COMPLETS

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End-of-Semester overview

M	W	
4/21 Optimizations 2	4/23 Workshop day	4/25 Optimizations 3
4/28 Workshop day	4/30 Team Presentations	5/02 Team Presentations
5/05 Review for final exam	5/07	5/09
5/12	^{5/14} Final exam: 8:00 AM - 11:00 AM Norton 210 (this room)	



Algebraic Identities [p. 536]

Constant folding

"...evaluate constant expressions at compile time and replace the constant expressions by their values."

Algebraic Identities [p. 536]

See footnote 2:

"Arithmetic expressions should be evaluated the same way at compile time as they are at run time. K. Thompson has suggested an elegant solution to constant folding: compile the constant expression, execute the target code on the spot, and replace the expression with the result. Thus, the compiler does not need to contain an interpreter."

Peephole optimization [p 549]

"The peephole is a small, sliding window on a program." [p. 549]

"In general, repeated passes over the target code are necessary to get the maximum benefit." [p. 550]

Peephole optimization: redundant LD/ST

LD RO, a ST a, RO

If the ST instruction has a label, cannot remove it. (If instructions are in the same block we're OK.)

This case takes several slides...



if E=K gobo L1 gobo L2 L1: ...do something...

L2: ... do something...

• • •

Eliminate jumps over jumps





if El=K goto L2 if E=K goto L1 goto L2 1. ... 2. 12: ... If E is set to a constant value other than K, then...

if E=K goto L1 if true goto L2 goto L2 1. ... 2. 12:conditional jump becomes unconditional...

if E=K goto L1 goto L2 goto L2 1. 12:and the unreachable code can be removed.

9060 L1 ... L1: 9060 L2

gobo L1 L1: gobo L2 gobo L2L1: gobo L2...





if a < b goto L1 if a < b goto L2 L1: goto L2 ... 12: L2: ...similar arguments can be made for conditional jumps.

Oplimization

- The semantics of a program must be preserved by optimizations.
- The compiler does not know a programmer's intent - it can only reason about the program as written.

Dala-flow analysis

View program execution as a sequence of state transformations.

Each program state consists of all
the variables in the program along
with their current values.

State transformation



State transformation



Dala-flow analysis

Begin by considering only the flow
graph for a single function.

Properties

- @ Wilhin a basic block:
 - Program point after a statement is same as program point before the next statement.
 - Why?

Properties

o Between basic blocks:

- "If there is an edge from block B1 to block B2, then the program point after the last statement of B1 may be followed immediately by the program point before the first statement of B2."

[p. 597]

Execution path

"An execution path (or just path) from point p_1 to point p_n [is] a sequence of points p_1 , p_2 , ..., p_n such that for each i = 1, 2, ..., n-1, either

1. p_i is the point immediately preceding a statement and p_{i+1} is the point immediately following that same statement, or

2. p_i is the end of some block and p_{i+1} is the beginning of a successor block."

[p. 597]

Example 9.8 (p. 598)

(1)d1: a = 1B1Path: (1,2,3,4,9) (2) Path: (1,2,3,4,5,6,7,8,3,4,9) (3)if read() <= 0 goto B4 **B**2 a has value 1 first (4 time (5) is executed. (5) d1 reaches (5) on B3 d2: b = athe first iteration. (6) $d_3: a = 243$ (7)a has value 243 goto B2 at (5) on the second (8)and subsequent iterations. (9) d3 reaches (5) on those iterations.

Program points

Reaching definitions

"The definitions that may reach a program point along some path are known as reaching definitions."

[p. 598]

Gathering different data for different uses

to determine possible values

"... at point (5) ... the value of a is one of { 1 , 243 } and ... it may be defined by one of { d1 , d3 }." [p. 598]

"... at point (5) ... there is no definition that must be the definition of a at that point, so this set is empty for a at point (5). Even if a variable has a unique definition at a point, that definition must assign a constant to the variable. Thus, we may simply describe certain variables as 'not a constant', instead of collecting all their possible values or all their possible definitions."

