

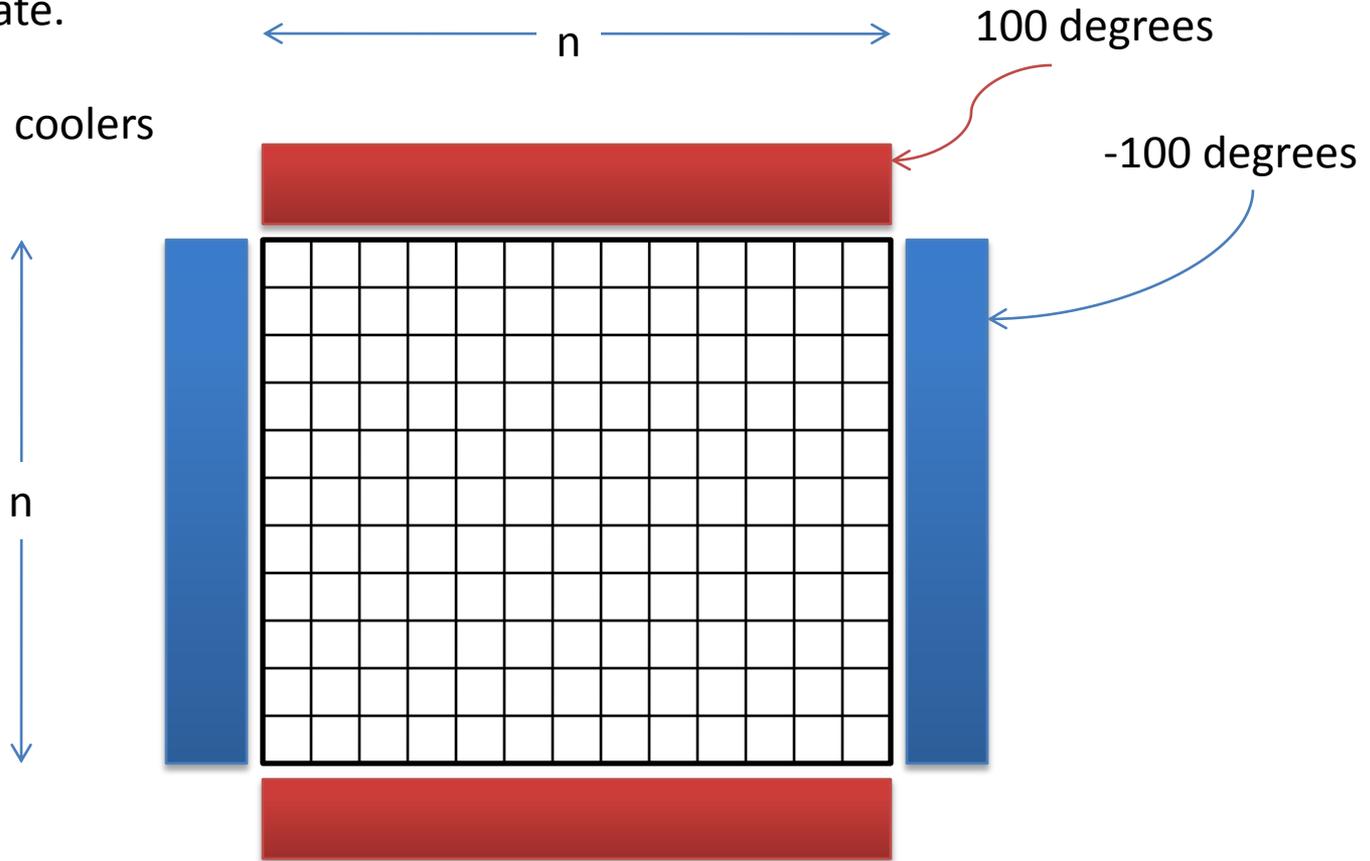
CSE-633 Parallel Algorithms
Spring 2009

Stationary Temperature Distribution In A Square
Plate

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Problem to Solve

$n \times n$ size plate.
 n^2 fields.
Heaters and coolers
on edges

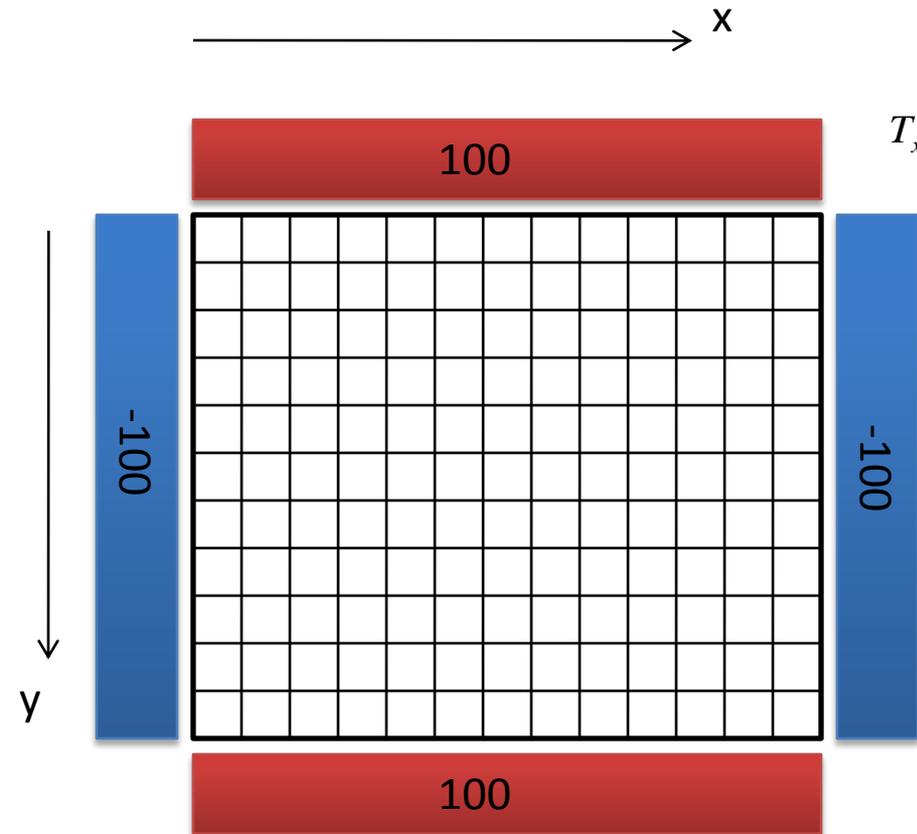


Problem to Solve

Iterative process:

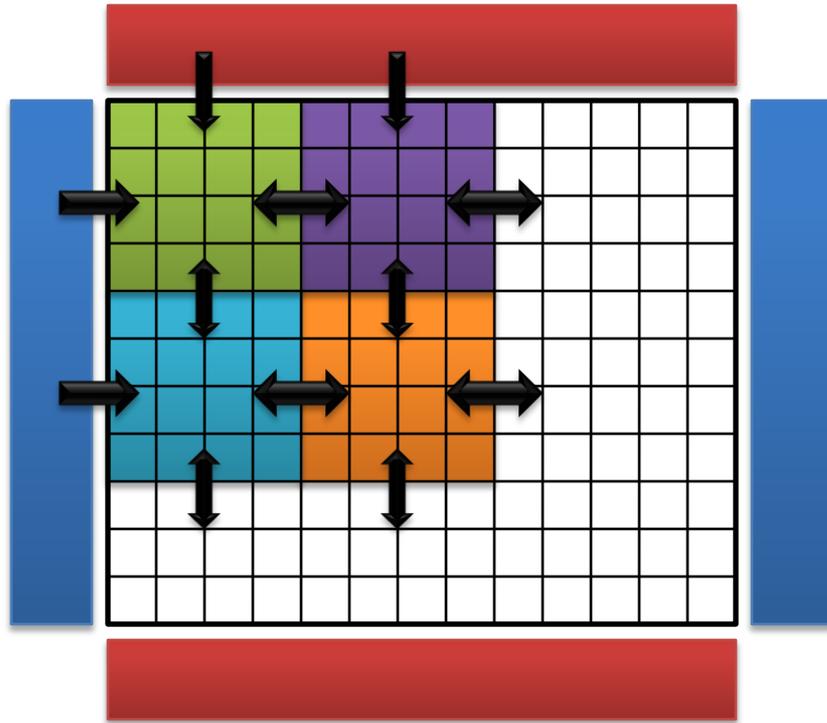
- In iteration i a new temperature value is calculated for each field on the plate, using the temperatures from iteration $i-1$:

$$T_{x,y}(i) = \frac{T_{x-1,y}(i-1) + T_{x+1,y}(i-1) + T_{x,y-1}(i-1) + T_{x,y+1}(i-1)}{4}$$



Solving the Problem

- Several processors to solve the problem.
 - h horizontal
 - v vertical
 - $h*v$ total processors.
- Each processor gets an equal part of the plate, i.e. a smaller rectangle.
- Each processor does all calculations within its rectangle and communicates values on edges with neighbouring processors.
- Processors on edges will use values from heaters/coolers, i.e. static values.



