Phases of a compiler

Intermediate Representation (IR): specification and generation

Figure 1.6, page 5 of text
Intermediate Representations
Directed Acyclic Graph (DAG)

- Similar to a syntax tree
- No repeated nodes: structure sharing
Ex. 6.1 [p 359]

\[ a + a \times (b - c) + (b - c) \times d \]
Ex. 6.1 [p 359]

\[ a + a \ast (b - c) + (b - c) \ast d \]
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Things can be more complicated if expressions have side effects.
### SDT

**Tree or DAG**

<table>
<thead>
<tr>
<th>Production</th>
<th>Semantic Rule</th>
</tr>
</thead>
<tbody>
<tr>
<td>$E \rightarrow E_1 + T$</td>
<td>$E$.node = new Node('+', E.node, T.node)</td>
</tr>
<tr>
<td>$E \rightarrow E_1 - T$</td>
<td>$E$.node = new Node('-', E.node, T.node)</td>
</tr>
<tr>
<td>$E \rightarrow E_1 * T$</td>
<td>$E$.node = new Node('*', E.node, T.node)</td>
</tr>
<tr>
<td>$E \rightarrow T$</td>
<td>$E$.node = T.node</td>
</tr>
<tr>
<td>$T \rightarrow (E)$</td>
<td>$T$.node = E.node</td>
</tr>
<tr>
<td>$T \rightarrow id$</td>
<td>$T$.node = new Leaf(id, id.entry)</td>
</tr>
<tr>
<td>$T \rightarrow num$</td>
<td>$T$.node = new Leaf(num, num.val)</td>
</tr>
</tbody>
</table>

*Figure 6.4 in text (p. 360), corrected according to errata sheet.*
SDT

Tree or DAG

- SDT produces a tree if each call to Node creates a new tree node.

- SDT produces a DAG if for each call to Node there is a check whether this node already exists, and if so it returns a reference to the existing node rather than returning a new node.
Example

\[
\begin{align*}
  p_1 &= \text{Leaf}(id, \text{entry-a}) \\
  p_2 &= \text{Leaf}(id, \text{entry-a}) = p_1 \\
  p_3 &= \text{Leaf}(id, \text{entry-b}) \\
  p_4 &= \text{Leaf}(id, \text{entry-c}) \\
  p_5 &= \text{Node}('-', p_3, p_4) \\
  p_6 &= \text{Node}('*', p_1, p_5) \\
  p_7 &= \text{Node}('+', p_1, p_6) \\
  p_8 &= \text{Leaf}(id, \text{entry-b}) = p_3 \\
  p_9 &= \text{Leaf}(id, \text{entry-c}) = p_4 \\
  p_{10} &= \text{Node}('-', p_3, p_4) = p_5 \\
  p_11 &= \text{Leaf}(id, \text{entry-d}) \\
  p_{12} &= \text{Node}('*', p_5, p_{11}) \\
  p_{13} &= \text{Node}('+', p_7, p_{12})
\end{align*}
\]
Value-number method
Algorithm 6.3 [p. 361]

- **Input:** label op, node l, node r
- **Output:** The value number of a node in the array with signature <op,l,r>
- **Method:** Search the array for a node M with signature <op,l,r>. If there is such a node, return the value number of M. If not, create in the array a new node N with signature <op,l,r> and return its value number.
Value-number method
Algorithm 6.3 [p. 361]

- **Input:** label op, node l, node r
- **Output:** The value number of a node in the array with signature <op,l,r>
- **Method:** Search the array for a node M with signature <op,l,r>. If there is such a node, return the value number of M. If not, create in the array a new node N with signature <op,l,r> and return its value number.

Can use hash table for efficiency.
Revisiting 6.1
see construction steps in figure 6.5 [p. 360]

<p>| | | |</p>
<table>
<thead>
<tr>
<th></th>
<th></th>
<th></th>
</tr>
</thead>
<tbody>
<tr>
<td>1</td>
<td>id</td>
<td>→ to ST entry for a</td>
</tr>
<tr>
<td>2</td>
<td>id</td>
<td>→ to ST entry for b</td>
</tr>
<tr>
<td>3</td>
<td>id</td>
<td>→ to ST entry for c</td>
</tr>
<tr>
<td>4</td>
<td>-</td>
<td>2</td>
</tr>
<tr>
<td>5</td>
<td>*</td>
<td>1</td>
</tr>
<tr>
<td>6</td>
<td>+</td>
<td>1</td>
</tr>
<tr>
<td>7</td>
<td>id</td>
<td>→ to ST entry for d</td>
</tr>
<tr>
<td>8</td>
<td>*</td>
<td>4</td>
</tr>
<tr>
<td>9</td>
<td>+</td>
<td>6</td>
</tr>
</tbody>
</table>
Three-address code

- The DAG does not say anything about how the computation should be carried out.
- For example, there could be one instruction to do this computation:
  \[ t_1 = x + y \times z \]
Three-address code

- In three-address code instructions can have no more than one operator on the right of an assignment.

