



Parallel Odd-Even Transposition Sort using MPI

CSE 633: Parallel Algorithms

Course Instructor: Dr. Russ Miller

UB Distinguished Professor

**Department of Computer Science & Engineering
State University of New York at Buffalo**

Prepared by: Asif Imran (UB Person number: 50249959)

Agenda



- Overview of the project
- Proposed algorithm with justification
- Architecture of the solution
- Experimentation in CCR
- Obtained results and analysis
- Challenges
- Learnings
- Conclusion and Future Work



Overview of the project

Odd-Even Transposition sorting

Think fo Bubble sort

The diagram illustrates the four steps of Odd-Even Transposition sorting on an array of 8 elements (A[0] to A[6]). Each step shows a comparison between adjacent elements, with a curved arrow indicating the direction of comparison. The elements are represented as a 2D table:

| | | | | | | |
|------|------|------|------|------|------|------|
| A[0] | A[1] | A[2] | A[3] | A[4] | A[5] | A[6] |
| 1 | 2 | 9 | 7 | 6 | 10 | 11 |

Step 1: A comparison between A[0] and A[1] (1 and 2). The arrow points from A[0] to A[1].

| | | | | | | |
|------|------|------|------|------|------|------|
| A[0] | A[1] | A[2] | A[3] | A[4] | A[5] | A[6] |
| 1 | 2 | 7 | 9 | 6 | 10 | 11 |

Step 2: A comparison between A[2] and A[3] (7 and 9). The arrow points from A[2] to A[3].

| | | | | | | |
|------|------|------|------|------|------|------|
| A[0] | A[1] | A[2] | A[3] | A[4] | A[5] | A[6] |
| 1 | 2 | 7 | 6 | 9 | 10 | 11 |

Step 3: A comparison between A[4] and A[5] (9 and 10). The arrow points from A[4] to A[5].

| | | | | | | |
|------|------|------|------|------|------|------|
| A[0] | A[1] | A[2] | A[3] | A[4] | A[5] | A[6] |
| 1 | 2 | 6 | 7 | 9 | 10 | 11 |

Step 4: A comparison between A[6] and A[7] (11 and 11). The arrow points from A[6] to A[7].

Think of bubble sort....



- Unrealistic to parallelize
- Inherently sequential nature of the sort algorithms
- Why Odd-Even Transposition sort?
 - Bigger opportunity to parallelize
 - Key idea is to decouple the compare swaps
 - Consists of two different phases of sequence
 - For example: During even phases, compare swaps are executed on the even pairs and vice versa.