Algorithm

- 0 Initial calculations (find neighbours/setup arrays)
- 1 Loop:
 - 2 Calculate new values for each field rectangle
 - 3 Synchronize with neighbours
- 4 Gather and save result in text file

Basically, the loop is being parallelized.

Implementation

h-by-v mesh

Communication diameter: $\Theta(\max(h,v))$

Bisection width: $\Theta(\min(h,v))$

h-by-v in stead of x-by-x \rightarrow More options for #PEs.

Loop stop condition:

Each processors communicates an INT to neighbors along with edge values.

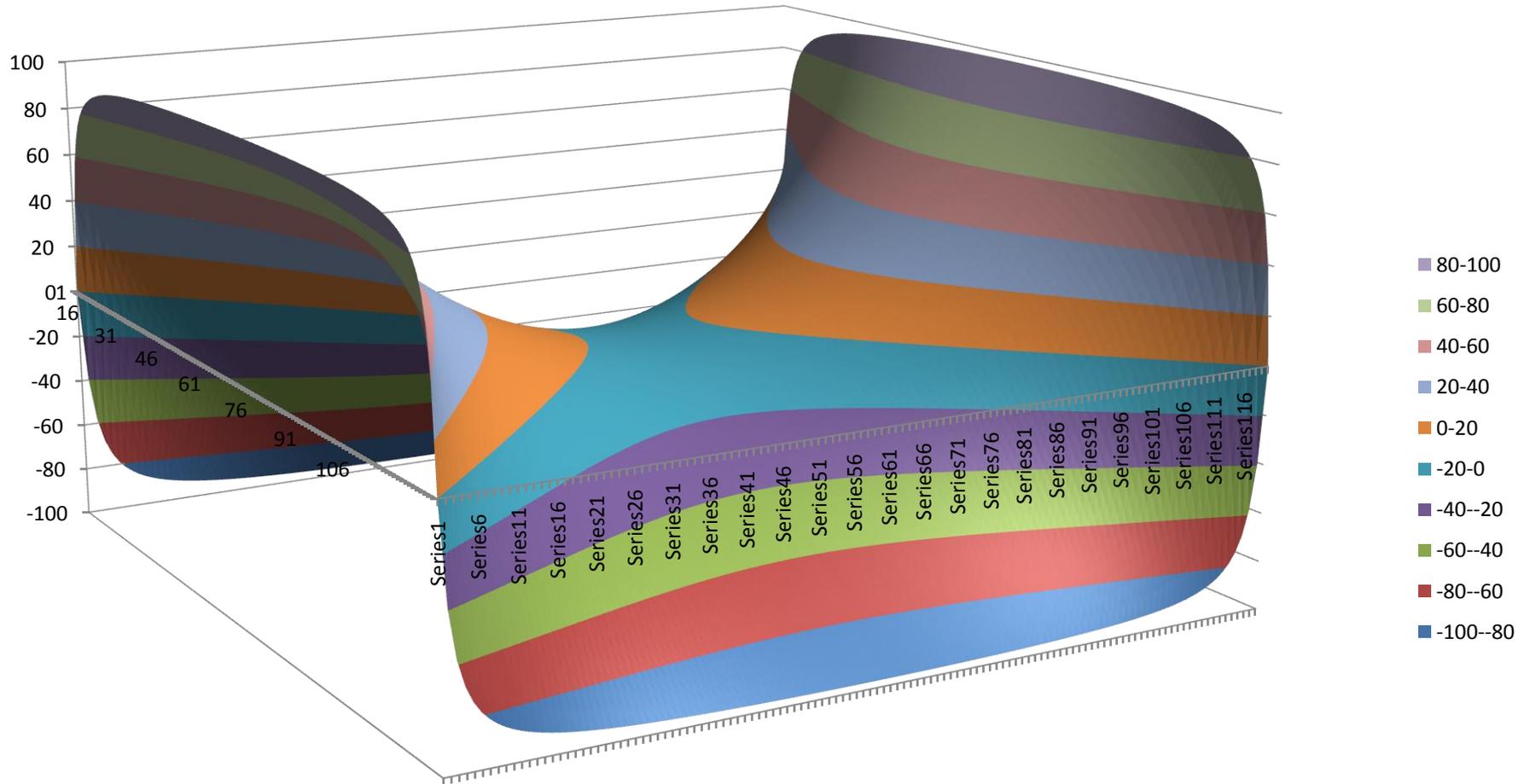
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if (PE updates over threshold) Send 0
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else Send min known value +1
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min known value is min of own value and received values in last iteration.

