

Sep 6

Def. (Preference list)  $\forall w \in W, L_w$ : total ranking of all men  $m \in M$   
 $\forall m \in M, L_m$ : total ranking of all women  $w \in W$

Ex:  $n = 2$

$M = \{BP, BBT\}$

$W = \{JA, AJ\}$

$L_{BP}$ :  $AJ > JA$

$L_{JA}$ :  $BP > BBT$

$L_{BBT}$ :  $AJ > JA$

$L_{AJ}$ :  $BP > BBT$

$2n$ : preference list.  
 $2n \times n = 2n^2$  elements overall

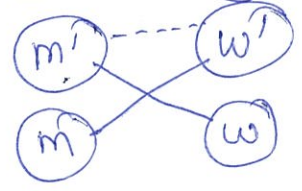
Def: A stable matching is a perfect matching with no instability

Def: Instability: Given the  $2n$  pref. lists, a perfect matching  $S$  we say a pair  $(m', w') \notin S$  is an instability IF

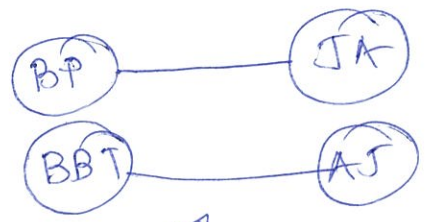
(1)  $m' > m$  in  $L_{w'}$

AND

(2)  $w' > w$  in  $L_{m'}$ .



Ex:



NOT a stable matching!

Q1: Is  $(BBT, JA)$  an instability?  $\leftarrow$  NO  
 Q2: Is  $(BP, AJ)$  an instability?  $\leftarrow$  YES!