

CSE 443
Compilers

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Phases of a compiler

Syntactic
structure

Symbol Table

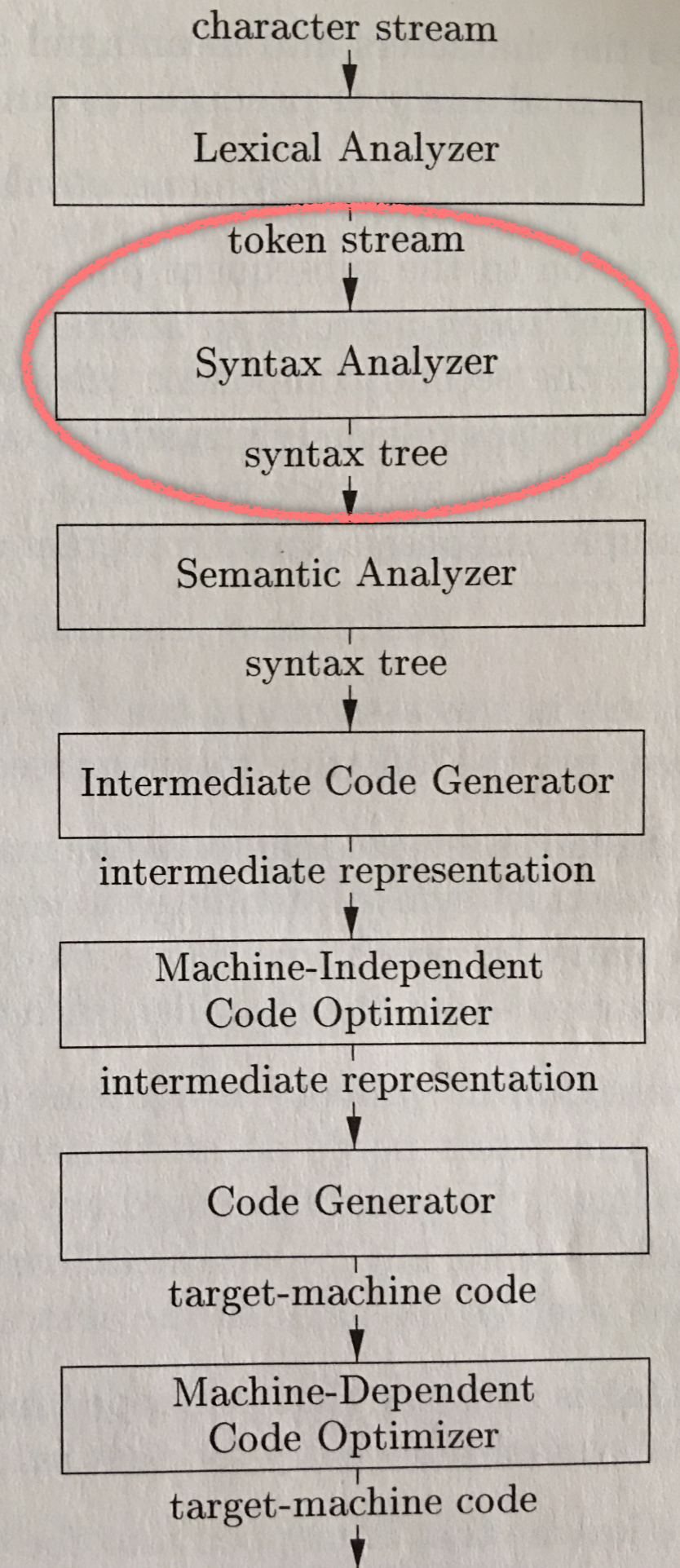


Figure 1.6,
page 5 of text

Recursion and parentheses

- To generate $2+3*4$ or $3*4+2$, the parse tree is built so that $+$ is higher in the tree than $*$.
- To force an addition to be done prior to a multiplication we must use parentheses, as in $(2+3)*4$.
- Grammar captures this in the recursive case of an expression, as in the following grammar fragment:

$\langle \text{expr} \rangle \rightarrow \langle \text{expr} \rangle + \langle \text{term} \rangle \mid \langle \text{term} \rangle$