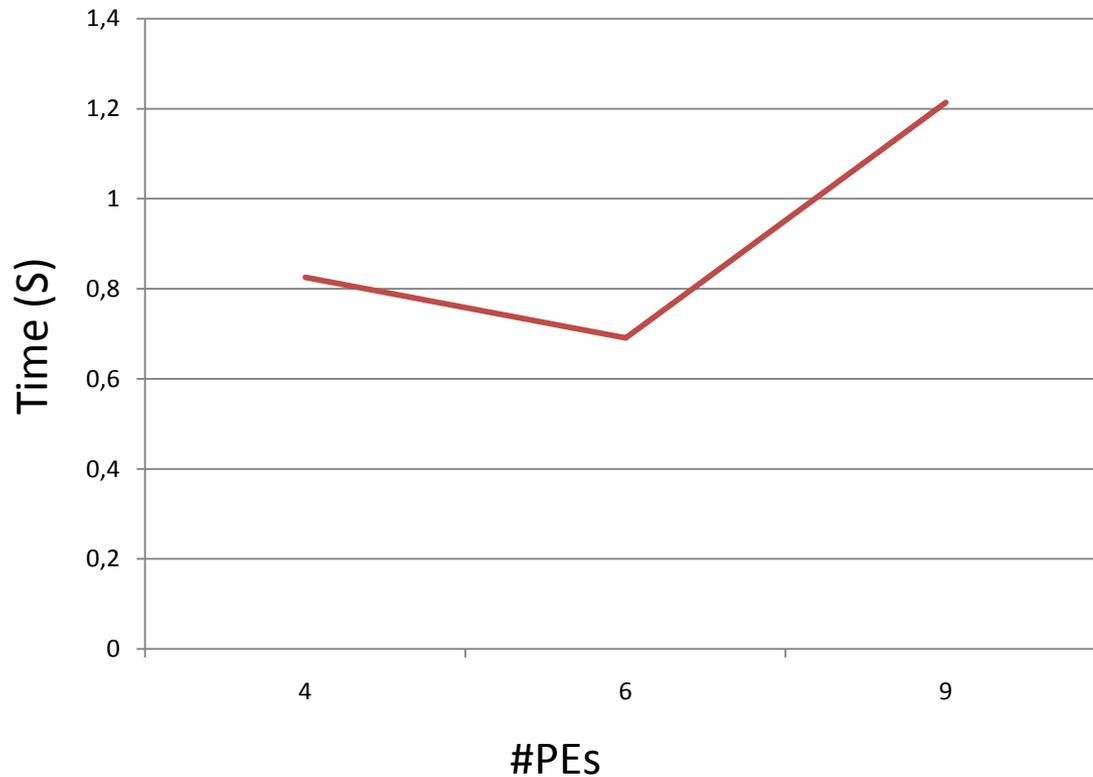
Any PE: If **min known value** > v+h then end loop

Result: Temperature in plate



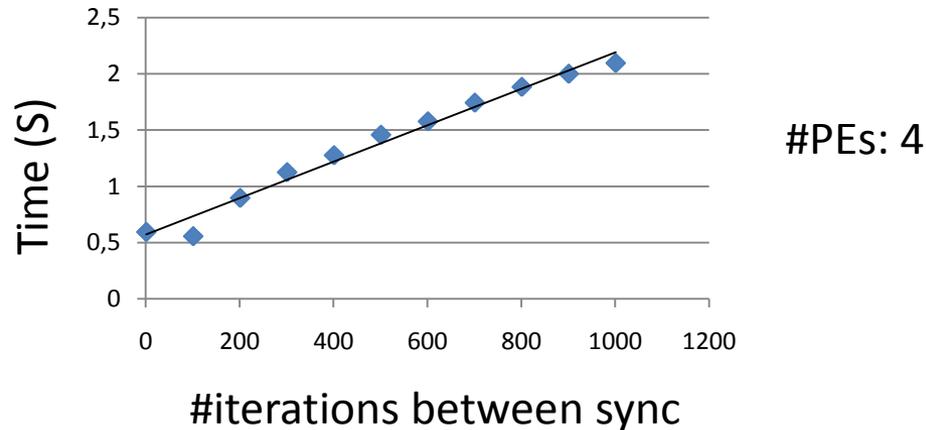
Problem!