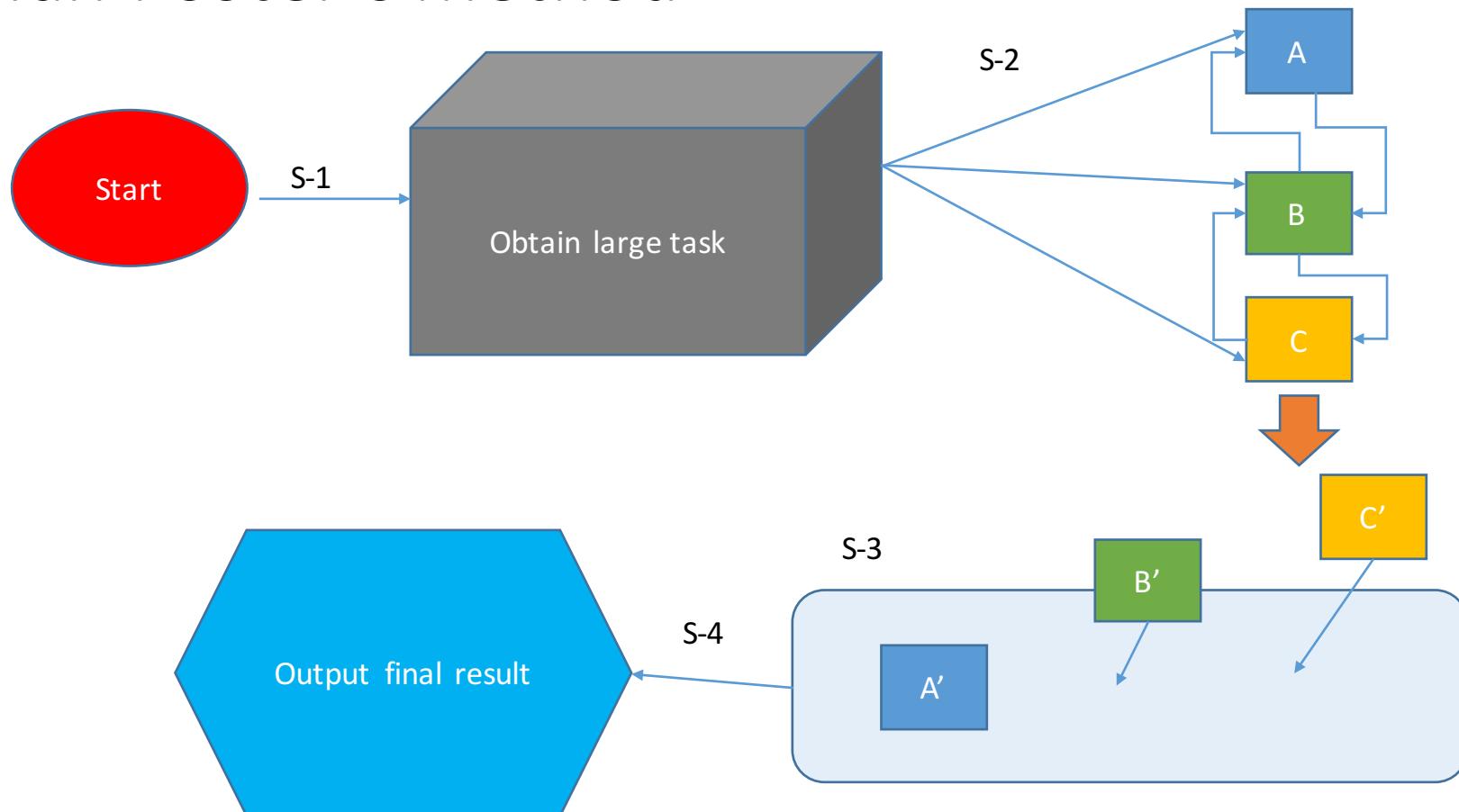
Goal of the project



- Design, implementation, and analyze parallel solution of interest on modern large-scale multiprocessor/multi-core systems. [1]
- Acclimatization to real life high performance multiprocessor computing environment and obtaining knowledge on how to use them.
- Use Foster's method [2]
- Use Amdahl's law for calculation of speedup [2]



