

# Lecture 18

CSE 331

Oct 11, 2023

# Please do fill in the feedback

note @281

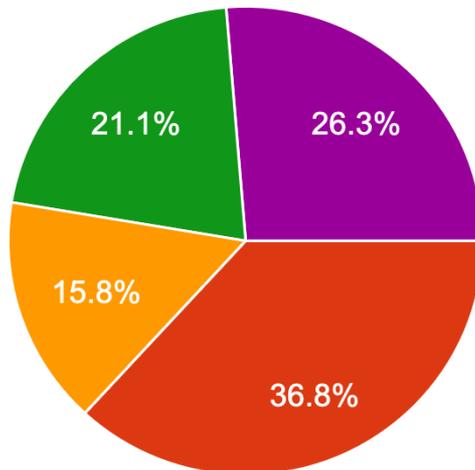
stop following 2 views

Actions

## Feedback on CSE 331

Overall your feeling about CSE 331

19 responses



- Very Happy
- Challenged and happy
- Challenged and meh
- Challenged and unhappy
- Challenged and very unhappy
- I'm bored!

# Mid-terms next week

Mid-term 1: next Wed in class

Mid-term 2: Fri next week in class

# Grading status

Hopefully by tonight: Quiz 1, HW 3

# Project Coding submissions

 note @305   

stop following **39 views**

Actions ▾

## Issue with project coding submissions

So it seems like with the latest update to Autolab has broken a part of the grading of the coding projects (currently the issue has been reported for Problem 1 but I suspect the issue will be there for other problems as well).

Specifically, Autolab assigns the correct grade to the student who submits for the group but incorrectly throws an error for the other students in the group.

So going forward:

- I'll be implementing a fix for that and hope to be done **by the end of the week**
  - Once the fix is in place, I'll ask everyone who has already submitted to re-submit.
- In the meantime, y'all can still submit your code to check if your submission works-- it's just that for now please only look at the score assigned to the student who submit.

Thanks to those brought this to my notice and apologies for any inconvenience this might cause y'all.

autolab project

Edit good note | 0

Updated 6 hours ago by Atri Rudra

# HW 4 is out

## Homework 4

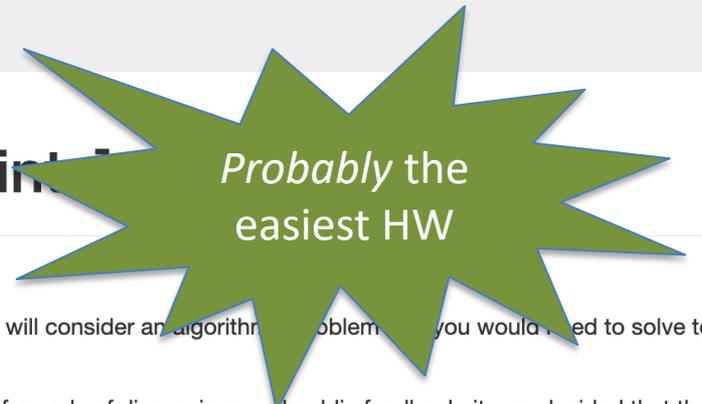
Due by **11:30pm, Tuesday, October 17, 2023.**

Make sure you follow all the [homework policies](#).

All submissions should be done via [Autolab](#).

The [care package on minimizing the maximum lateness problem](#) would be useful for Q3 and *might* be useful for Q2(b) as well.

### Question 1 (High Speed Internet) [50 points]



#### The Problem

We come back to the issue of many USA regions not having high speed internet. In this question, you will consider an algorithmic problem that you would need to solve to help out a (fictional) place get high speed Internet.

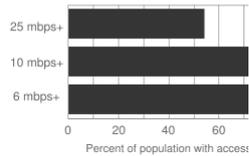
You are the algorithms whiz in the effort to bring high speed Internet to **SomePlaceInUSA**. After lots of rounds of discussions and public feedback, it was decided that the most cost-effective way to bring high speed internet to **SomePlaceInUSA** was to install high speed cell towers to connect all houses in **SomePlaceInUSA** to high speed internet. There are two things in your favor:

1. It just so happens that all of the  $n$  houses in **SomePlaceInUSA** are on the side of a straight road that runs through the town.