$\langle \text{term} \rangle \rightarrow \langle \text{term} \rangle * \langle \text{factor} \rangle \mid \langle \text{factor} \rangle$

$\langle \text{factor} \rangle \rightarrow \langle \text{variable} \rangle \mid \langle \text{constant} \rangle \mid \text{“}(\text{”} \langle \text{expr} \rangle \text{“})\text{”}$

RL \subseteq CFL

- Given a regular language L we can always construct a context free grammar G such that $L = \mathcal{L}(G)$.
- For every regular language L there is an NFA $M = (S, \Sigma, \delta, F, s_0)$ such that $L = \mathcal{L}(M)$.
- Build $G = (N, T, P, S_0)$ as follows:
 - $N = \{ N_s \mid s \in S \}$
 - $T = \{ t \mid t \in \Sigma \}$
 - If $\delta(i, a) = j$, then add $N_i \rightarrow a N_j$ to P
 - If $i \in F$, then add $N_i \rightarrow \varepsilon$ to P
 - $S_0 = N_{s_0}$

$RL \subsetneq CFL$

- Show that not all CF languages are regular.
- To do this we only need to demonstrate that there exists a CFL that is not regular.
- Consider $L = \{ a^n b^n \mid n \geq 1 \}$
- Claim: $L \in CFL, L \notin RL$

Relevance?

Nested '{' and '}'

```
public class Foo {  
    public static void main(String[] args) {  
        for (int i=0; i<args.length; i++) {  
            if (args[i].length() < 3) { ... }  
            else { ... }  
        }  
    }  
}
```

Context Free Grammars and parsing

- $O(n^3)$ algorithms to parse any CFG exist
- Programming language constructs can generally be parsed in $O(n)$

Top-down & bottom-up

- A top-down parser builds a parse tree from root to the leaves
 - easier to construct by hand
- A bottom-up parser builds a parse tree from leaves to root
 - Handles a larger class of grammars
 - tools (yacc/bison) build bottom-up parsers

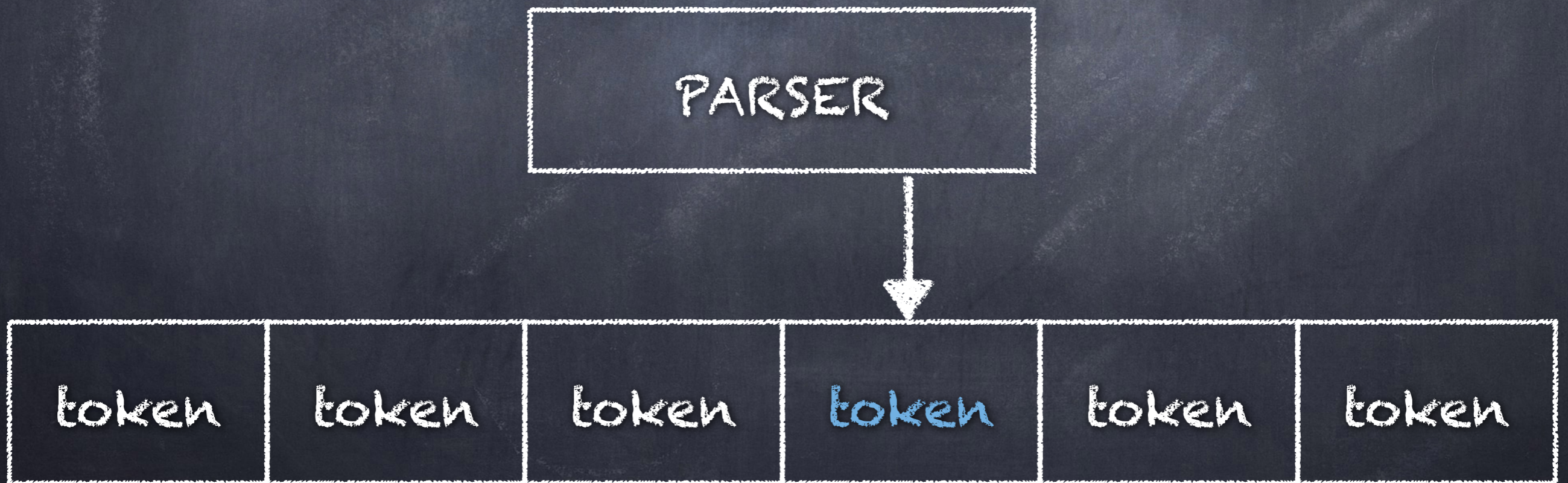
Our presentation

First top-down, then bottom-up

- Present top-down parsing first.
- Introduce necessary vocabulary and data structures.
- Move on to bottom-up parsing second.

vocab: look-ahead

- The current symbol being scanned in the input is called the lookahead symbol.