- \(x+y \times z\) must be broken into two instructions:
  \[t_1 = y \times z\]
  \[t_2 = x + t_1\]
Three address code is a linearized representation of ... a DAG in which explicit names correspond to the interior nodes of the graph. [p. 363]

\[ t_1 = b - c \]
\[ t_2 = a \times t_1 \]
\[ t_3 = a + t_2 \]
\[ t_4 = t_1 \times d \]
\[ t_5 = t_3 + t_4 \]
Three address code instructions
(see 6.2.1, pages 364-5)

1. \( x = y \ op \ z \)
2. \( x = \ op \ y \) (treat i2r and r2i as unary ops)
3. \( x = y \)
4. goto L
5. if \( x \) goto L / ifFalse \( x \) goto L
6. if \( x \) relop \( y \) goto L
7. function calls:
   - param \( x \)
   - call p, n
   - \( y = \) call p
   - return \( y \)
8. \( x = y[i] \) and \( x[i] = y \)
9. \( x = &y, \ x = *y, \ *x = y \)
"The description of three-address instructions specifies the components of each type of instruction, but it does not specify the representation of these instructions in a data structure."

[p. 366]
Quadruples

Instructions have four fields:
   op, arg1, arg2, result

Example: \( t_3 = a + t_2 \) is represented as

<table>
<thead>
<tr>
<th>op</th>
<th>arg1</th>
<th>arg2</th>
<th>result</th>
</tr>
</thead>
<tbody>
<tr>
<td>+</td>
<td>a</td>
<td>( t_2 )</td>
<td>( t_3 )</td>
</tr>
</tbody>
</table>

Example: \( t_4 = - c \) is represented as

<table>
<thead>
<tr>
<th>op</th>
<th>arg1</th>
<th>arg2</th>
<th>result</th>
</tr>
</thead>
<tbody>
<tr>
<td>minus</td>
<td>c</td>
<td></td>
<td>( t_4 )</td>
</tr>
</tbody>
</table>
Quadruples

Identifiers would be pointers to symbol table entries. Compiler-introduced temporaries can be added to the symbol table.

<table>
<thead>
<tr>
<th>op</th>
<th>arg1</th>
<th>arg2</th>
<th>result</th>
</tr>
</thead>
<tbody>
<tr>
<td>+</td>
<td>→ entry for a</td>
<td>→ entry for t₂</td>
<td>→ entry for t₃</td>
</tr>
</tbody>
</table>
Triples

Instructions have three fields:
\text{op}, \text{arg1}, \text{arg2}

Example:
\[ t_2 = \ldots \]
\[ t_3 = a + t_2 \] is represented as

\[
\begin{array}{|c|c|c|c|}
\hline
\text{line} & \text{op} & \text{arg1} & \text{arg2} \\
\hline
5 & \text{computation of } t_2 & \text{arg1} & \text{arg2} \\
\hline
6 & + & a & (5) \\
\hline
\end{array}
\]
Indirect triples

Because order matters (due to embedded references instead of explicit variables) it is more challenging to rearrange instructions with triples than with quadruples.

Indirect triples allow for easier reordering (see page 369).
Static Single Assignment (SSA) 
an additional constraint on the three address code

1) Each variable is assigned to exactly once.

\[
\begin{align*}
    x &= r + 1 \\
    y &= s \times 2 \\
    x &= 2 \times x + y \\
    y &= y + 1 \\
    x_1 &= r + 1 \\
    y_1 &= s \times 2 \\
    x_2 &= 2 \times x_1 + y_1 \\
    y_2 &= y_1 + 1
\end{align*}
\]
Static Single Assignment (SSA) is an additional constraint on the three address code.

1) Each variable is assigned to exactly once.

2) Need $\phi$ function to merge split variables:

\[
\text{if (e) then } \{ x = a \} \text{ else } \{ x = b \} \\
y = x
\]

With SSA:

\[
\text{if (e) then } \{ x_1 = a \} \text{ else } \{ x_2 = b \} \\
y = \phi(x_1, x_2)
\]
\( \phi \) function implementation

In \( y = \phi(x_1, x_2) \) simply let \( y, x_1 \) and \( x_2 \) be bound to the same address.
Type equivalence

Name equivalence: two types are equivalent if and only if they have the same name.

Structural equivalence: two types are equivalent if and only if they have the same structure. A type is structurally equivalent to itself (i.e. int is both name equivalent and structurally equivalent to int)
Name equivalence

```c
int x = 3;
int y = 5;
int z = x * y;
```

The type of `z` is `int`.
The type of `x * y` is `int`.
The names of the types are the same, so the assignment is legal.
Structural equivalence

```c
struct S { int v; double w; };
struct T { int v; double w; };

int main() {
    struct S x;
    x.v = 1; x.w = 4.5;
    struct T y;
    x = y;
    return 0;
}
```

Under name equivalence the assignment is disallowed.

Under structural equivalence the assignment is permitted.

What does C do?
C does not allow the assignment

bash-3.2$ gcc type.c
type.c:9:5: error: assigning to 'struct S' from incompatible type 'struct T'
  x = y;
  ~ ~
1 error generated.
Structural equivalence

struct S { int v; double w; };
struct T { int a; double b; };

int main() {
    struct S x;
    x.v = 1; x.w = 4.5;
    struct T y;
    x = y;
    return 0;
}
Consider...

```c
struct Rectangular { double x; double y; }
struct Polar { double r; double theta; }

int main() {
    struct Rectangular p;
    p.x = 3.14; x.y = 3.14;
    struct Polar q;
    q = p;
    return 0;
}
```

Should this be allowed?
Interpretation matters

polar interpretation

rectangular interpretation
Our language
(use name equivalence)

- primitive types: integer, real, Boolean, character, string
- user-defined types:
  - record types have names
    - type rec : [ real : x := 0, y := 0 ]
  - array types have names
    - type arr : 2 -> string
  - function types have names
    - type fun : ( real : x ) -> rec
Recursive records

A record type must allow a component to be of the same type as the type itself:

```
type Node: [ integer datum:=0 ; Node rest:=null ]
```