

*Shake-and-Bake:*  
**Applications and Advances**

**Russ Miller & Charles M. Weeks**

**Hauptman-Woodward Med. Res. Inst.**

**Principal Contributors:**

**C.-S. Chang**

**G.T. DeTitta**

**S.M. Gallo**

**H.A. Hauptman**

**H.G. Khalak**

**D.A. Langs**

**R. Miller**

**S. Potter**

**C.M. Weeks**

**Partial funding from NIH and NSF.**

# Outline of Talk

---

*SnB*

- ◆ *Shake-and-Bake*
  - **The Minimal Function**
- ◆ *SnB*
  - **Results**
- ◆ *SnB v2.0*
  - **Rationale**
  - **Results**
- ◆ **Summary**

# Direct Methods

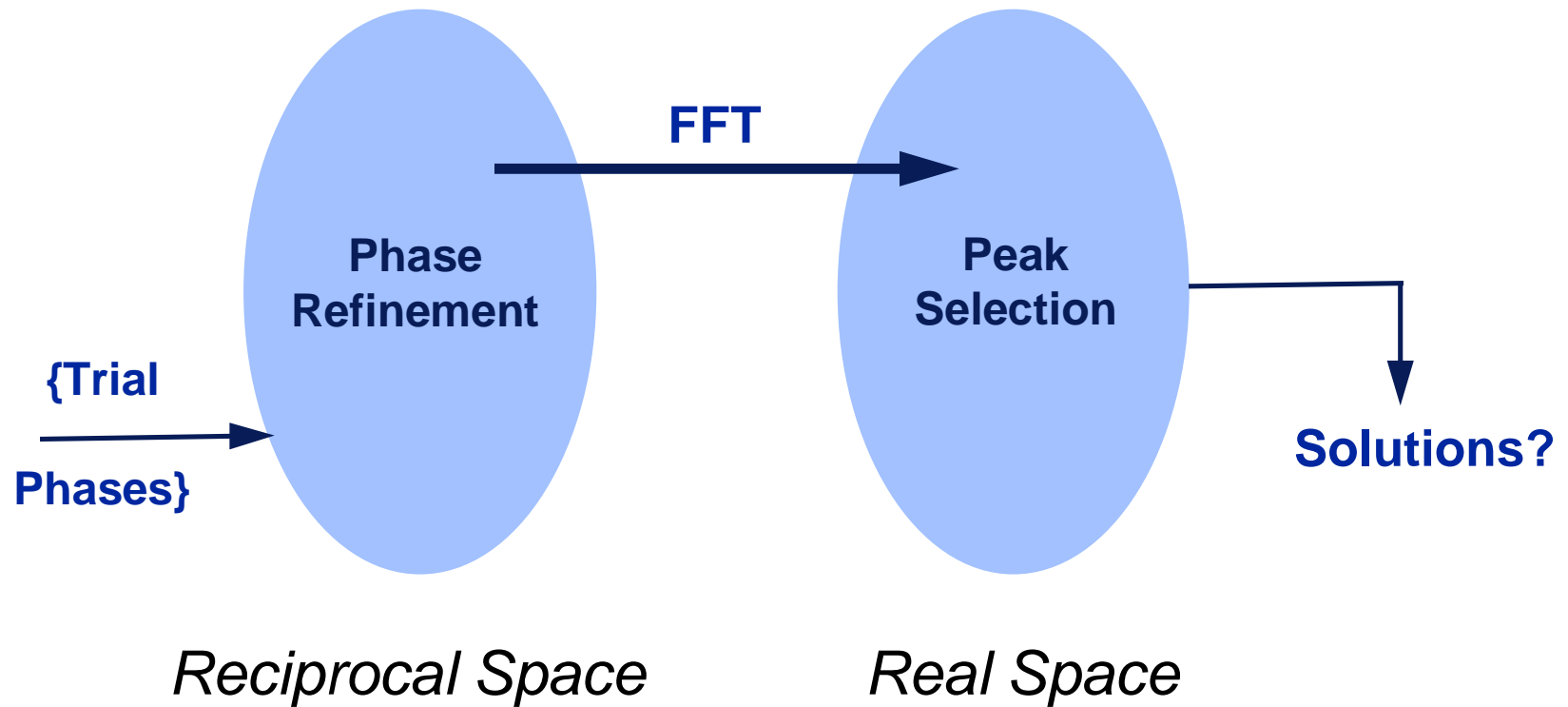
---

*SnB*

- ◆ *Direct Methods* use probabilistic theories to exploit linear relationships among phases.
- ◆ Resolution of 1.2Å or better.
- ◆ Routinely applied to structures with 150 or fewer atoms.
- ◆ Standard packages:
  - SHELX
  - teXsan
  - SIR92/96