Top-down parsing

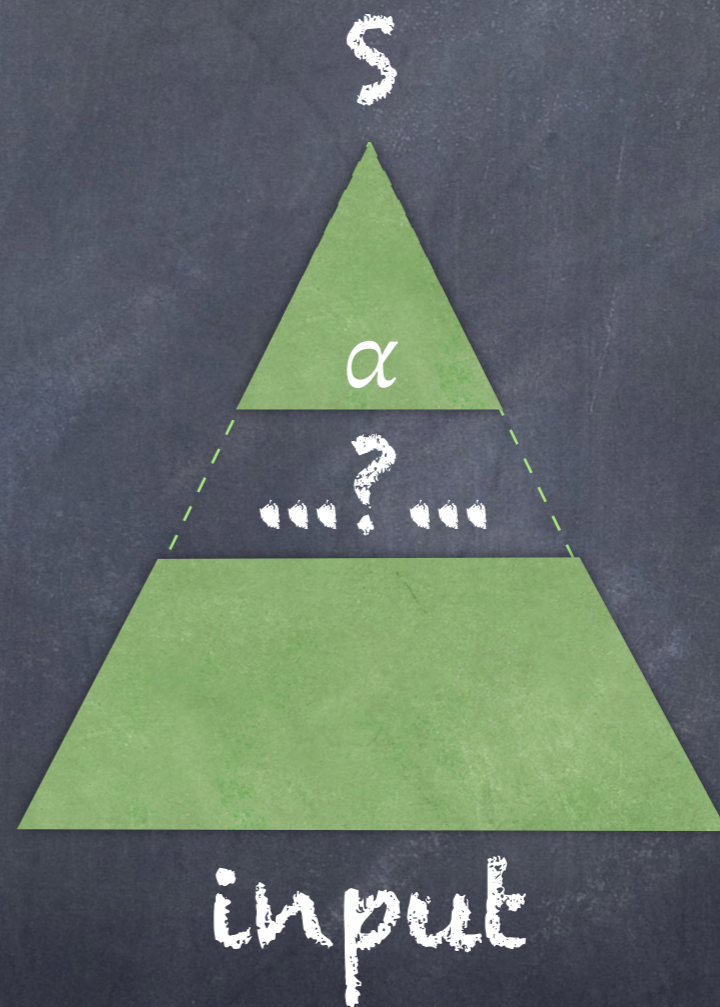
- Start from grammar's start symbol
- Build parse tree so its yield matches input
- predictive parsing: a simple form of recursive descent parsing

Basic idea:
try to build a derivation
 $S \Rightarrow^* \text{input}$

$S \Rightarrow^* \alpha$

...?...

$\Rightarrow^* \text{input}$



FIRST(α)

- If $\alpha \in (NUT)^*$ then FIRST(α) is "the set of terminals that appear as the first symbols of one or more strings of terminals generated from α ."

[p. 64]

- Ex: If $A \rightarrow a \beta$ then FIRST(A) = $\{a\}$
- Ex. If $A \rightarrow a \beta \mid B$ then FIRST(A) = $\{a\} \cup \text{FIRST}(B)$

FIRST(α)

- First sets are considered when there are two (or more) productions to expand $A \in N$: $A \rightarrow \alpha \mid \beta$
- Predictive parsing requires that $\text{FIRST}(\alpha) \cap \text{FIRST}(\beta) = \emptyset$

ϵ productions

- If lookahead symbol does not match first set, use ϵ production not to advance lookahead symbol but instead "discard" non-terminal:
 - $optexpr \rightarrow expr \mid \epsilon$
- "While parsing $optexpr$, if the lookahead symbol is not in $FIRST(expr)$, then the ϵ production is used" [p. 66]

Left recursion

- Grammars with left recursion are problematic for top-down parsers, as they lead to infinite regress.