[p. 599]

for 'constant folding'

9.2.2 Data-flow analysis schema

"In each application of data-flow analysis, we associate with every program point a dataflow value that represents an abstraction of the set of all possible program states that can be observed at that point." [p. 599]

"The set of possible data-flow values is the domain..." [p. 599]

"We denote the data-flow values before and after each statements by IN[s] and OUT[s], respectively." [p. 599]

9.2.2 Data-flow analysis schema

"The data-flow problem is to find a solution to a set of constraints on the IN[s]'s and OUT[s]'s, for all statements s. There are two sets of constraints: those based on the semantics of the statements ("transfer functions") and those based on the flow of control." [p. 599]

Transfer functions

Information can flow forwards or backwards.

Forward flow: $OUT[s] = f_s (IN[s])$ Backward flow: $IN[s] = g_s (OUT[s])$

Control flow constraints

In a sequence s1, s2, ..., sn without jumps, $IN[s_{i+1}] = OUT[s_i]$ for all i=1,2,...,n-1For data-flow between blocks, take "the union of the definitions after last statements of each of the predecessor blocks." [p. 600]

9.2.3 Data-flow schemas on basic blocks

Suppose a basic block B consists of the sequence of statements $s_1, s_2, ..., s_n$. Define $IN[B] = IN[S_1]$ and $OUT[B] = OUT[S_n]$.

The transfer function of B:

$$f_B = f_{sn} \circ \cdots \circ f_{s2} \circ f_{s1}$$

The transfer function of B: $OUT[B] = f_B(IN[B])$

9.2.3 Data-flow schemas on basic blocks

Forward flow problem $OUT[B] = f_B(IN[B])$ IN[B] = UP a predecessor of B OUT[P] Backward flow problem IN[B] = 9B(OUT[B])OUT[B] = US a successor of B IN[S]
9.2.3 Data-flow schemas on basic blocks

"...data-flow equations usually do not have a unique solution. Our goal is to find the most 'precise' solution that satisfies the two sets of constraints: control-flow and transfer constraints. That is, we need a solution that encourages valid code improvements, but does not justify unsafe transformations..."

[p. 601]

"A definition d reaches a point p if there is a path from the point immediately following d to p, such that d is not 'killed' along that path." [p. 601]

"We kill a definition of a variable x if there is any other definition of x anywhere along the path." [p. 601]

"A definition of a variable x is a statement that assigns, or may assign, a value to x."

What is meant by "may assign"?

"Procedure parameters, array accesses, and indirect references all may have aliases, and it is not easy to tell if a statement is referring to a particular variable x." [p. 601]

"Program analysis must be conservative" [p. 601]

Transfer equations for reaching definitions For this definition: d: u = v + wσ is a dataflow value The transfer equation is: $f_d(\sigma) = gend \cup (\sigma - killd)$ where gend = {d}. killd is the set of all other definitions of u in the program The argument of a transfer function is a data-flow value, which "represents an abstraction of the set of all possible program states that can be observed for that point." [p. 599] Recall too that a program state consists of all the variables

in the program along with their current values.











 $gen_{B1} = \{ d1, d2, d3 \}$ kill_{B1} = $\{ d4, d5, d6, d7 \}$

Q: Why kill d4 - d7 here, since they are not on a path to B1?

A: Here we are looking just at this block, and not trying to account for flow between blocks.

Inter-block flow is taken into account later.















Extending transfer equations from statements to blocks

Composition of f1 and f2: $f_1(x) = gen_1 \cup (x - kill_1)$ $f_2(x) = gen_2 \cup (x - kill_2)$ $f_2(f_1(x)) = gen_2 \cup ((gen_1 \cup (x - kill_1)) - kill_2)$ = genz \cup ((gen_1 - kill_2) \cup ((x - kill_1) - kill_2)) = genz \cup (gen1 - kill2) \cup (x - (kill1 \cup kill2))

Extending transfer equations from statements to blocks

In general:

 $f_B(x) = gen_B \cup (x - kill_B)$ kill_B = $U_{i\in n}$ kill_i

```
gens = genn U
(genn-2 - killn) U
(genn-2 - killn-2 - killn) U
... U
(gen1 - kill2 - kill3 - ... - killn)
```

Extending transfer equations from statements to blocks

"The gen set contains all the definitions inside the block that are "visible" immediately after the block – we refer to them as downwards exposed. A definition is downwards exposed in a basic block only if it is not "killed" by a subsequent definition to the same variable inside the same basic block." [p. 605] Iterative algorithm for reaching definitions

Algorithm [p. 606]

INPUT: A flow graph for which kills and gens have been computed for each block B.