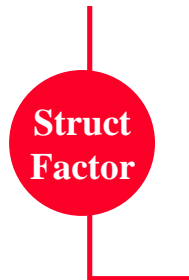
# Conventional Direct Methods

*SnB*



# *Shake-and-Bake*

{Trial  
Structures}



FFT<sup>-1</sup>



# The Minimal Function

*SnB*

$$R = \frac{\sum_T W_T (\cos \phi_T - est_T)^2}{\sum_T W_T}$$

Triple:  $\phi_T = \phi_h + \phi_k + \phi_{-h-k}$

$$W_T = \left( \frac{2}{N^{1/2}} \right) |E_h E_k E_{-h-k}|$$

$est_T$  is the known expected value of  $\cos \phi_T$

# *Shake-and-Bake*

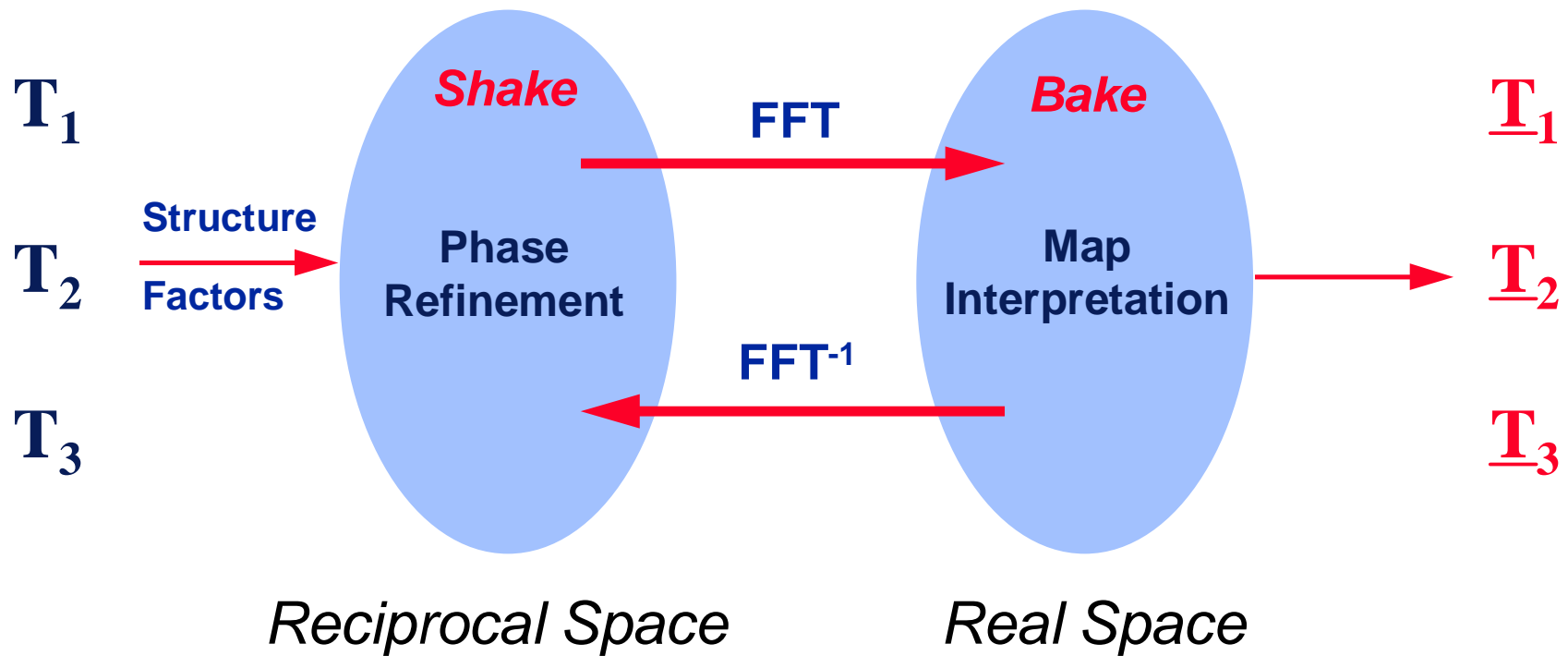
---

*SnB*

- ◆ **Direct Methods Optimization Technique**
- ◆ **Multiple Random-Atom Trial Structures**
- ◆ **Real/Reciprocal Space Cycling**
- ◆ **Phase Refinement Techniques:**
  - **Parameter Shift**
  - **Tangent Formula**
- ◆ **Minimal Function as FOM**