Left recursion example

- Grammar:

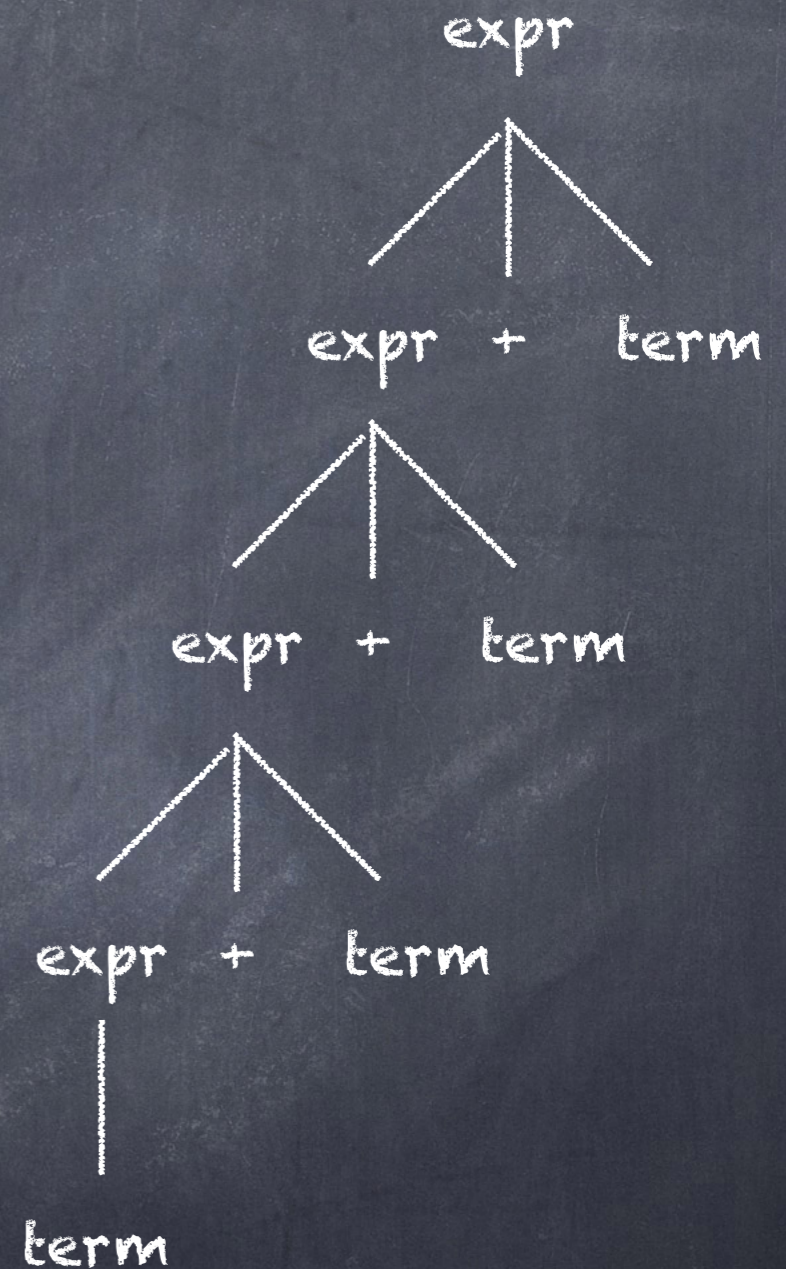
$\text{expr} \rightarrow \text{expr} + \text{term} \mid \text{term}$

$\text{term} \rightarrow \text{id}$

- FIRST sets for rule alternatives are not disjoint:

- $\text{FIRST}(\text{expr}) = \text{id}$

- $\text{FIRST}(\text{term}) = \text{id}$



Left recursion example

Grammar:

$A \alpha$

β

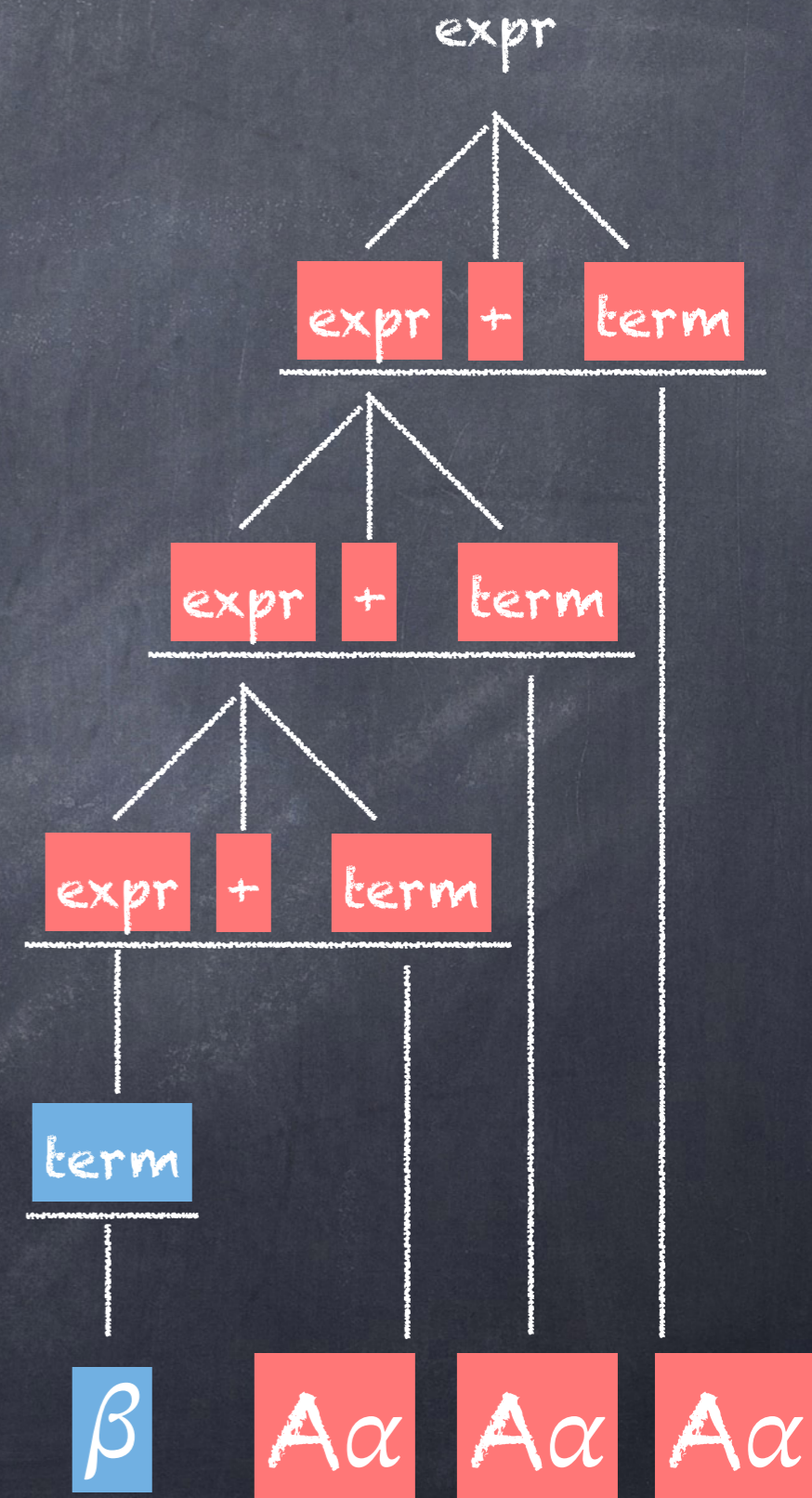
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$\text{FIRST}(\text{term}) = \text{id}$