OUTPUT: IN[B] and OUT[B], the set of definitions reaching the entry and exit of each block B of the flow graph

```
METHOD:

OUT[ENTRY] = 0

for (each basic block B other than ENTRY) { OUT[B] = 0 }

while (changes to any OUT occurs) {

for (each basic block B other than ENTRY) {

IN[B] = U<sub>P a predecessor of B</sub> OUT[P]

OUT[B] = genB U (IN[B] - kill<sub>B</sub>)
```

Iterative algorithm for reaching definitions

Algorithm [p. 606]

INPUT: A flow graph for which H each block B.

OUTPUT: IN[B] and OUT[B], the and exit of each block B of the

Written this way to allow different entry conditions for different data flow algorithms.

METHOD:

OUT[ENTRY] = 0 for (each basic block B other than ENTRY) { OUT[B] = 0 } while (changes to any OUT occurs) { for (each basic block B other than ENTRY) { IN[B] = U_{P a predecessor of B} OUT[P] OUT[B] = genB U (IN[B] - kill_B)



Example 9.12 - building off figure 9.13 OUT[ENTRY] = Ø for (each basic block B other than ENTRY) { OUT[B] = Ø } while (changes to any OUT occurs) { for (each basic block B other than ENTRY) { IN[B] = UP a predecessor of B OUT[P] OUT[B] = genB U (IN[B] - killB)

	OUT[B]0	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2	
B1	Represent di o	ls a bit vector	; where each d	l is a definiti	on from 9.13	
B2	Union of sets	A U B: A OR B	Differen	nce of sets A ·	- B: A AND B'	
B3	Compute in order B1, B2, B3, B4, EXIT For example: INFB271 = OUTFB171 11 OUTFB470 = 111 0000 11 000 0000 = 111 0000					
B4	$OUT[B2]^1 = ge$	$n_{B2} \cup (IN[B2]^1$	- kill _{B2})			
EXIT		= 000 1100 + = 000 1100 +	(111 0000 - 11 001 0000 = 00	0 0001) 1 1100		

Example 9.12 - building off figure 9.13 OUT[ENTRY] = 0 for (each basic block B other than ENTRY) { OUT[B] = 0 } while (changes to any OUT occurs) { for (each basic block B other than ENTRY) { IN[B] = UP a predecessor of B OUT[P] OUT[B] = genB U (IN[B] - killB)

	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000				
B2	000 0000				
B3	000 0000				
B4	000 0000				
EXIT	000 000				

ENTRY B1 d1: i = m - 1OUT[ENTRY] = Ø d2: j = n $d_3: a = u_1$ for (each basic block B other than ENTRY) { $OUT[B] = \emptyset$ } while (changes to any OUT occurs) { B2 d4: i = i + 1for (each basic block B other than ENTRY) { ds: j = j - 1IN[B] = UP a predecessor of B OUT[P]B.3. d6: a = u2OUT[B] = genb u (IN[B] - killb) **B4** d7: i = u3EXIT OUT[B] IN[B]1 OUT[B]1 IN[B]2 OUT[B]2 **B1** 000 0000 000 0000 111 0000 000 0000 IN[B1] = pred(B1) = ENTRY **B**2 $OUT[B1] = gen_{B1} \cup (IN[B1] - kill_{B1})$ 000 0000 gen $B1 = \{ d1, d2, d3 \}$ **B**3 $kill_{B1} = \{ d4, d5, d6, d7 \}$ 000 0000 **B4** EXIT 000 0000