# Shake-and-Bake

*SnB*

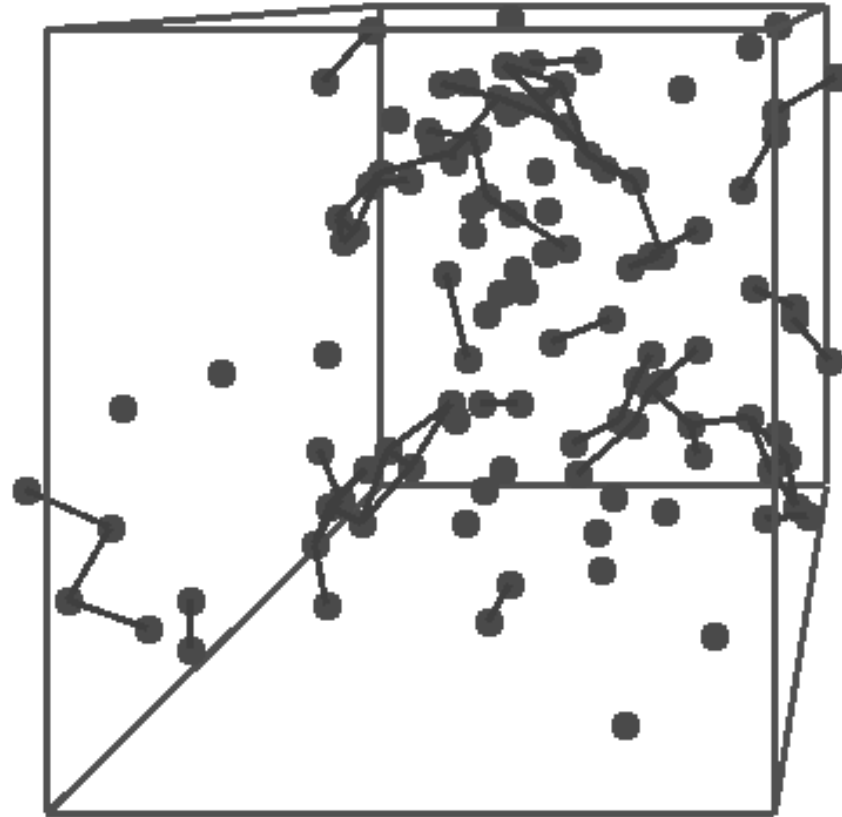




# *SnB*: Random Start

---

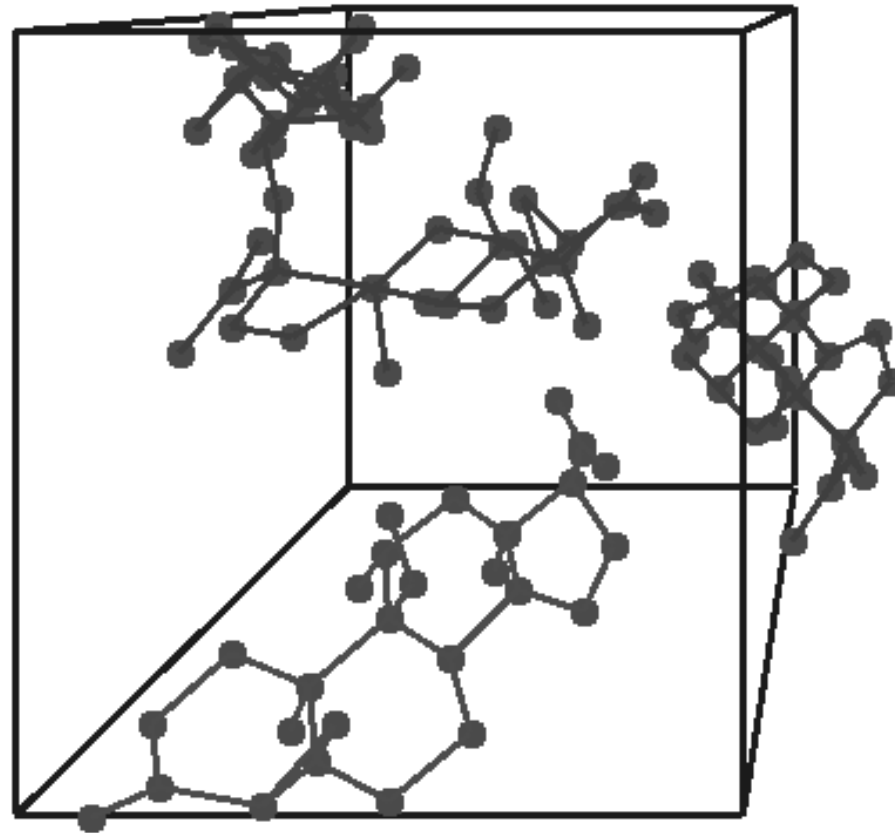
*SnB*



# *SnB*: Final Structure

---

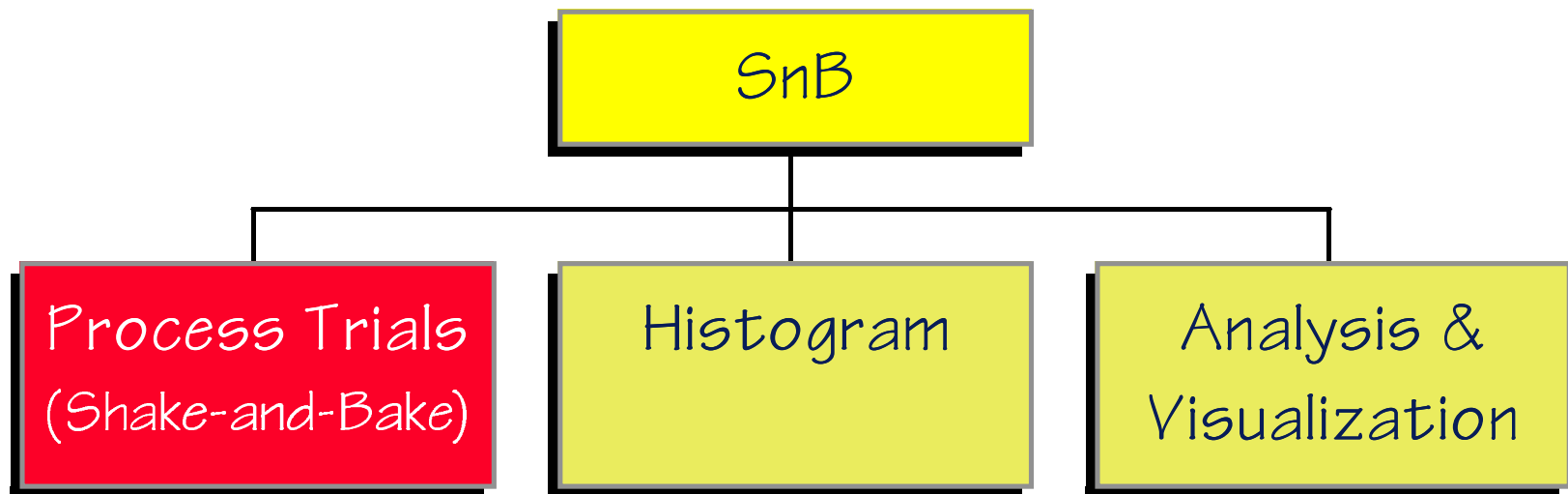
*SnB*



# Structure of *SnB*

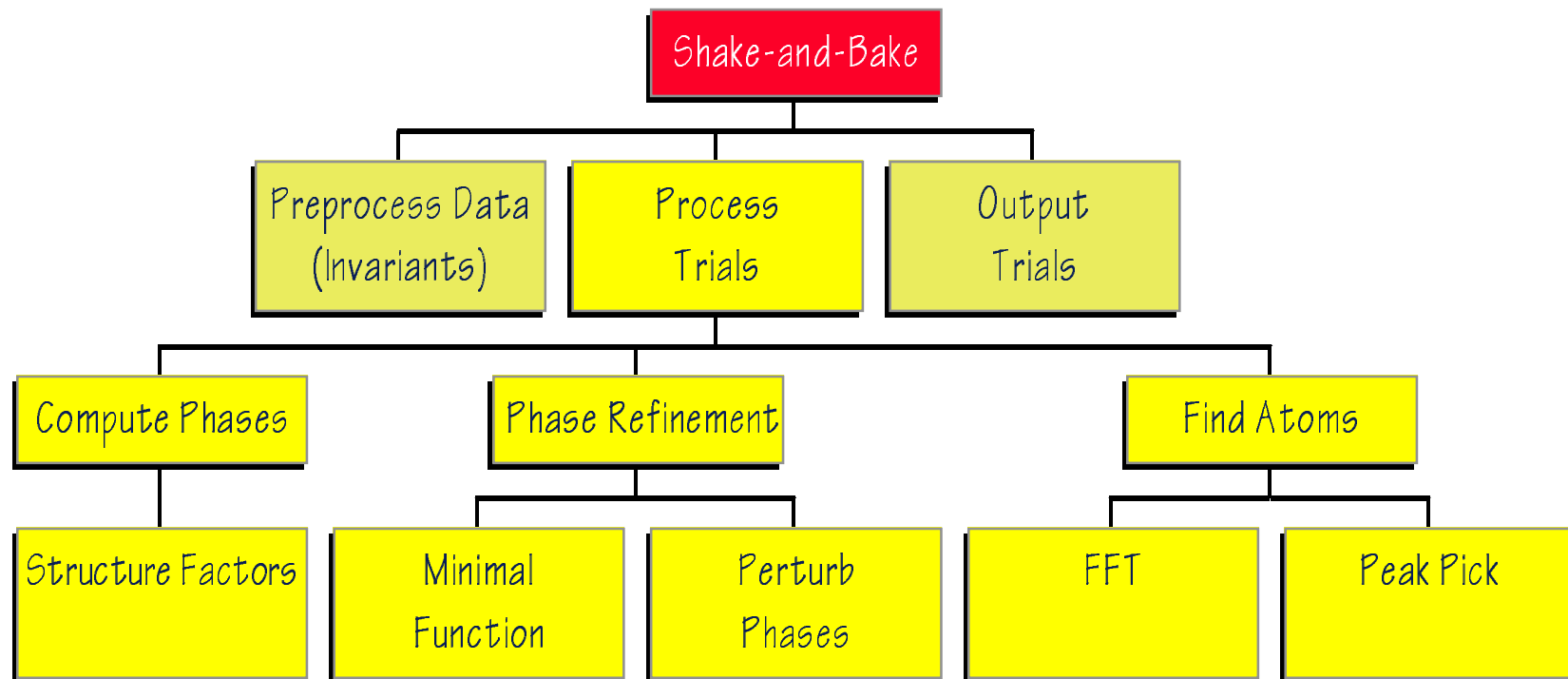
---

*SnB*



# Shake-and-Bake

*SnB*



# *SnB* Parameters



---

	<b>Default</b>	<b>Ph8755</b>	<b>ToxII</b>
<b>Atoms (asu)</b>	<i>n</i>	<b>74</b>	<b>508</b>
<b>Phases</b>	<i>8n - 10n</i>	<b>740</b>	<b>5,000</b>
<b>Triples</b>	<i>70n - 100n</i>	<b>7,400</b>	<b>50,000</b>
<b>Cycles (PS)</b>	<i>n/2</i>	<b>40</b>	<b>255</b>
<b>Peaks recycled</b>	<i>0.8n - n</i>	<b>74</b>	<b>400</b>
<b>E-Fourier Steps</b>	<b>2</b>	<b>2</b>	<b>5</b>