Rewriting grammar to remove left recursion

• expr rule is of form $A \rightarrow A\alpha \mid \beta$

• Rewrite as two rules

• $A \rightarrow \beta R$

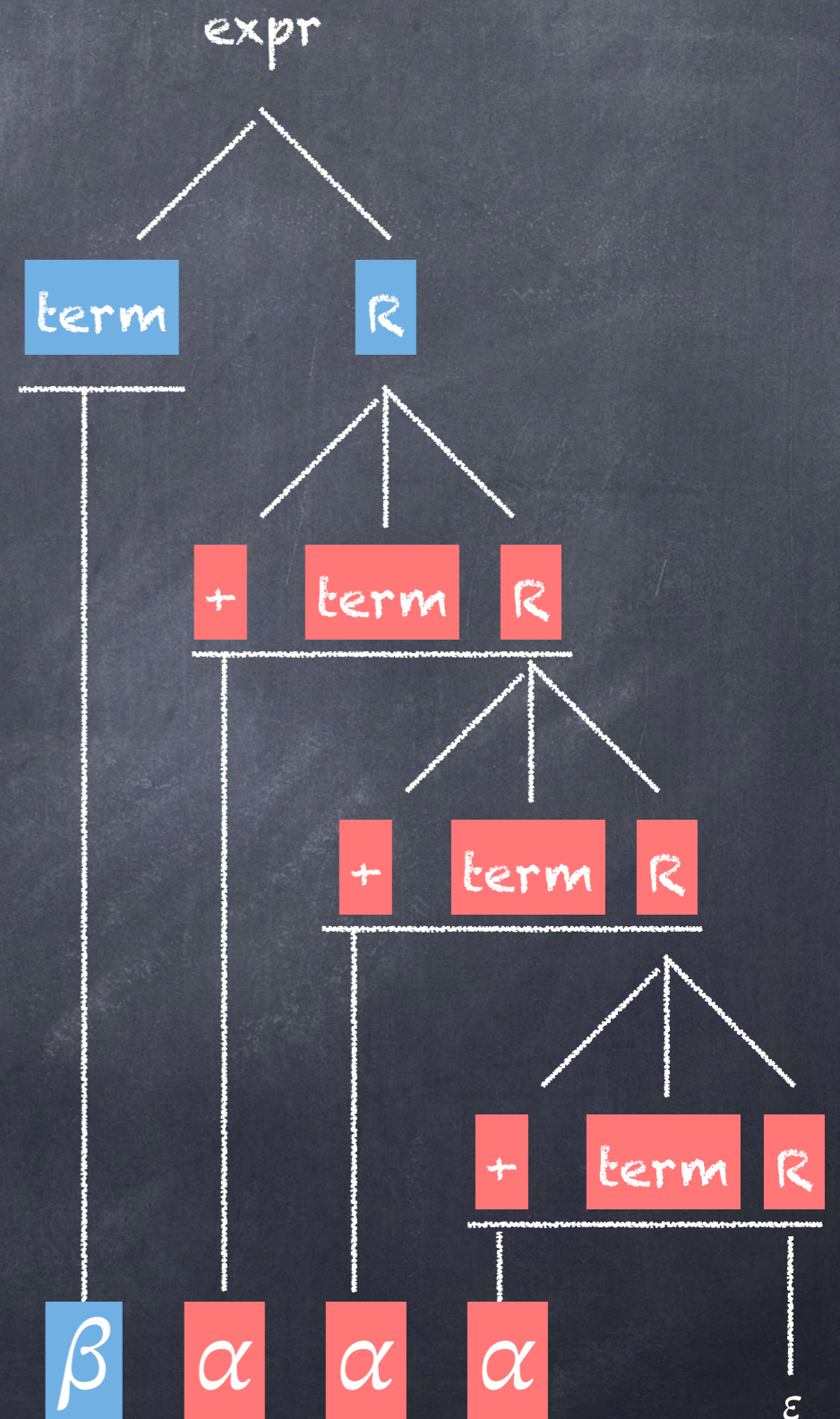
• $R \rightarrow \alpha R \mid \epsilon$

Back to example

• Grammar is re-written as

• $\text{expr} \rightarrow \text{term } R$

• $R \rightarrow + \text{term } R \mid \epsilon$



Ambiguity

- A grammar G is ambiguous if $\exists \sigma \in \mathcal{L}(G)$ that has two or more distinct parse trees.
- Example - dangling 'else':

if $\langle \text{expr} \rangle$ then if $\langle \text{expr} \rangle$ then $\langle \text{stmt} \rangle$ else $\langle \text{stmt} \rangle$

if $\langle \text{expr} \rangle$ then { if $\langle \text{expr} \rangle$ then $\langle \text{stmt} \rangle$ } else $\langle \text{stmt} \rangle$

if $\langle \text{expr} \rangle$ then { if $\langle \text{expr} \rangle$ then $\langle \text{stmt} \rangle$ else $\langle \text{stmt} \rangle$ }

dangling else resolution

- usually resolved so else matches closest if-then
- we can re-write grammar to force this interpretation (ms = matched statement, os = open statement)

