

Closed book, closed-notes-except-for-1-sheet, closed neighbors, 48 minutes. Do ALL THREE questions on the exam pages themselves. Please *show all your work*; this may help for partial credit. The exam totals 67 pts., subdivided as shown.

**(1) (6 + 4 + 4 + 4 + 6 + 4 = 28 pts. total)**

First, let us employ the simple hash function  $h$  that adds up the index-numbers of all letters in alpha-order  $a = 1$ ,  $b = 2$ ,  $c = 3$ , etc. For instance,  $h(\text{"bud"}) = 2+21+4 = 27$ , which gives  $3 \bmod 8$ .

- (a) For a hash table with chaining of size 8 that is behaving like a set, insert the four words **bad** **bed** **bid** **dad** in that order.
- (b) Now iterate thru the hash table from bucket 0 down to 7, and reinsert the items in *that* order into a hash table of size 4.
- (c) Take the same iteration in (b) and insert the words into a binary search tree, using alphabetical order as the comparison function.
- (d) This time show the BST that results from the insertion sequence **bad** **bed** **bid** **dad** as in (a).
- (e) Now show the steps and result of forming a heap out of the length-4 vector **bad** **bed** **bid** **dad**, keeping the maximum word in alphabetical order on top. You may use either the technique of inserting the words in that order into an initially empty heap, or the generally-faster results of calling `make_heap` on the vector as given.
- (f) Comparing your answers to (c) and (d), and thinking of all the data structures in this problem, suppose you had a longer vector in sorted order like **bad** **bed** **bid** **dad** **did** **eat** **fat** **goose**... How would you try to make a well-balanced binary search tree out of that vector?

**(2) (9 × 3 = 27 pts. total)**

For each task below labeled 1.–10., say which of the following best describes its running time:

- (a) Guaranteed  $O(1)$  time.
- (b) Amortized  $O(1)$  time.
- (c) Usually  $O(1)$  time.
- (d) Guaranteed  $O(\log n)$  time.
- (e) Usually  $O(\log n)$  time.
- (f) Guaranteed  $O(n)$  time.

In all cases  $n$  denotes the number of items currently in the underlying data structure, and any other parameters are stated. The variable `vec` stands for a vector, `dlist` for a doubly-linked list (not necessarily sorted), `valli` for a “Valli” data structure, `bst` for a BST—i.e. a general binary search tree, `itr` for an iterator of the appropriate kind, and `item` for a typical item in the data structure. *Justifications* are not required, but might help for partial credit. The tasks are:

1. For a BST iterator `itr`, the call `itr++`; -----
2. `dlist.push_back(item)`; (equivalently, `dlist.insert(dlist.end(), item)`); -----
3. `vec.push_back(item)`; -----
4. `dlist.erase(itr)`; -----
5. `vec.erase(itr)`; where `itr` points in the middle of `vec`. -----
6. For a Valli iterator `itr`, the call `itr++`; -----
7. `valli.find(item)`;, assuming `valli` just refreshed with `ratio r = log2(n)`. -----
8. `bst.find(item)`; -----
9. Preorder traversal of a BST. -----

**(3) (12 pts.)**

Suppose Project 1 had been changed to make you create a set of words that do **not** remain words when “turned inside out.” That is, suppose you have the following containers:

```
vector<string> words;
Valli<string> turnedWords;
...
//assume you've already run code that reads the dictionary file into words
//and for every read word, inserts wordTurn(word) into the Valli container.
...
set<string> unturnables;    //initially the empty set
...
//your code on this problem goes here.
```

Write code with iterators that inserts into `untturnables` every word that is *not* in `turnedWords`—that is, not equal to the turning of itself or some other word. END OF EXAM