Ian Foster's method



Pictorial depiction of odd-even sort mechanism

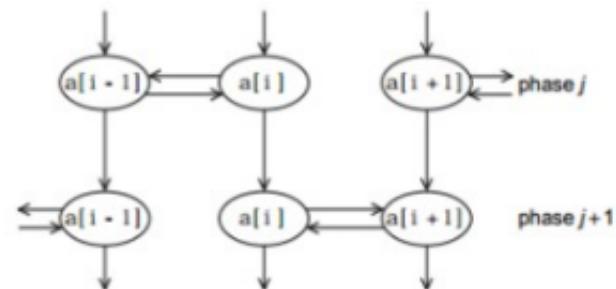


- Even positions

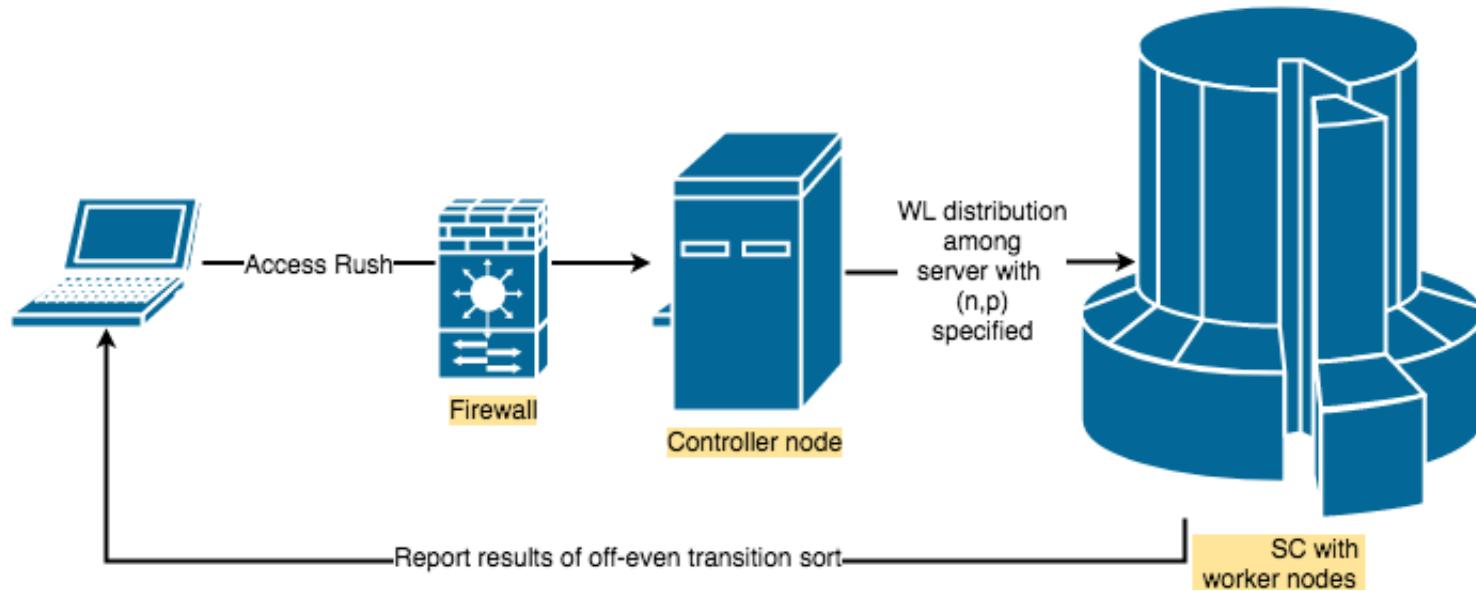
$(a[0], a[1]), (a[2], a[3]), (a[4], a[5]), \dots,$

- Odd positions

$(a[1], a[2]), (a[3], a[4]), (a[5], a[6]), \dots$



Architecture of Odd-Even Transposition sort



Experimentation



- Involved allocation of resources followed by execution of code to collect run-time
- Used script file
- Specified number of servers
- Specified number of CPUs
- Specified number of tasks per process
- Obtained –exclusive access to the resources
- Calculated speedup values using Amdahl's law

Script for running SLURM jobs



```
#!/bin/sh
#SBATCH --salloc
#SBATCH --partition=general-compute --qos=general-compute
#SBATCH --time=1:00:00
#SBATCH --nodes=16
#SBATCH --ntasks-per-node=1
#SBATCH --constraint=IB
#SBATCH --job-name= "Odd_Even"
#SBATCH --mail-user=asifimra@buffalo.edu
#SBATCH --mail-type=ALL
#SBATCH --requeue
# The initial srun will trigger the SLURM prologue on the compute nodes.
I_MPI_PMI_LIBRARY=/usr/lib64/libpmi.so srun
mpirun -np 16 ./oddeven2
echo "All Done!"
```

Server Configuration [4]