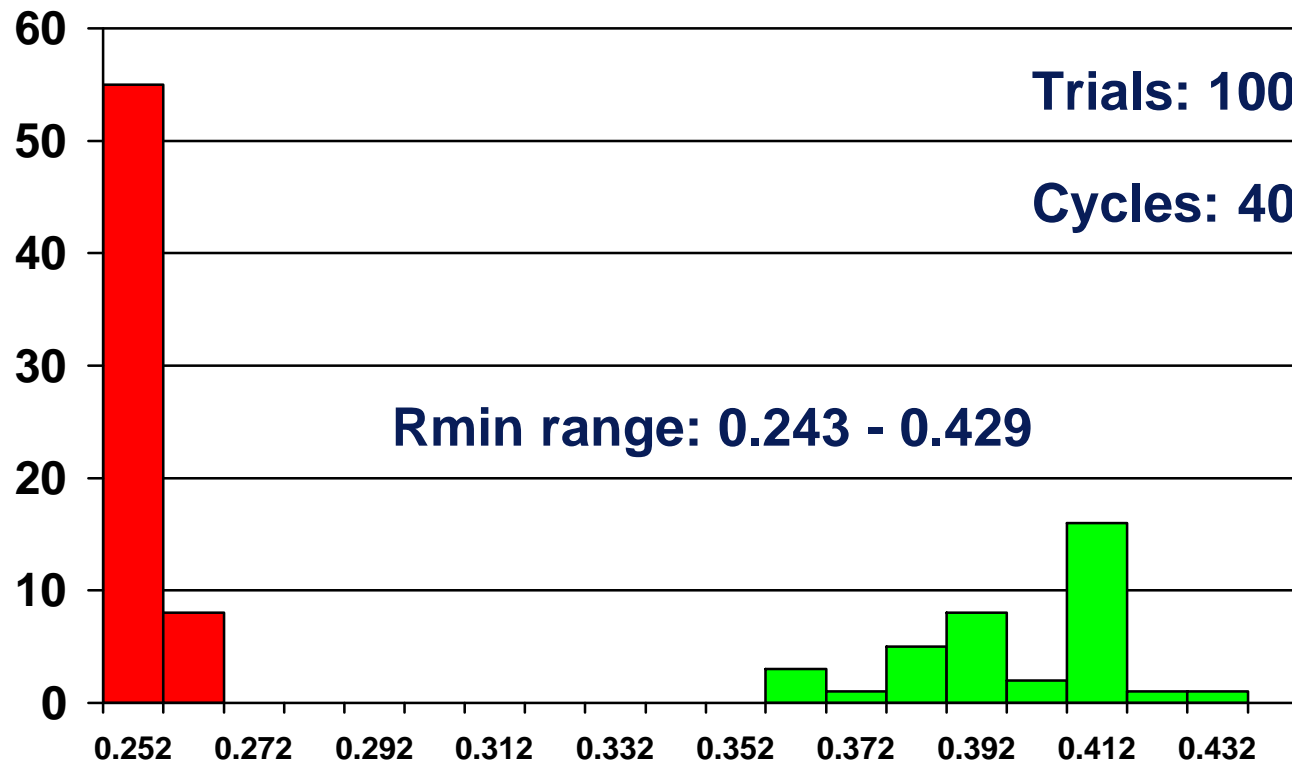
---

# Ph8755: *SnB* Histogram

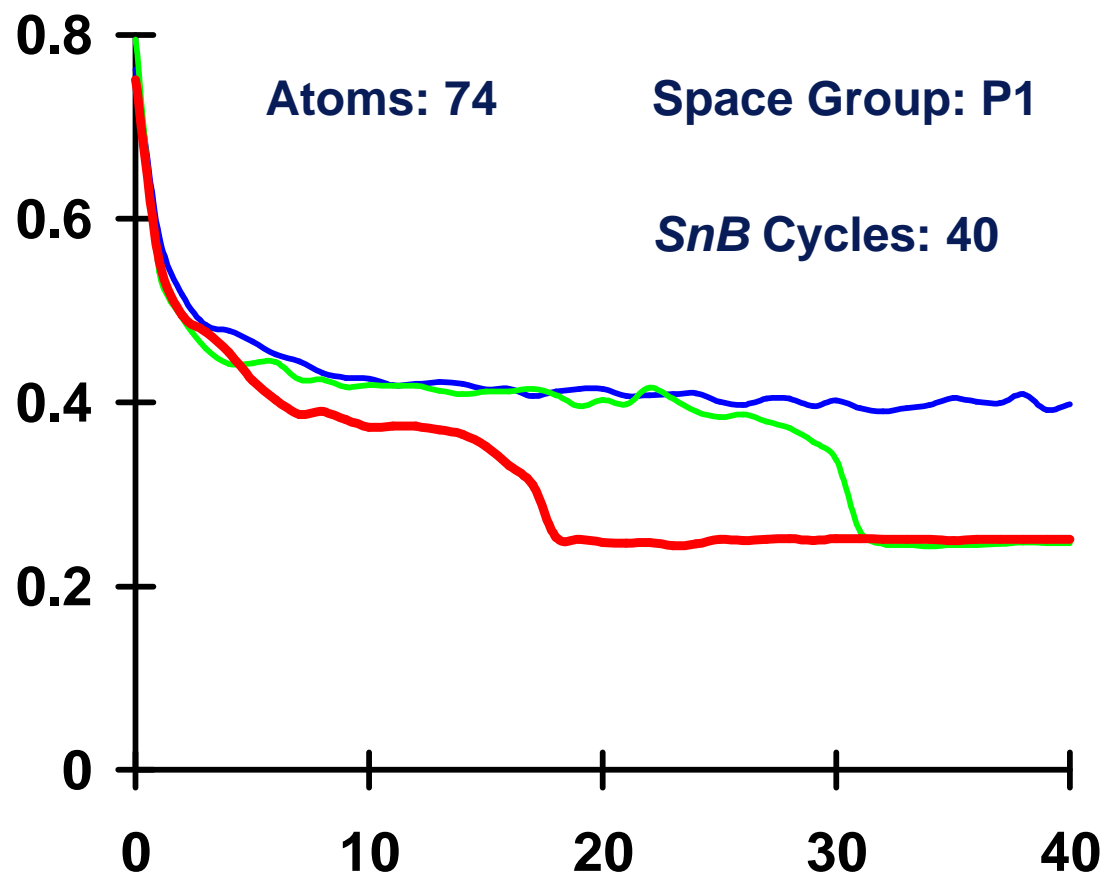
*SnB*

Atoms: 74  
Space Group: P1

Phases: 740  
Triples: 7,400



# Ph8755: Trace of *SnB* Solution *SnB*



# ToxII: *SnB* Histogram

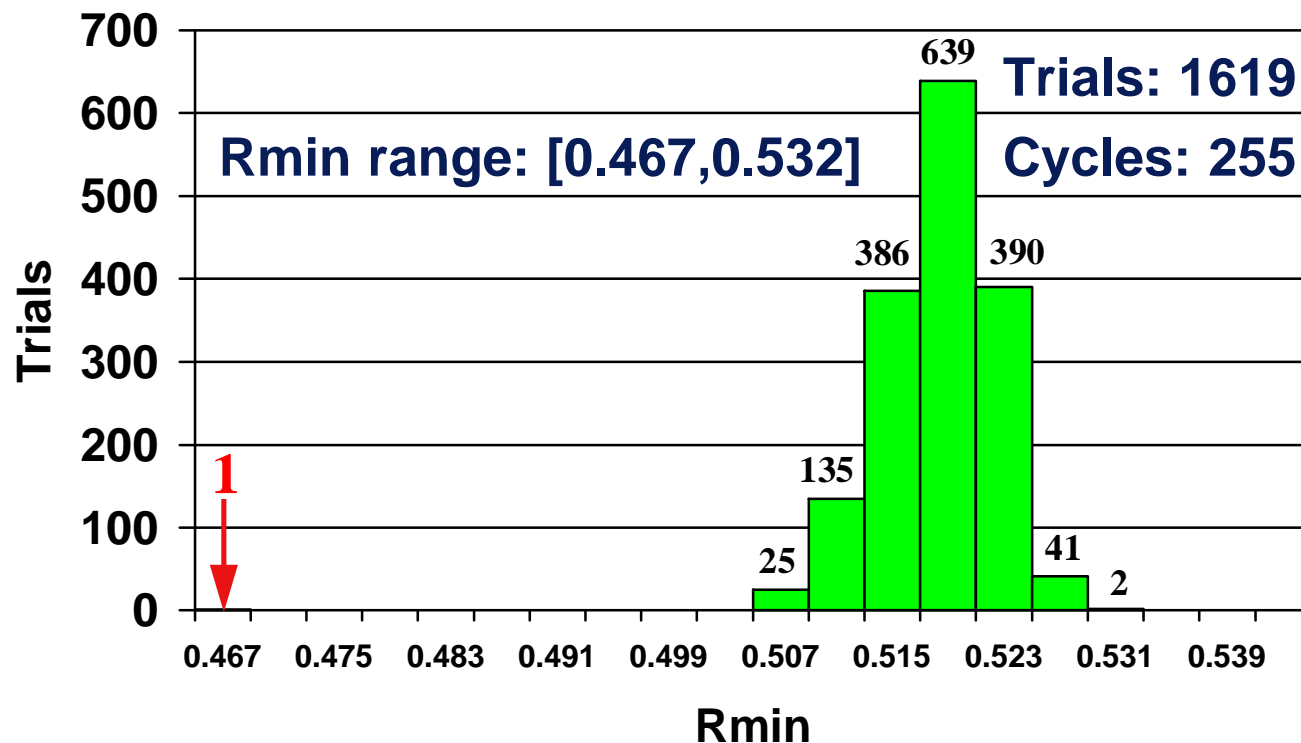
*SnB*

Atoms: 500

Phases: 5,000

Space Group:  $P2_12_12_1$

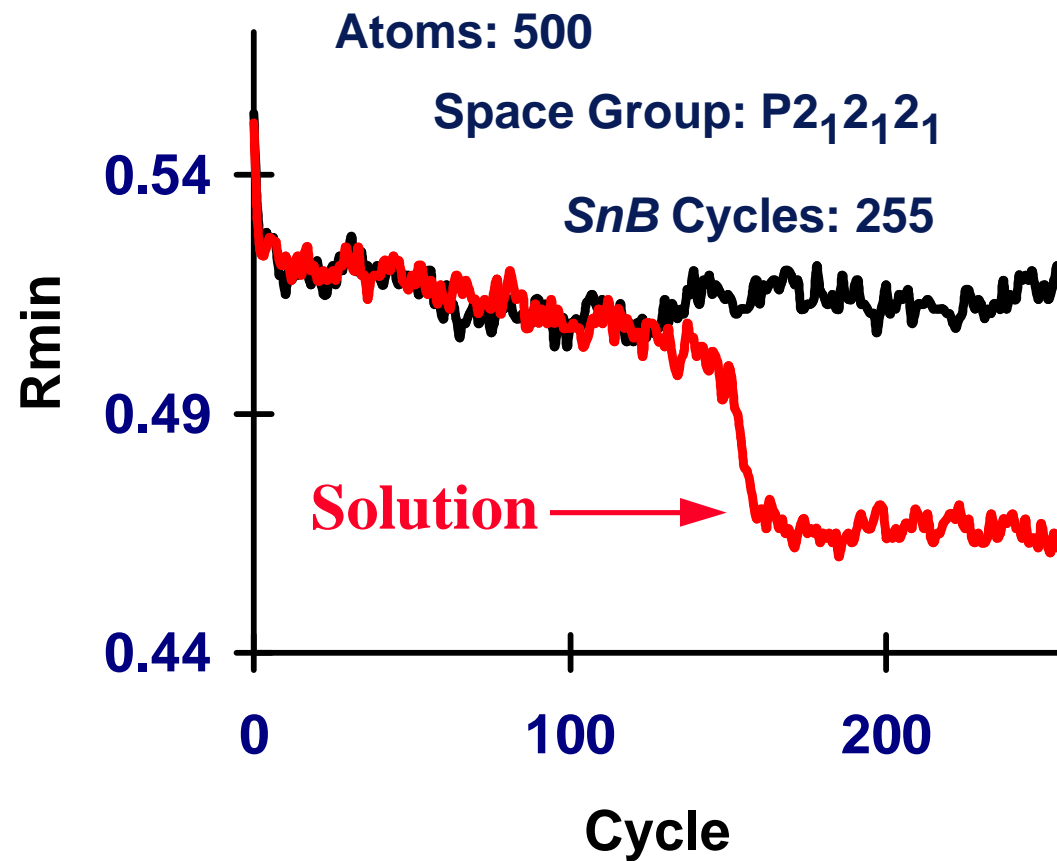
Triples: 50,000





# Tox II: Trace of *SnB* Solution

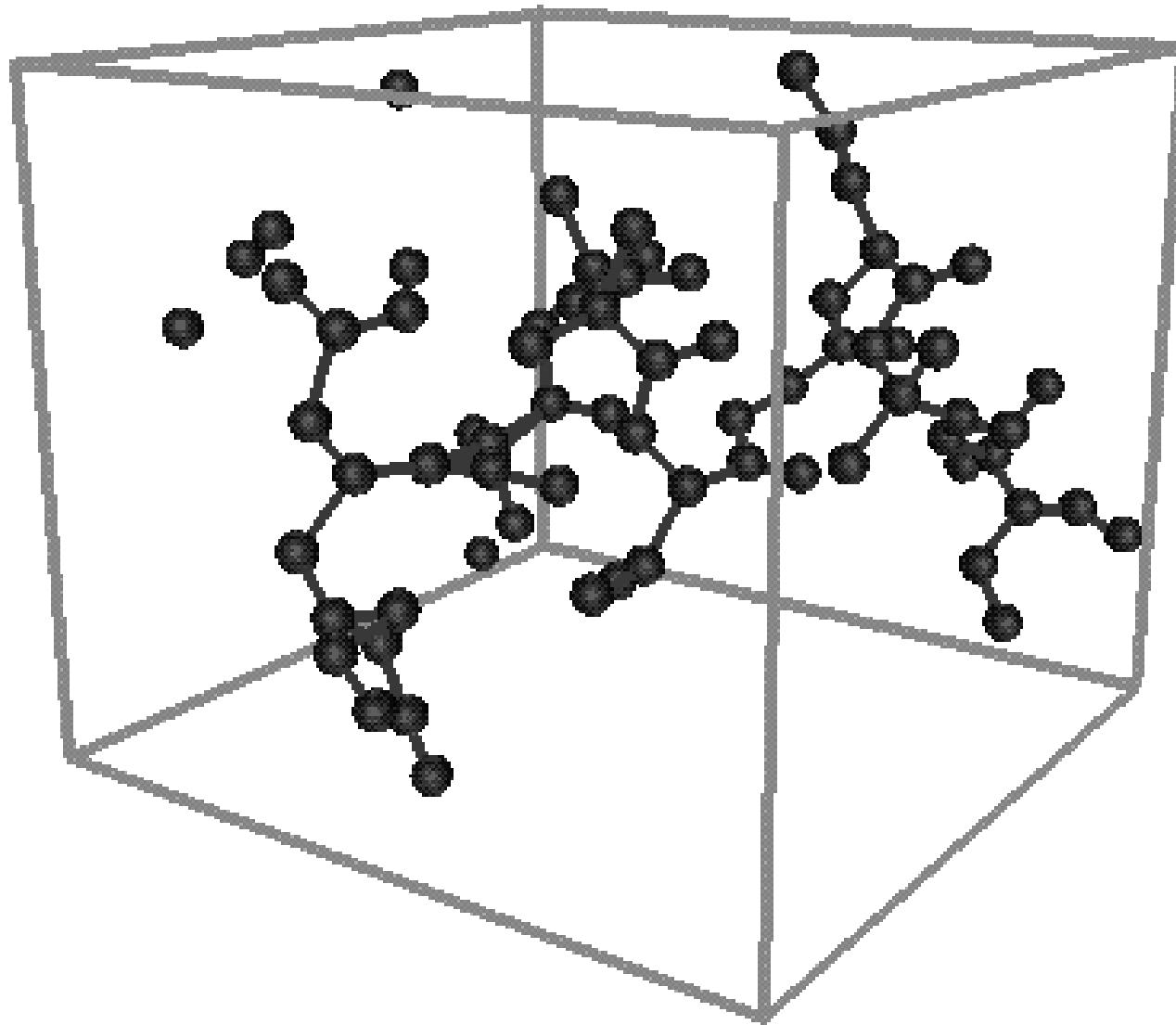
*SnB*



# Visualization in *SnB* (Ph8755)

*Geomview*: Geometry Center, U. Minn.

*SnB*



# Some *SnB* Applications

*SnB*

STRUCTURE	LOCATION	ATOMS	SP GRP	RES
Vancomycin	Penn	258	P <sub>4</sub> 2 <sub>1</sub> 2	0.9Å
I4 Peptide	HWI	289	I4	1.1
Microlide	France	296	P2 <sub>1</sub>	1.1
Gramicidin A	HWI	317	P2 <sub>1</sub> 2 <sub>1</sub> 2 <sub>1</sub>	0.86
Er-1 pheromone	UCLA	328	C2	1.0
Crambin	HWI	~400	P2 <sub>1</sub>	0.83