Program turns out to be less than perfect for parallelization.

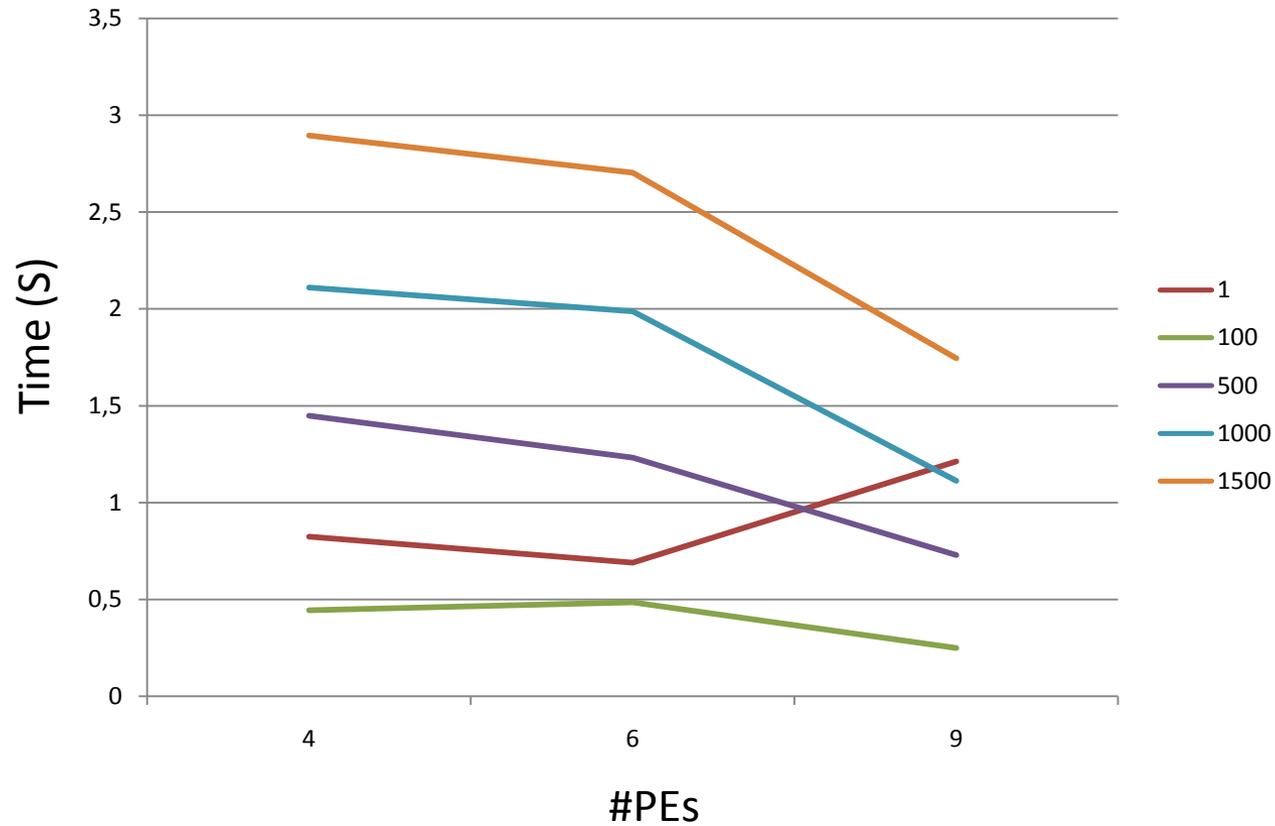


Problem!