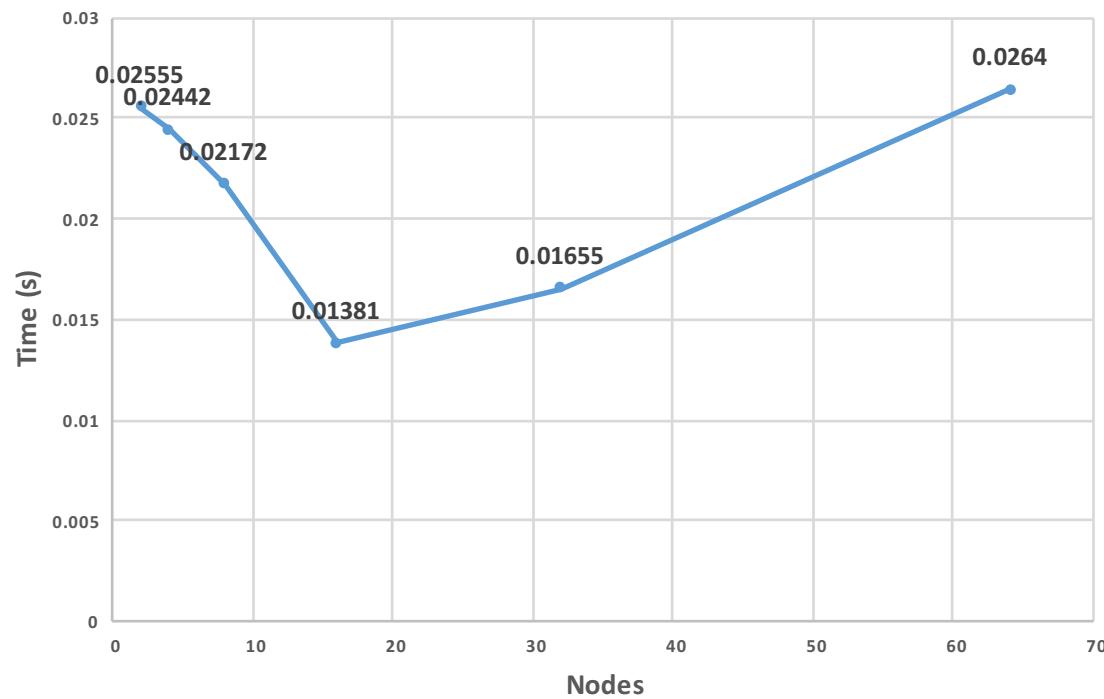


| Type of Node | Approximate # of Nodes | # Cores per Node | Clock Rate | RAM | Network* | SLURM TAGS |
|--------------|------------------------|------------------|------------|------|-----------------|--------------|
| Compute | 372 | 12 | 2.40GHz | 48GB | Infiniband (QL) | IB CPU-E5645 |



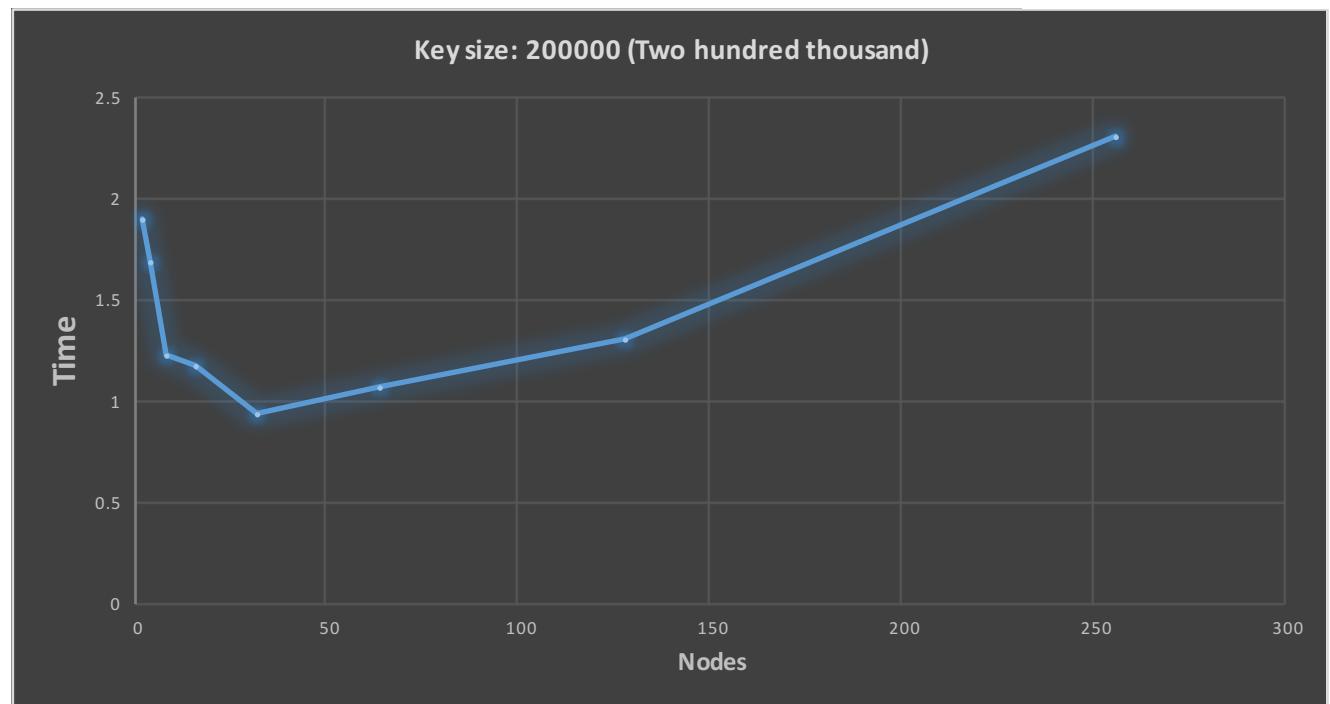
Key size 100000 (One hundred thousand)

