PARALLEL ANT COLONY OPTIMIZATION

CSE633 Parallel Algorithm
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Problem Statement

Traveling Salesperson
- Given a list of cities and distances,
  find the shortest distance city A to city B

NP-hard Question
- Just try to optimize the solution

Distance has different costs
- Chance of either direction is different
- The order of cities does not matter as long as it has the shortest distance
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Algorithm - SACO

- The Simple Ant Colony Optimization
- Population based optimization
- Artificial Pheromone System
- Typically used to find shortest path problem
- Computationally Expensive
- Approximate Solution
Algorithm - Process

1. Construct Ant Solutions

2. Pheromones Evaporation

3. Update Pheromones

4. Termination Criteria
1. **Construct Ant Solutions**
- Each iteration consists of X ants. Each ant constructs its own solution (each ant walks from start to destination)

Suppose And A’s original path [1, 4, 2, 3, 4, 2, 3, 4, 5]

2. **Removes loops in solution**
- Ant A condensed path [1, 4, 5]
- Ant B Path [1, 6, 7, 5]
Algorithm 3. Update Pheromone

Update Pheromones

The faster routes have higher pheromones, therefore increasing the chance that the path is chosen by ants.

We add the pheromone change to the path taken by ants.

**Ant Pheromone = 1 / Edges of Path**
- Ant A condensed path [1, 4, 5]
  - A's Pheromone Change = 1 / 2
- Ant B Path [1, 6, 7, 5]
  - B's Pheromone evaporation = 1 / 3
Algorithm
4. Termination Criteria

1. No major changes in solution
   When the solution no longer changes, it may mean that the optimum path has been found

2. Max number or iteration reached
   We have a set max iteration to keep things in check
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Parallel Approach

1. Each Processor is assigned several random “cities” as center point of random clusters
2. From each “city” attempt to reach the start and end point several times
3. Select the optimal solution among the random “cities”
3. Update pheromone according to local optimal
Parallel Approach

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Results - Test Settings

Max Iterations : 1000
Evaporation Rate : 0.7
Ants : 7
Graph Size : 100, 300, 500, 900, 1000, 2000
Termination Criteria : 20 Consecutive “optimal” solutions
Skylake processors - 1, 16, 32, 64, 128, 256
Max runtime : 30 minutes
Weights are initialized with same cost
Results:
16~128 Processors

256 processors takes significantly longer on most cases and constantly ends on 1000 iterations.

Samples with less processors end within the iteration range but typically have sub-par results.
Results: 16~256 Processors

16 and 32 processors takes the least time.
Results: 16~64 Processors

32 processors performs slightly better on the long term

<table>
<thead>
<tr>
<th>Time</th>
<th>16 Processors</th>
<th>32 Processors</th>
</tr>
</thead>
<tbody>
<tr>
<td>100 * 100</td>
<td>19</td>
<td>16</td>
</tr>
<tr>
<td>300 * 300</td>
<td>18</td>
<td>25</td>
</tr>
<tr>
<td>500 * 500</td>
<td>49</td>
<td>38</td>
</tr>
</tbody>
</table>
**Results:**

1000*1000

<table>
<thead>
<tr>
<th>Processor #</th>
<th>Time (Second)</th>
</tr>
</thead>
<tbody>
<tr>
<td>16</td>
<td>134</td>
</tr>
<tr>
<td>32</td>
<td>99</td>
</tr>
<tr>
<td>64</td>
<td>165</td>
</tr>
<tr>
<td>128</td>
<td>259</td>
</tr>
</tbody>
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Observation

1. More processors isn’t necessary better
   a. A single ant’s perception of the weights won’t change until it has reached the end point. By which many iterations, or none, may have passed

2. Communication Cost is really heavy
   a. Updating the weight matrix requires heavy communication between the processors
Observation

3. On larger maps, finding a path alone is very expensive
   a. less processors converges on less optimal solutions
   b. more processors will run a lot faster, but will almost never converge
Using more processors...

Can sometimes reach optimal solution the first time an ant has finished it’s path, but during the first round for all the ants the solution has a high variance, therefore affecting how well the solution converges.

Simply put, the optimal solution may not have enough influence over the other non-optimal solutions

**Ants round 1 for 256 processors**

-> 2 -> 12 -> _bunch or random not optimal solutions_ -> ...

**Ants round N for 256 processors**

-> _bunch or random not optimal solutions_ -> ... -> 2 -> ...
Using less processors...

The solution will converge too fast, and very often not on the optimal solution since the influence is too strong for example...

**Ants round 1 for 4 processors**
- 10 -> 20 -> 15...

**Ants round N for 4 processors**
- 10 -> 10 -> 10...
Observation

To find Best Time Given Solution:
- how long does it take to reach optimal solution?
- Looking for path with route length 2, how long will it take
- Try more processors

To find Best Solution Given Time:
- In a time limit, how good will be your optimal result?
- Give me your best result in 3 minutes
- Try less processors