

This *closed-book/closed-notes* quiz counts as 40 points toward assignments, as provided on the printed course syllabus. Each question is multiple choice and has a unique best answer worth 4 points. (If you have doubt between two answers, partial credit may be given for a written justification of your choice.) Please **circle** your chosen answer.

YOUR NAME+ID HERE:

(1) A *proposition* can be:

- (a) A statement like “this cat has nine lives.”
- (b) A variable like  $P$  or  $Q$ .
- (c) A compound statement like  $P \vee (Q \rightarrow P)$ .
- (d) A predicate  $P(x)$  where  $x$  is replaced by a particular value.
- (e) All of the above.

(2) An implication  $P \rightarrow Q$  is guaranteed to be true when:

- (a)  $P$  is true.
- (b)  $Q$  is true.
- (c)  $Q \rightarrow P$  is true.
- (d) One of  $P$  or  $Q$  is false.

(3) A *formula* or *predicate*  $F(x_1, \dots, x_n)$  with free variables  $\vec{x} = x_1, \dots, x_n$  becomes a proposition (in lecture I preferred to say *sentence* or *propositional sentence*) when and only when:

- (a) Every variable is filled in by an instance element.
- (b) Every variable is quantified.
- (c) Every variable is either filled in or quantified.
- (d) It is always true, i.e., when  $(\forall \vec{x})F(\vec{x})$  is true.

(4) If a Boolean formula  $F$  is true when all of its variables are false, then:

- (a)  $F$  is a tautology.
- (b)  $F$  is satisfiable.
- (c)  $F$  is unsatisfiable.
- (d)  $F$  is a contradiction-in-terms.

(5) An example of a Boolean formula that is true when all of its variables are false is:

- (a)  $P \wedge Q$ .
- (b)  $P \vee Q$ .
- (c)  $P \rightarrow Q$ .
- (d)  $P \text{ xor } Q$ .

(6) The Boolean formula  $P \vee Q \rightarrow R \wedge S$  is read as:

- (a)  $(P \vee (Q \rightarrow R)) \wedge S$ .
- (b)  $P \vee ((Q \rightarrow R) \wedge S)$ .
- (c)  $((P \vee Q) \rightarrow R) \wedge S$ .
- (d)  $(P \vee Q) \rightarrow (R \wedge S)$ .

(7) The statement “ $P$  if  $Q$ ” means:

- (a)  $P \rightarrow Q$ .
- (b)  $Q \rightarrow P$ .
- (c) Both (a) and (b).
- (d) Neither (a) nor (b).

(8) The formulas  $P \text{ xor } Q$  and  $\neg(P \leftrightarrow Q)$  are:

- (a) Tautologies.
- (b) Logically equivalent (in lecture I said “semantically equivalent”).
- (c) Both unsatisfiable.
- (d) Inconsistent with each other.

(9) The logical argument “Given  $P \rightarrow Q$  and  $Q$ , we can conclude that  $P$  is true” is:

- (a) Valid.
- (b) A fallacy.
- (c) True by default.
- (d) OK if you make it before breakfast.

(10) The person who is most honored for making logic into a branch of mathematics, even named in the basic `true/false` type of programming languages such as Java, C, and C++, lived:

- (a) In ancient Greece.
- (b) In the Middle Ages or Renaissance.
- (c) In the 1800's.
- (d) Until a few years ago.