| Key size: 100000 | |
|------------------|---------|
| Processors | Time |
| 2 | 0.02555 |
| 4 | 0.02442 |
| 8 | 0.02172 |
| 16 | 0.01381 |
| 32 | 0.01655 |
| 64 | 0.0264 |



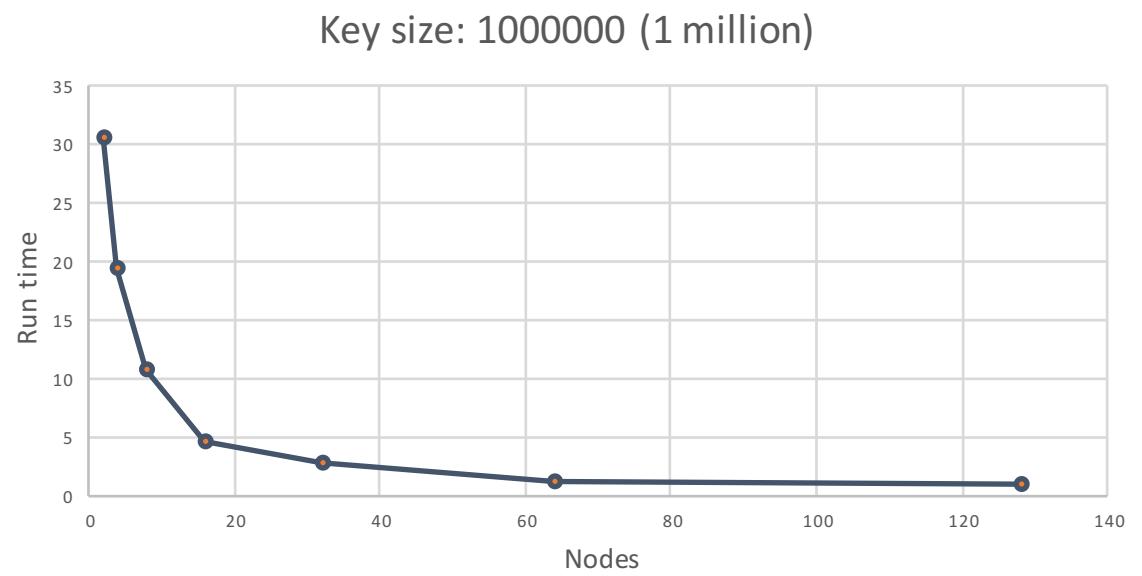


| Key size: 200000 | |
|------------------|--------|
| Processors | Time |
| 2 | 1.896 |
| 4 | 1.6833 |
| 8 | 1.2287 |
| 16 | 1.1688 |
| 32 | 0.934 |
| 64 | 1.07 |
| 128 | 1.311 |
| 256 | 1.610 |