Alpha-1 peptide	OCI/U. of T.	471	P1	0.92
Rubredoxin	HWI	497	P2 <sub>1</sub>	1.0
Scorpion Toxin II	HWI	624	P2 <sub>1</sub> 2 <sub>1</sub> 2 <sub>1</sub>	0.96

# Factors Determining Success Rate *SnB*

---

- ◆ **Data quality**
- ◆ **Resolution**
- ◆ **Complexity and connectivity of structure**
- ◆ **Space group**
- ◆ *Presence of heavy atoms*

# An Interesting I4 Structure

---

*SnB*

## ◆ Structure:

- ❑ Peptide with 10 Sulfurs
- ❑ 289 nonH atoms total
- ❑ 1.1Å resolution data

## ◆ Bugs: Special Positions & Refinement

## ◆ Results (*SnB 2.0*)

- ❑ PS: 53% success rate
- ❑ PS/Rest: 44% success rate
- ❑ Tan: 25% success rate

# Extending Resolution: the I4 Structure

---

*SnB*

- ◆ **Truncate to 1.2Å - 1.5Å**
- ◆ **Solutions at all resolutions**
  - **1.2Å:** Standard bimodal distribution
  - **1.3Å:** Standard bimodal distribution
  - **1.4Å:** Good, but some mixing of solutions and nonsolutions