 $\begin{array}{l} \text{OUT[ENTRY]} = \emptyset \\ \text{for (each basic block B other than ENTRY) } \text{OUT[B]} = \emptyset \\ \text{while (changes to any OUT occurs) } \\ \text{for (each basic block B other than ENTRY) } \\ \text{IN[B]} = UP \text{ a predecessor of B OUT[P]} \\ \text{OUT[B]} = \text{geng } U \text{ (IN[B] - kill_B)} \\ \\ \end{array}$

	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000	000 0000	111 0000		
B2	000 0000	111 0000	001 1100		
B3	000 0000	IN[B2] = p	red(B2) = 0	$UT[B1] \cup O$	UT[B4]
B4	000 0000	$gen_{B2} = \{ d$	4, d5	NTORT - MUR	
EXIT	000 0000	$Kill_{B2} = \{ d \}$	(1, d2, d7)		

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ENTRY

EXIT

B1

B2

 $\begin{array}{l} \text{OUT[ENTRY]} = \emptyset \\ \text{for (each basic block B other than ENTRY) } \left\{ \begin{array}{l} \text{OUT[B]} = \emptyset \end{array} \right\} \\ \text{while (changes to any OUT occurs) } \\ \text{for (each basic block B other than ENTRY) } \\ \text{IN[B]} = UP a \text{ predecessor of B OUT[P]} \\ \text{OUT[B]} = gen_B \cup (IN[B] - kill_B) \\ \end{array} \right\} \\ \begin{array}{l} \text{d1: } i = m-1 \\ d2: j = n \\ d3: a = u1 \\ d4: i = i+1 \\ d5: j = j-1 \\ d5: j = j-1 \\ d5: j = j-1 \\ d6: a = u2 \\ d6: a = u2 \\ d7: i = u3 \\ \end{array}$

	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000	000 0000	111 0000		
B2	000 0000	111 0000	001 1100		
B3	000 0000	001 1100	000 1110		
B4	000 0000	IN[B3] = pred(B3) = OUT[B2] OUT[B3] = gen_B3 U (IN[B3] - kill_B3)			
EXIT	000 0000	$gen_{B3} = \{ d6 \}$ kill_{B3} = $\{ d3 \}$	}		

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ENTRY

EXIT

B1

B2

 $\begin{array}{l} \text{OUT[ENTRY]} = \emptyset \\ \text{for (each basic block B other than ENTRY) } \text{OUT[B]} = \emptyset \\ \text{while (changes to any OUT occurs) } \\ \text{for (each basic block B other than ENTRY) } \\ \text{IN[B]} = UP a \text{ predecessor of B OUT[P]} \\ \text{OUT[B]} = \text{genb} \cup (\text{IN[B]} - \text{kill}_B) \\ \\ \end{array}$

	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000	000 0000	111 0000		
B2	000 0000	111 0000	001 1100		
B3	000 0000	001 1100	000 1110		
B4	000 0000	001 1110	001 0111	$gen_{B4} = \{ d7 \}$ kill _{B4} = $\{ d1, \}$	d4 }
EXIT	000 0000	$IN[B4] = OUT[B2] \cup OUT[B3]$ $OUT[B4] = gen_{B4} \cup (IN[B4] - kill_{B4})$			

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ENTRY

EXIT

B1

B2

 $\begin{array}{l} \text{OUT[ENTRY]} = \emptyset \\ \text{for (each basic block B other than ENTRY) } \text{OUT[B]} = \emptyset \\ \text{while (changes to any OUT occurs) } \\ \text{for (each basic block B other than ENTRY) } \\ \text{IN[B]} = \cup_{P a \text{ predecessor of B OUT[P]}} \\ \text{OUT[B]} = \operatorname{geng} \cup (IN[B] - kill_B) \\ \\ \end{array}$

	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000	000 0000	111 0000		
B2	000 0000	111 0000	001 1100		
B3	000 0000	001 1100	000 1110		
B4	000 0000	001 1110	001 0111		
EXIT	000 0000	001 0111	001 0111	IN[EXIT] = 0 OUT[EXIT] =	UT[B4] IN[EXIT]