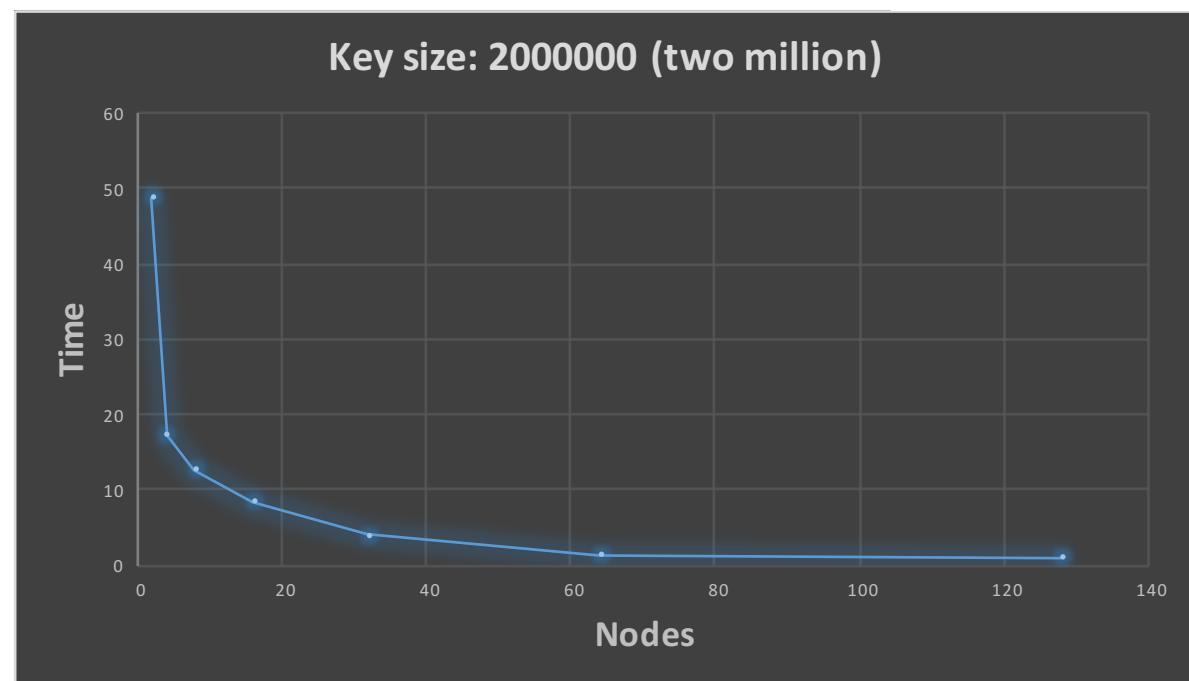


| Key size: 1000000 (1 million) | |
|-------------------------------|---------|
| Processors | Speedup |
| 2 | 30.609 |
| 4 | 19.447 |
| 8 | 10.799 |
| 16 | 4.649 |
| 32 | 2.873 |
| 64 | 1.329 |
| 128 | 0.901 |