  - **1.5Å:** Solutions (~50 deg. phase error) but *not* recognizable by FOM
- ◆ **Recognize low-resolution solutions??**

# *SnB* 2.0: Rationale

---



- ◆ **Improve running time**
  - Build from ground up
- ◆ **Provide additional features**
  - Inverse Fourier
  - Density modification
  - Grid size
  - “Twice Baking”
  - Peaks at special positions

# *SnB* v2.0 Parameters/Proteins



<i>Structure</i>	<i>Atoms (n)</i>	<i>Heavy Atoms</i>	<i>Phases</i>	<i>Cycles</i>	<i>Max Succ Rate</i>
<b>Vancomycin</b>	<b>202</b>	<b>Cl 8</b>	<b>2000</b>	<b>200</b>	<b>0.8%</b>
<b>I4 Peptide</b>	<b>248</b>	<b>S10</b>	<b>1900</b>	<b>250</b>	<b>53.0</b>
<b>Gramicidin A</b>	<b>272</b>	<b>-</b>	<b>3000</b>	<b>275</b>	<b>1.1</b>
<b>Crambin</b>	<b>327</b>	<b>S6</b>	<b>3000</b>	<b>300</b>	<b>4.8</b>
<b>Rubredoxin</b>	<b>395</b>	<b>FeS6</b>	<b>4000</b>	<b>400</b>	<b>6.2</b>
<b>Scorpion Toxin II</b>	<b>508</b>	<b>S8</b>	<b>5000</b>	<b>500</b>	<b>1.4</b>