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ENTRY

EXIT

B1

B2





	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000	000 0000	111 0000	000 0000	111 0000
B2	000 0000	111 0000	001 1100	111 0111	001 1110
B3	000 0000	001 1100	000 1110		
B4	000 0000	001 1110	001 0111		
EXIT	000 0000	001 0111	001 0111		



	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000	000 0000	111 0000	000 0000	111 0000
B2	000 0000	111 0000	001 1100	111 0111	001 1110
B3	000 0000	001 1100	000 1110	001 1110	000 1110
B4	000 0000	001 1110	001 0111		
EXIT	000 0000	001 0111	001 0111		



	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000	000 0000	111 0000	000 0000	111 0000
B2	000 0000	111 0000	001 1100	111 0111	001 1110
B3	000 0000	001 1100	000 1110	001 1110	000 1110
B4	000 0000	001 1110	001 0111	001 1110	001 0111
EXIT	000 0000	001 0111	001 0111		



	OUT[B]°	IN[B]1	OUT[B]1	IN[B]2	OUT[B]2
B1	000 0000	000 0000	111 0000	000 0000	111 0000
B2	000 0000	111 0000	001 1100	111 0111	001 1110
B3	000 0000	001 1100	000 1110	001 1110	000 1110
B4	000 0000	001 1110	001 0111	001 1110	001 0111
EXIT	000 0000	001 0111	001 0111	001 0111	001 0111

Useful for constant propagation and constant folding (§8.5.4 - p. 536, §9.4 - p. 632). Additional discussion and examples:

en.wikipedia.org/wiki/Constant_folding

Useful for global common subexpression elimination (§9.1.4 - p. 588, §9.2.6 - p. 610, §9.5 p. 639). Additional discussion and examples:

en.wikipedia.org/wiki/Common_subexpression_elimination
9.2.5 Live variable analysis

Useful for effective register management.

"After a value is computed in a register, and presumably used within a block, it is not necessary to store that value if it is dead at the end of the block. Also, if all registers are full and we need another register, we should favor using a register with a dead value, since that value does not have to be stored." [p. 608]

9.2.5 Live variable analysis

"In live variable analysis we wish to know for variable x and point p whether the value of x at p could be used along some path in the flow graph starting at p. If so, we say x is live at p; otherwise, x is dead at p." [p. 608]

In contrast to reaching analysis, which used a forward transfer function, live variable analysis uses a backward transfer function.

9.2.5 Live variable analysis definitions, page 609

def is "the set of variables defined in B prior to any use of that variable in B"

uses is "the set of variables whose values may be used in B prior to any definition of the variable" 9.2.5 Live variable analysis definitions, page 609

 $IN[EXIT] = \emptyset$ $IN[B] = use_B \cup (OUT[B] - def_B)$ $OUT[B] = U_{S a successor of B} IN[S]$

9.2.5 Live variable analysis Algorithm [p. 610]

INPUT: A flow graph with def and use computed for each block.

OUTPUT: IN[B] and OUT[B], the set of variables live on entry and exit of each block of the flow graph.

```
METHOD:

IN[EXIT] = Ø

for (each basic block B other than EXIT) { IN[B] = Ø }

while (changes to any IN occur) {

for (each basic block B other than EXIT) {

OUT[B] = Use B other than EXIT) {

IN[B] = use U (OUT[B] - defb)
```

"An expression x+y is available at a point p if every path from the entry node to p evaluates to x+y, and after the last such evaluation prior to reaching p, there are no subsequent assignments to x or y." [p. 610]

"...a block kills expression x+y if it assigns (or may assign) x or y and does not subsequently recompute x+y." [p. 610]

"A block generates expression x+y if it definitely evaluates x+y and does not subsequently define x or y." [p. 611]

FLAUTE 9.17



"...the expression 4 * i in block B3 will be a common subexpression if 4 * i is available at the entry point of block B3." [p 611]





"It will be available if i is not assigned a new value in block B2, ..." [p 611]

Here 4 * i in B3 can be replaced by value of £1, regardless of which branch is taken.