- MPI communication dominates arithmetic calculations
- Not able to make plate as large as wanted (got error above 150x150 fields)
- Solution?
 - Do more iterations of calculations between communication.
 - Reduces #sync rounds from ~2000 to ~25

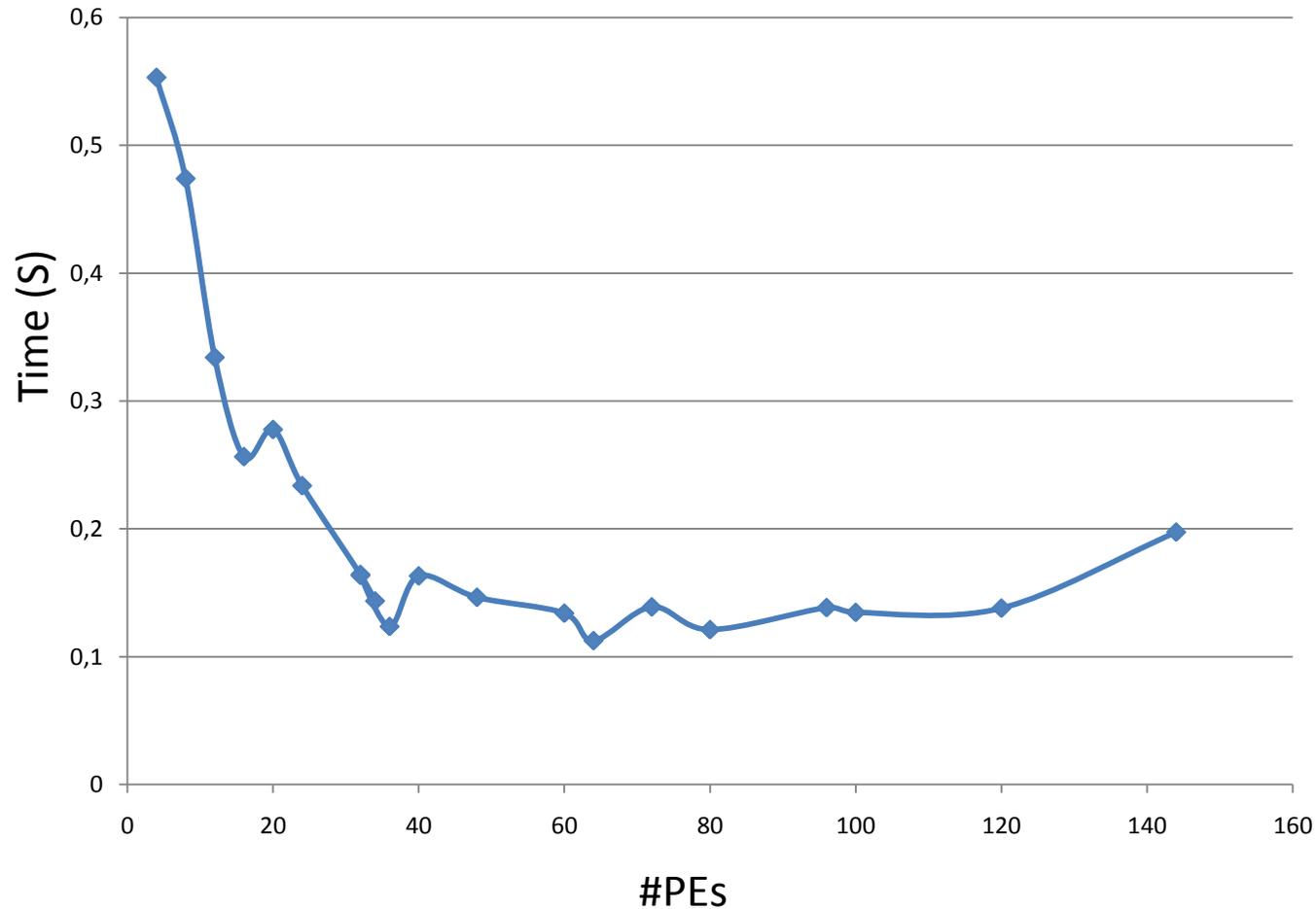


- 100 iterations per synchronization is the sweet spot!



Results: Running time

- Runs with varying # PEs, with 100 iterations per sync. Average over 10 runs.



Results: Running time

- Runs with varying # PEs, with 100 iterations per sync. Average over 10 runs.
 - Minimum at 64 PEs: 0,112559s.
 - Little gains > 30 PEs.
 - Smaller speedup than expected.

Results: Speedup

- Runs with varying # PEs, with 100 iterations per sync. Average over 10 runs.