**Note:  $n$  = independent protein atoms**



# SnB 2.0: Varying Peaks



<i>Structure</i>	<b>50</b>	<b>100</b>	<b>200</b>	<b>300</b>	<b>400</b>
<b>Vancomycin</b>	<b>0.4%</b>	<b>0.6%</b>	<b>0.2%</b>	---	---
<b>I4 Peptide</b>	<b>53.0</b>	<b>52.0</b>	<b>45.0</b>	---	---
<b>Gramicidin A</b>	<b>0.0</b>	<b>0.3</b>	<b>1.1</b>	<b>0.7%</b>	---
<b>Crambin</b>	<b>4.3</b>	<b>4.8</b>	<b>3.3</b>	<b>3.4</b>	---
<b>Rubredoxin</b>	<b>5.7</b>	<b>6.2</b>	<b>5.4</b>	<b>3.9</b>	<b>3.4%</b>
<b>Scorpion Toxin II</b>	---	<b>1.0</b>	<b>1.4</b>	<b>0.4</b>	<b>0.1</b>

# *SnB* 2.0: Varying Cycles



Structure	Success Rates while varying <i>SnB</i> Phase Refinement Cycles					
	$0.25n$	$0.5n$	$0.75n$	$n$	$1.25n$	$1.5n$
<b>Vancomycin</b>	<b>0.1%</b>	<b>0.4%</b>	<b>0.4%</b>	<b>0.6%</b>	<b>0.7%</b>	-
<b>I4 Peptide</b>	<b>27.0</b>	<b>40.0</b>	<b>48.0</b>	<b>53.0</b>	-	-
<b>Gramicidin A</b>	<b>0.0</b>	<b>0.4</b>	<b>0.6</b>	<b>0.9</b>	<b>1.2</b>	<b>2.0%</b>
<b>Crambin</b>	<b>3.1</b>	<b>4.1</b>	<b>4.6</b>	<b>4.8</b>	-	-
<b>Rubredoxin</b>	<b>4.6</b>	<b>5.5</b>	<b>5.9</b>	<b>6.0</b>	-	-
<b>Scorpion Toxin II</b>	<b>0.05</b>	<b>0.5</b>	<b>1.0</b>	<b>1.4</b>	-	-

# *SnB* 2.0: Phase Refinement



<i>Structure</i>	<i>Peaks</i>	<i>PS Standard</i>	<i>PS Restricted</i>	<i>Tangent</i>
<b>Vancomycin</b>	<b>100</b>	<b>0.6%</b>	<b>0.4%</b>	<b>0.3%</b>
<b>I4 Peptide</b>	<b>50</b>	<b>53.0</b>	<b>44.0</b>	<b>25.0</b>
<b>Gramicidin A</b>	<b>200</b>	<b>1.1</b>	<b>0.5</b>	<b>0.0</b>
<b>Crambin</b>	<b>100</b>	<b>4.8</b>	<b>3.7</b>	<b>2.2</b>
<b>Rubredoxin</b>	<b>150</b>	<b>6.0</b>	<b>5.2</b>	<b>4.0</b>
<b>Scorpion Toxin II</b>	<b>200</b>	<b>1.4</b>	<b>1.0</b>	<b>0.7</b>

# *SnB* 2.0 Parameters ( $>1.1\text{\AA}$ )

---

*SnB*

## ◆ Peaks

- ❑  $0.4n$  if “heavy” atoms present
- ❑  $0.8n$  if all *C,N,O*

## ◆ Phase Refinement

- ❑ *Unrestricted* Parameter Shift

## ◆ Cycles

- ❑  $n/2$  if  $n < 400$  and “heavy” atoms present
- ❑  $n$  otherwise

# *SnB* 2.0: Timings

(SGI R10000 Workstation)



<i>Structure</i>	<i>non-H Atoms</i>	<i>Space Group</i>	<i>n/2 Cycles</i>	<i>Trials/ Day</i>	<i>Solns/ Day</i>
<b>Vancomycin</b>	<b>258</b>	<b>P4<sub>3</sub>2<sub>1</sub>2</b>	<b>100</b>	<b>391</b>	<b>1.5</b>
<b>I4 Peptide</b>	<b>289</b>	<b>I4</b>	<b>125</b>	<b>274</b>	<b>110</b>
<b>Gramicidin A</b>	<b>317</b>	<b>P2<sub>1</sub>2<sub>1</sub>2<sub>1</sub></b>	<b>135</b>	<b>572</b>	<b>2</b>
<b>Crambin</b>	<b>~400</b>	<b>P2<sub>1</sub></b>	<b>150</b>	<b>1029</b>	<b>42</b>
<b>Rubredoxin</b>	<b>497</b>	<b>P2<sub>1</sub></b>	<b>200</b>	<b>294</b>	<b>16</b>
<b>Scorpion Toxin II</b>	<b>624</b>	<b>P2<sub>1</sub>2<sub>1</sub>2<sub>1</sub></b>	<b>250</b>	<b>109</b>	<b>0.5</b>

**Note: For each structure, optimum no. of peaks used.**

# Computing Platforms

---

*SnB*

- ◆ **Unix Workstations**

- **SGI, Sun, DEC/Alpha**

- **Wintel/Linux**

- ◆ **Parallel Computers**

- **Cray T3D/E, TMC CM-5, IBM SP2**

- **SGI Origin 2000**

- **HP-Convex Exemplar**

- ◆ **Cray C90**

# Summary

---

*SnB*

- ◆ ***Shake-and-Bake: Dual-Space Direct Methods***
- ◆ **Targeted at 100-800 atom structures**
- ◆ ***SnB* version 2.0**
  - ❑ Optimized code with Inverse FFT
  - ❑ Additional Density Modification Options
  - ❑ Improved Fourier Recycling: “Twice Baking”
  - ❑ I/O: |E| calculation and visualization interface
  - ❑ (SIR/SAS/MAD Invariants with estimated values)
- ◆ **<http://www.hwi.buffalo.edu/SnB/>**

**SnB**