Figure 9.17

"... or if ... 4 * i is recomputed after i is assigned in B2." [p 611]

Again, 4 * i in B3 can be replaced by value of t1, regardless of which branch is taken (since t1 contains the correct value of 4 * i in both cases)



9.2.6 Available expressions Informally:

"If at point p set S of expressions is available, and q is the point after p, with statement x=y+z between them, then we form the set of expressions available at q by the following steps:

1. Add to 5 the expression y+z. 2. Delete from 5 any expression involving variable x."

[p. 611]

Example 9.15

Statement	Available expressions
	Ø
a = b + c	
	{b+c}
b=a-d	
	{a-d}
c = b + c	
	$\{a-d\}$
d = a - d	
	Ø

"We can find available expressions in a manner reminiscent of the way reaching definitions are computed. Suppose U is the 'universal' set of all expressions appearing on the right of one or more statement of the program. For each block B, let IN[B] be the set of expressions in U that are available at the point just before the beginning of B. Let OUT[B] be the same for the point following the end of B. Define e_gens to be the expressions generated by B and e_kills to be the set of expressions in U killed in B. Note that IN, OUT, egen, and e kill can all be represented by bit vectors." [p. 612]

9.2.6 Available expressions definitions, page 612

OUT[ENTRY] = \emptyset OUT[B] = e_genb n (IN[B] - e_killb) IN[B] = $\bigcap_{P \ a \ predecessor \ of \ B}$ OUT[P]

9.2.6 Available expressions definitions, page 612

 $OUT[ENTRY] = \emptyset$ $OUT[B] = e_gen_B \cap (IN[B] - e_kill_B)$ $IN[B] = \bigcap_{P \ a \ predecessor \ of \ B} OUT[P]$

Note use of Π rather than U. "...an expression is available at the beginning of a block only if it is available at the end of ALL its predecessors." [p. 612]

Algorithm [p. 614]

INPUT: A flow graph with e_kill_B and e_gen_B computed for each block B. The initial block is B1.

OUTPUT: IN[B] and OUT[B], the set of expressions available at the entry and exit of each block of the flow graph.

METHOD:

OUT[ENTRY] = Ø for (each basic block B other than ENTRY) { OUT[B] = U } while (changes to any OUT occur) { for (each basic block B other than EXIT) { IN[B] = ∩P a predecessor of B OUT[P] OUT[B] = e_genB ∩ (IN[B] - e_kill_B)

Algorithm [p. 614]

INPUT: A flow graph with e_kill_B and e_gen_B computed for each block B. The initial block is B1.

OUTPUT: IN[B] and OUT[B], the set of expressions available at the entry and exit of each block of the flow graph.

METHOD:

 $\begin{array}{l} \text{OUT[ENTRY]} = \emptyset \\ \text{for (each basic block B other than ENTRY) } \left\{ \begin{array}{l} \text{OUT[B]} = U \right\} \\ \text{while (changes to any OUT occur) } \\ \text{for (each basic block B other than EXIT) } \\ \text{IN[B]} = \bigcap_{P \text{ a predecessor of B OUT[P]}} \\ \text{OUT[B]} = e_gen_B \cap (IN[B] - e_kill_B) \end{array} \right\} \\ \begin{array}{l} \text{Recall: U is} \\ \text{set of all} \end{array}$

expressions



	Reaching definitions	Live variables	Available expressions
Domain	sets of definitions	sets of variables	sets of expressions
Direction	forward	backward	forward
Transfer function	genb U (x - killb)	use U(x - defb)	e_gens $\bigcap (x - e_kill_B)$
Boundary	$OUT[ENTRY] = \emptyset$	$IN[EXIT] = \emptyset$	$OUT[ENTRY] = \emptyset$
Meet (^)	U	U	Γ
Equations	$OUT[B] = f_B(IN[B])$ $IN[B] = \Lambda_{P,pred(B)}OUT[P]$	$IN[B] = f_B(OUT[B])$ $OUT[B] = \Lambda_{S,succ(B)}IN[S]$	$OUT[B] = f_B(IN[B])$ $IN[B] = \Lambda_{P,pred(B)}OUT[P]$
Initialize	$OUT[B] = \emptyset$	$IN[B] = \emptyset$	OUT[B] = U