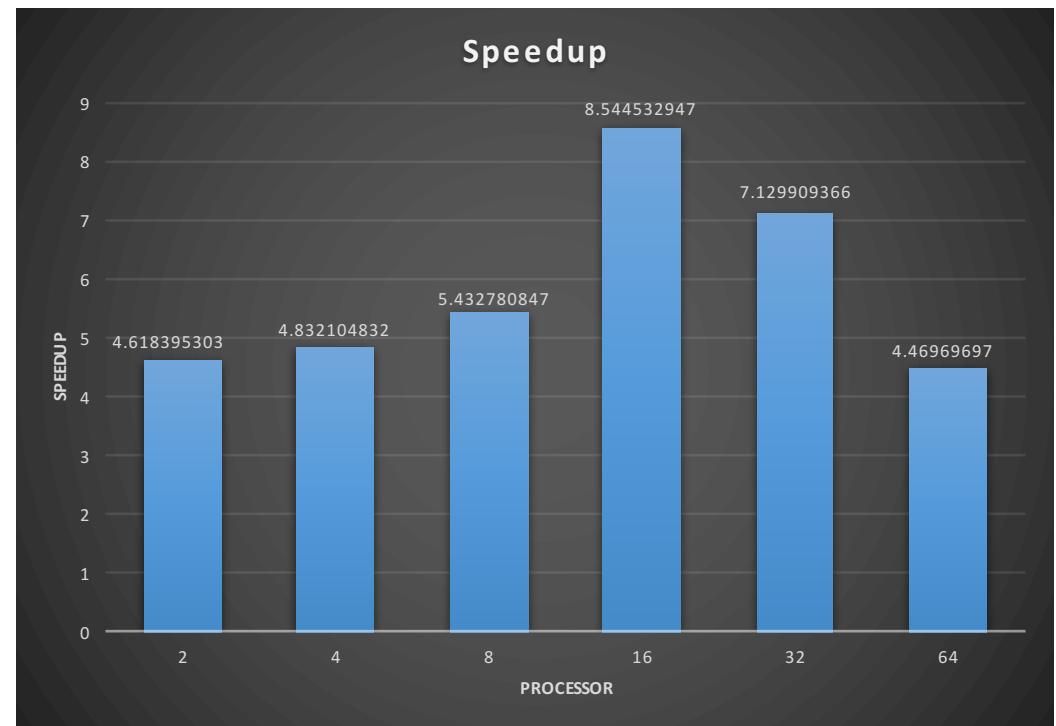
| Key size: 200000 (2 million) | |
|------------------------------|---------|
| Processors | Speedup |
| 2 | 48.905 |
| 4 | 17.312 |
| 8 | 12.688 |
| 16 | 8.491 |
| 32 | 4.142 |
| 64 | 1.464 |
| 128 | 0.996 |



Speedup



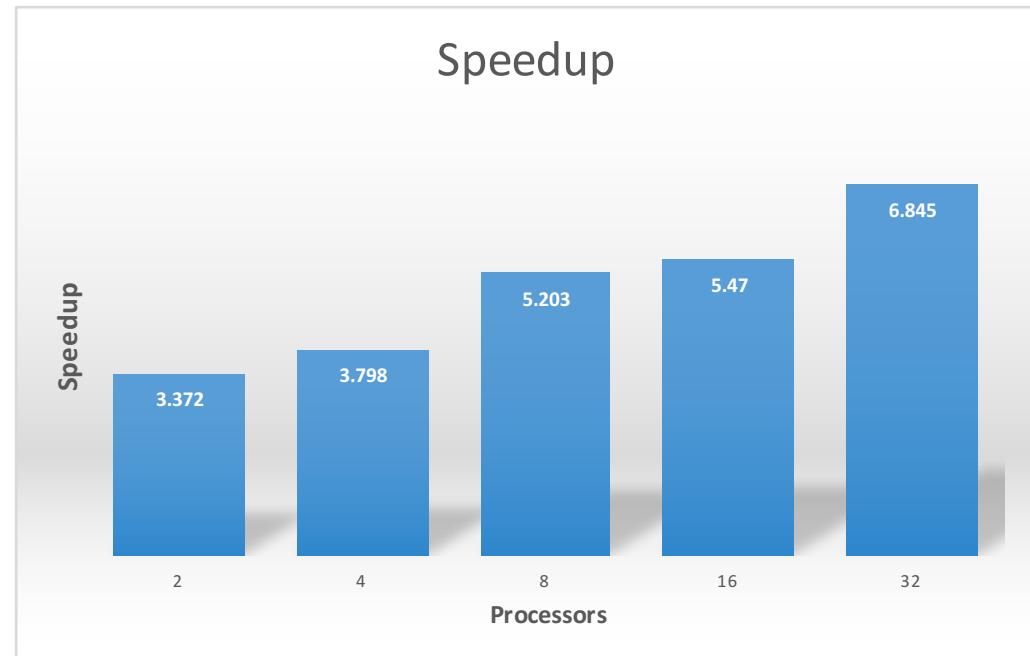
| Key size: 100000 | |
|------------------|-------------|
| Processors | Speedup |
| 2 | 4.618395303 |
| 4 | 4.832104832 |
| 8 | 5.432780847 |
| 16 | 8.544532947 |
| 32 | 7.129909366 |
| 64 | 4.46969697 |



