

First, problem 5 on HW5:

HW 5.5: Given $G=(V,E)$ directed! and $s, t \in V$. \xrightarrow{g} 2CNF ϕ st.

$(x, N) \in \text{ANFA} \Leftrightarrow N$ has a path from s to a final state t that processes x .

$\phi = (s) \wedge (\bar{t}) \wedge \bigwedge_{(u,v) \in E} (\bar{u} \vee v)$

$\phi_G = \bigvee_{s,t \in V} \phi_{s,t}$

ϕ is satisfiable iff there is no path from s to t .

3SAT $\phi = C_1 \wedge C_2 \wedge \dots \wedge C_m$
 $C_j = (\bar{x}_i \vee \bar{x}_k \vee x_l)$
 order s, i, k, l, t

\vec{c} is an acc comp of M on input x .

$\{I_1, I_2\}$ $\{I_t\}$

Problems (1) and (3A) of the exam:

$\text{ANFA} = \{ \langle x, N \rangle : N \text{ is an NFA and } N \text{ accepts } x \}$

$(x, N) \in \text{ANFA} \Leftrightarrow N$ has a path from s to a final state t that processes x .

$\phi = (s) \wedge (\bar{t}) \wedge \bigwedge_{(u,v) \in E} (\bar{u} \vee v)$

$\phi_G = \bigvee_{s,t \in V} \phi_{s,t}$

$M \xrightarrow{f}$ Verifier of computations by M
 V_m B-ADLBA
 can be a ahead w 2-tape DFA
 Runs in linear time etc.

$L(V_m) = \{ \langle M, x, \vec{c} \rangle : \vec{c} \text{ is an acc comp of } M \text{ on input } x \}$

$\{ \langle \neq I_0(x) \neq I_1 \neq I_2 \rangle \}$ $\{I_t\}$

$B = \{ \langle V \rangle : V \text{ is a DLBA and } L(V) \neq \emptyset \}$

B is RE since we can guess x and c

Problem (3B) of the exam:

④ ABET req'd

3SAT

(3b) $\Phi = C_1 \wedge C_2 \wedge \dots \wedge C_m$
 $C_j = (\bar{x}_i \vee \bar{x}_k \vee x_l)$
 order so $i < k < l$

$B = \{ \langle r_1, \dots, r_m \rangle : \exists a \in \{0,1\}^n : a \text{ violates each } r_j \}$
 $f: \mathcal{P}(B) \rightarrow \mathcal{P}(R) \quad R = \langle r_1, \dots, r_m \rangle$

st there is an a that violates each r_j
 \Leftrightarrow the same a satisfies each C_j in Φ .

$r_j = \underbrace{(0+1) \dots (0+1)}_{i-1 \text{ don't care}} \mid \underbrace{(0+1) \sim (0+1)}_{\text{pos } k-1} \mid \underbrace{(0+1) \dots (0+1)}_{\text{pos } l-1} \mid \underbrace{(0+1) \sim (0+1)}_{\text{pos } n}$

BENE since we can guess a