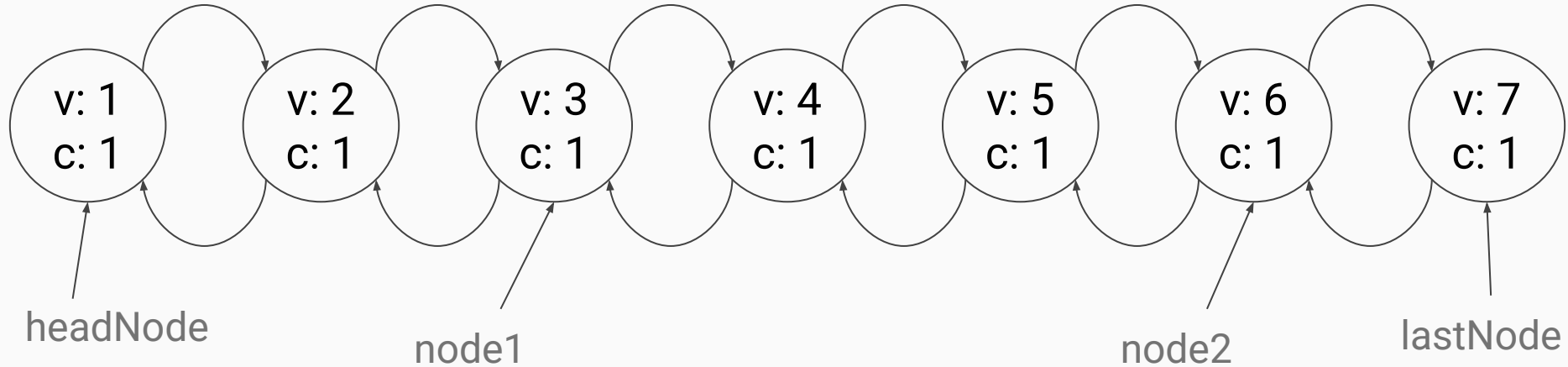
**Exercise:** Write a sequence of 7 values and draw the **SortedList** that would result from inserting those 7 values into an initially empty **SortedList**

Below your list write out the following questions (don't answer them)  
(Pick X, Y, node1 and node2 that you think make them difficult to answer)

1. Is this a valid **SortedList** of length 7?
2. What value is returned by **get(X)**?
3. What node is returned by **findRefBefore(Y, node1)**?
4. What does this list look like after calling **remove(node2)**?

## An Example (Not Necessarily a Good One)

Insertions: 1, 2, 3, 4, 5, 6, 7



1. Is this a valid list of length 7?
2. What value is returned by `get(0)`?
3. What node is returned by `findRefBefore(4, node1)`?
4. What does the list look like after calling `remove(node2)`?

# PA1: SortedList Exercise Part 2

**Exercise:** Trade papers with another student in the class

1. Answer the questions posed by the other student about their list
  - a. If you believe their list is not a valid `SortedList` of length 7, explain why
2. Below their questions, state *at least* one scenario that their list/questions may not account for
  - a. Example for the previous slide: It does not have any nodes with count > 1
3. Switch back and check the other students work

# PA1: SortedList Exercise Wrap Up

**Wrap Up:** Think about this exercise when writing tests

1. Take the role of the other student finding holes in your tests to think about things you may not be checking for
2. To cover the holes you may need to make different lists, or may just need to ask different questions about your current lists
  - a. The more situations you cover, the more confident you can be in an implementation that passes your tests
3. **DON'T STOP** writing tests after the testing phase...keep adding tests

# Other Tips for Testing

- Try to test just one function at a time
  - What if we want to test get? How can we build a list without using insert?
- After writing some tests, re-read the handout and for each function be on the lookout for sentences that describe untested behavior
- If AutoLab finds a bug in your implementation, don't think "I need to fix that bug", think "I need to figure out why MY tests didn't catch it".

# Summations – General Form

$$\sum_{i=j}^k f(i) = f(j) + f(j+1) + \dots + f(k)$$

# Summations - Examples

k is 7

$\sum_{i=4}^7 5i = 20 + 25 + 30 + 35$

f(i) is 5i

j is 4

f(4)      f(5)      f(6)      f(7)

# Summations - Examples

$n^2$  is  $n^2$        $f(i)$  is  $15n \cdot i$

$$\sum_{i=n}^{n^2} 15n \cdot i = 15n^2 + 15n \cdot (n + 1) + \dots + 15n^3$$

$j$  is  $n$

$f(n)$        $f(n+1)$        $f(n^2)$

The bounds of our summation  
can be unknowns!

# Simplifying the Summation

$$\sum_{i=1}^{n^2} 15n \cdot i$$

Identify the parts of this summation  
are **constant with respect to the  
summation variable**

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$$\sum_{i=1}^{n^2} 15n \cdot i$$

Identify the parts of this summation are **constant with respect to the summation variable**

(notice how on the previous slide each term had a  $15n$  that did not change...only the value of  $i$  did)

# Simplifying the Summation

$$\sum_{i=n}^{n^2} 15n \cdot i$$

Which of S1, S8, or S9 does this most resemble?

$$S1. \sum_{i=j}^k c = \dots$$

$$S8. \sum_{i=1}^k i = \dots$$

$$S9. \sum_{i=0}^k 2^i = \dots$$

# Simplifying the Summation

$$\sum_{i=1}^{n^2} 15n \cdot i$$

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# Simplifying the Summation

$$\sum_{i=n}^{n^2} 15n \cdot i$$

What parts of the summation don't match the rule?

$$\text{S8. } \sum_{i=1}^k i = \dots$$

# Simplifying the Summation

$$\sum_{i=n}^{n^2} 15n \cdot i$$

What parts of the summation don't match the rule?

$$S8. \sum_{i=1}^k i = \dots$$

Notice how the lower bound in S8 is NOT an unknown...it must be exactly 1 to match

# Recitation Exercise

Simplify the summation to its closed form solution using rules on the next slide

$$\sum_{i=1}^{n^2} 15n \cdot i$$

# Summation Rules

$$S1. \sum_{i=j}^k c = (k - j + 1)c$$

$$S2. \sum_{i=j}^k (cf(i)) = c \sum_{i=j}^k f(i)$$

$$S3. \sum_{i=j}^k (f(i) + g(i)) = \left( \sum_{i=j}^k f(i) \right) + \left( \sum_{i=j}^k g(i) \right)$$

$$S4. \sum_{i=j}^k (f(i)) = \left( \sum_{i=\ell}^k (f(i)) \right) - \left( \sum_{i=\ell}^{j-1} (f(i)) \right) \quad (\text{for any } \ell < j)$$

$$S5. \sum_{i=j}^k f(i) = f(j) + f(j+1) + \dots + f(k-1) + f(k)$$

$$S6. \sum_{i=j}^k f(i) = f(j) + \dots + f(\ell-1) + \left( \sum_{i=\ell}^k f(i) \right) \quad (\text{for any } j < \ell \leq k)$$

$$S7. \sum_{i=j}^k f(i) = \left( \sum_{i=j}^{\ell} f(i) \right) + f(\ell+1) + \dots + f(k) \quad (\text{for any } j \leq \ell < k)$$

$$S8. \sum_{i=1}^k i = \frac{k(k+1)}{2}$$

$$S9. \sum_{i=0}^k 2^i = 2^{k+1} - 1$$

$$\sum_{i=n}^{n^2} 15n \cdot i$$

"Bonus" Question

$$\sum_{x=0}^n \sum_{y=1}^k (x + 1)$$