Speedup [cont]



| Key size: 200000 | |
|------------------|---------|
| Processors | Speedup |
| 2 | 3.372 |
| 4 | 3.798 |
| 8 | 5.203 |
| 16 | 5.47 |
| 32 | 6.845 |



Speedup



- Amdahl's law

$$T_{\text{parallel}} = 0.9 \times T_{\text{serial}}/p + 0.1 \times T_{\text{serial}} = 18/p + 2,$$

$$S = \frac{T_{\text{serial}}}{0.9 \times T_{\text{serial}}/p + 0.1 \times T_{\text{serial}}} = \frac{20}{18/p + 2}$$

SLURM Job details for CPU = 2



```
[[asifimra@rush:~]$ scontrol show job 8751334
JobId=8751334 JobName=odd_even
  UserId=asifimra(549091) GroupId=cse633s18(89200175) MCS_label=N/A
  Priority=50214 Nice=0 Account=cse633s18 QOS=general-compute
  JobState=TIMEOUT Reason=TimeLimit Dependency=(null)
  Requeue=0 Restarts=0 BatchFlag=1 Reboot=0 ExitCode=0:15
  RunTime=00:15:08 TimeLimit=00:15:00 TimeMin=N/A
  SubmitTime=2018-04-24T22:34:55 EligibleTime=2018-04-24T22:34:55
  StartTime=2018-04-24T22:41:39 EndTime=2018-04-24T22:56:47 Deadline=N/A
  PreemptTime=None SuspendTime=None SecsPreSuspend=0
  Partition=general-compute AllocNode:Sid=srv-k07-14:37483
  ReqNodeList=(null) ExcNodeList=(null)
  NodeList=cpn-d14-[12,36]
  BatchHost=cpn-d14-12
  NumNodes=2 NumCPUs=2 NumTasks=2 CPUs/Task=1 ReqB:S:C:T=0:0:0:0
  TRES=cpu=2,mem=46000M,node=2
  Socks/Node==* NtasksPerN:B:S:C=1:0:0:0 CoreSpec=*
  MinCPUsNode=1 MinMemoryNode=23000M MinTmpDiskNode=0
  Features=IB DelayBoot=00:00:00
  Gres=(null) Reservation=(null)
  OverSubscribe=OK Contiguous=0 Licenses=(null) Network=(null)
  Command=/user/asifimra/myscript.sh
  WorkDir=/user/asifimra
  StdErr=/user/asifimra/test-srun.out
  StdIn=/dev/null
  StdOut=/user/asifimra/test-srun.out
  Power=
```

Challenges



- Long time to provision 64, 126 and 256 cores
- Unexpected service unavailability due to emergency.

Learning from the course



- Viewed the difference in run time as cores are increased
- Noticed how high performance computing systems and parallelization can speed up performance compared to sequential runs.
- Knowledge on MPI, Intel MPI and Open MPI systems
- Visit and seeing CCR infrastructure

Conclusion and future goals



- Results show that there should be an optimum number of CPU's which need to be allocated for the data load
- Each physical server initiated 1 process only
- Future Goal:
 - Extend this code to OpenMP and compare performance in CSE 702

References



- [1] <https://www.cse.buffalo.edu//faculty/miller/teaching.shtml>
- [2] Pacheco, P.S., 1997. *Parallel programming with MPI*. Morgan Kaufmann.
- [3] Foster, I., Zhao, Y., Raicu, I. and Lu, S., 2008, November. Cloud computing and grid computing 360-degree compared. In *Grid Computing Environments Workshop, 2008. GCE'08*(pp. 1-10). IEEE.
- [4] Academic Compute Cluster (UB-HPC). Link:
https://www.buffalo.edu/CCR/support/research_facilities/general_compute.html



Thank you