$\langle \text{stmt} \rangle \rightarrow \langle \text{ms} \rangle \mid \langle \text{os} \rangle$

$\langle \text{ms} \rangle \rightarrow \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{ms} \rangle \text{ else } \langle \text{ms} \rangle \mid \dots$

$\langle \text{os} \rangle \rightarrow \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{stmt} \rangle \mid \text{if } \langle \text{expr} \rangle \text{ then } \langle \text{ms} \rangle \text{ else } \langle \text{os} \rangle$

Left factoring

- If two (or more) rules share a prefix then their FIRST sets do not distinguish between rule alternatives.
- If there is a choice point later in the rule, rewrite rule by factoring common prefix
- Example: rewrite

$$A \rightarrow \alpha \beta_1 \mid \alpha \beta_2$$

• as

$$A \rightarrow \alpha A'$$

$$A' \rightarrow \beta_1 \mid \beta_2$$

Predictive parsing:

a special case of recursive-descent parsing that does not require backtracking

Each non-terminal $A \in N$ has an associated procedure:

```
void A() {  
    choose an A-production  $A \rightarrow X_1 X_2 \dots X_k$   
    for ( $i = 1$  to  $k$ ) {  
        if ( $x_i \in N$ ) {  
            call  $x_i()$   
        }  
        else if ( $x_i =$  current input symbol) {  
            advance input to next symbol  
        }  
        else error  
    }  
}
```


Predictive parsing:

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        }  
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            advance input to next symbol  
        }  
        else error  
    }  
}
```

There is non-determinism in choice of production. If "wrong" choice is made the parser will need to revisit its choice by backtracking.

A predictive parser can always make the correct choice here.

FIRST(X)

- if $X \in T$ then $\text{FIRST}(X) = \{ X \}$
- if $X \in N$ and $X \rightarrow Y_1 Y_2 \dots Y_k \in P$ for $k \geq 1$, then
 - add $a \in T$ to $\text{FIRST}(X)$ if $\exists i$ s.t. $a \in \text{FIRST}(Y_i)$ and $\varepsilon \in \text{FIRST}(Y_j) \forall j < i$ (i.e. $Y_1 Y_2 \dots Y_{i-1} \Rightarrow^* \varepsilon$)
 - if $\varepsilon \in \text{FIRST}(Y_j) \forall j \leq k$ add ε to $\text{FIRST}(X)$
- if $X \rightarrow \varepsilon \in P$, then add ε to $\text{FIRST}(X)$

FOLLOW(X)

- Place $\$$ in FOLLOW(S), where S is the start symbol ($\$$ is an end marker)
- if $A \rightarrow \alpha B \beta \in P$, then $\text{FIRST}(\beta) - \{\epsilon\}$ is in FOLLOW(B)
- if $A \rightarrow \alpha B \in P$ or $A \rightarrow \alpha B \beta \in P$ where $\epsilon \in \text{FIRST}(\beta)$, then everything in FOLLOW(A) is in FOLLOW(B)

Table-driven predictive parsing

Algorithm 4.32 (p. 224)

- INPUT: Grammar $G = (N, T, P, S)$
- OUTPUT: Parsing table M
- For each production $A \rightarrow \alpha$ of G :
 1. For each terminal $a \in \text{FIRST}(\alpha)$, add $A \rightarrow \alpha$ to $M[A, a]$
 2. If $\epsilon \in \text{FIRST}(\alpha)$, then for each terminal b in $\text{FOLLOW}(A)$, add $A \rightarrow \alpha$ to $M[A, b]$
 3. If $\epsilon \in \text{FIRST}(\alpha)$ and $\$ \in \text{FOLLOW}(A)$, add $A \rightarrow \alpha$ to $M[A, \$]$