# Make broadband more available

## Cattaraugus County

Population: 79518  
Median Income: \$41,368.88  
Access to any cable technology: 67.5%  
Access to two or more wireline providers: 61.2%

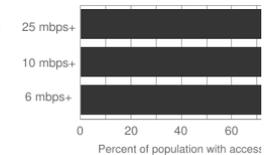


Say you are tasked to come up with the infrastructure

BOTH technical and societal issues

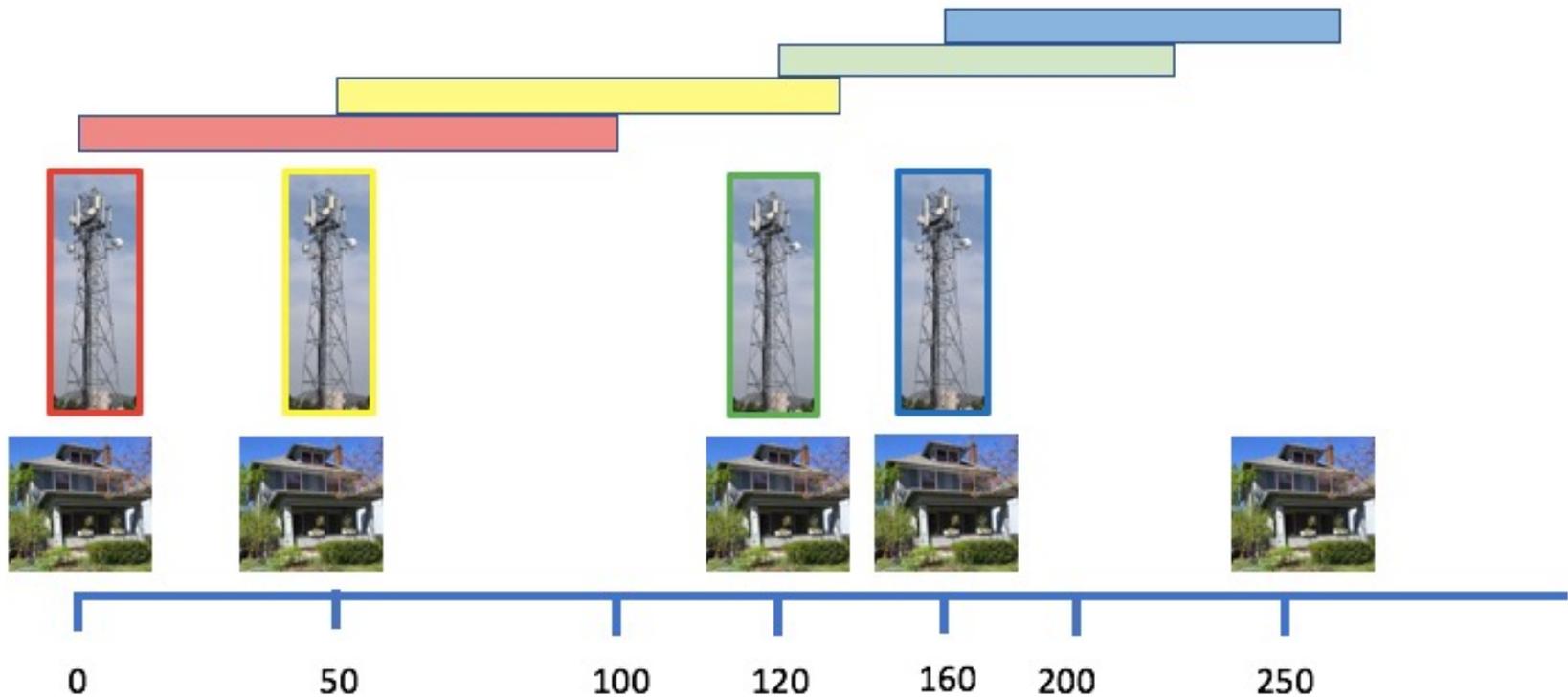
## Erie County

Population: 913295  
Median Income: \$49,817.67  
Access to any cable technology: 98.9%  
Access to two or more wireline providers: 96.8%



# HW 4 Q1: How to lay down towers

Here is a quick visual argument for the above leads to continuous cell coverage:



# Interval Scheduling Problem

**Input:**  $n$  intervals  $[s(i), f(i))$  for  $1 \leq i \leq n$

**Output:** A schedule  $S$  of the  $n$  intervals

No two intervals in  $S$  conflict

$|S|$  is maximized

# Analyzing the algorithm

$R$ : set of requests

Set  $S$  to be the empty set

While  $R$  is not empty

    Choose  $i$  in  $R$  with the earliest finish time

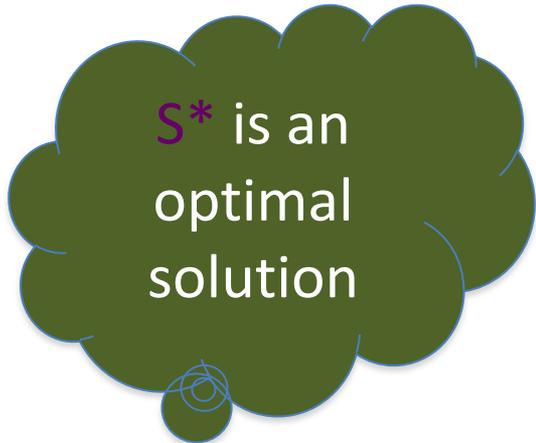
    Add  $i$  to  $S$

    Remove all requests that conflict with  $i$  from  $R$

Return  $S^* = S$



$S^*$  has no conflicts



$S^*$  is an optimal solution

# Greedy “stays ahead”



# Greedy stays ahead lemma

$$S^* = \{i_1, \dots, i_k\}$$

$$O = \{j_1, \dots, j_m\}$$

Lemma 1: For all  $1 \leq \ell \leq k$

$$f(i_\ell) \leq f(j_\ell)$$

# Questions?



# Proof of Lemma 1 on the board...



# Runtime analysis of Greedy Algo.

$R$ : set of requests

$O(1)$

Set  $S$  to be the empty set

Repeated at most  $n$  times

While  $R$  is not empty

$O(n)$

$O(1)$

Choose  $i$  in  $R$  with the earliest finish time

Add  $i$  to  $S$

$O(n)$

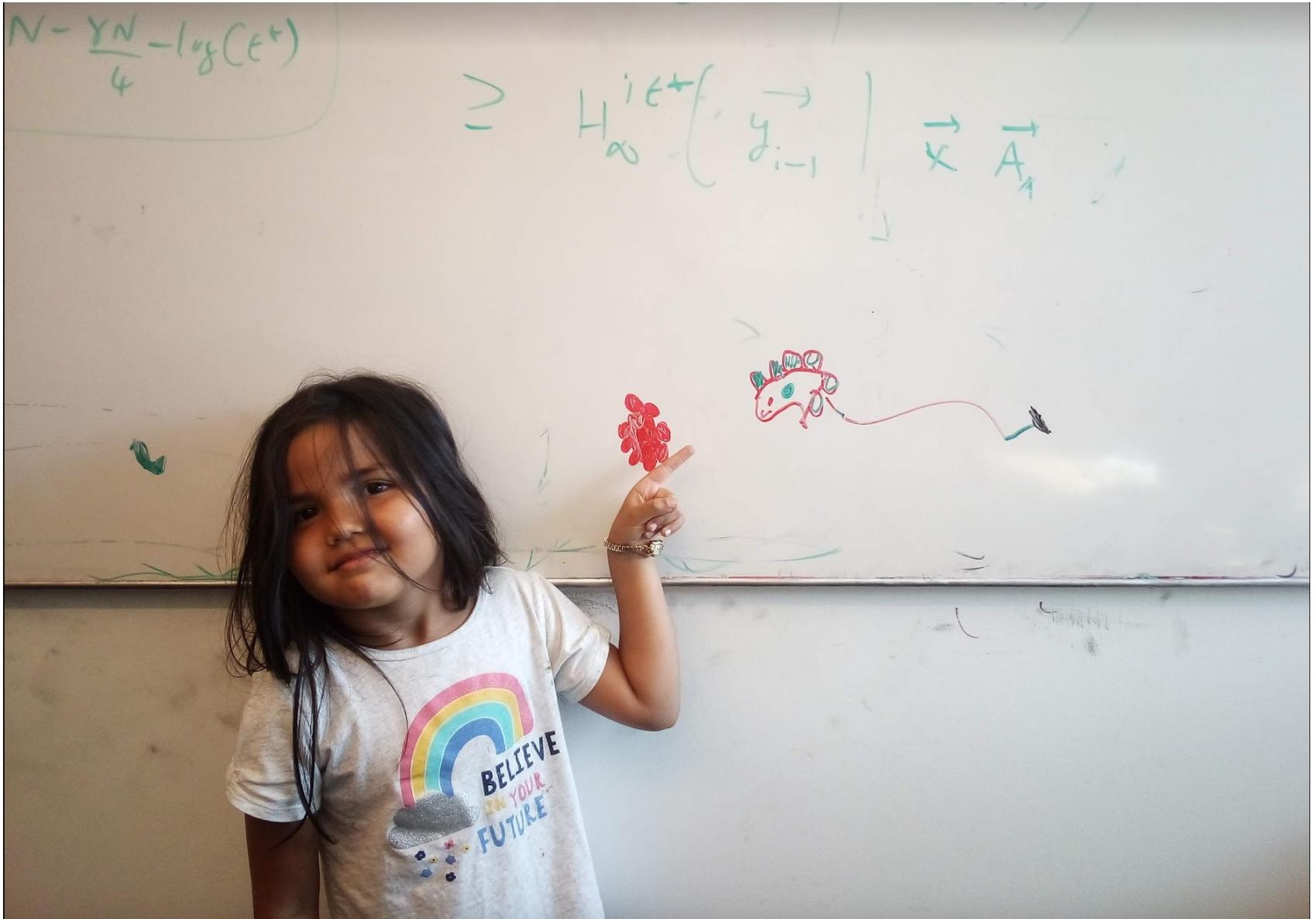
Remove all requests that conflict with  $i$  from  $R$

Return  $S^* = S$

$O(n)$

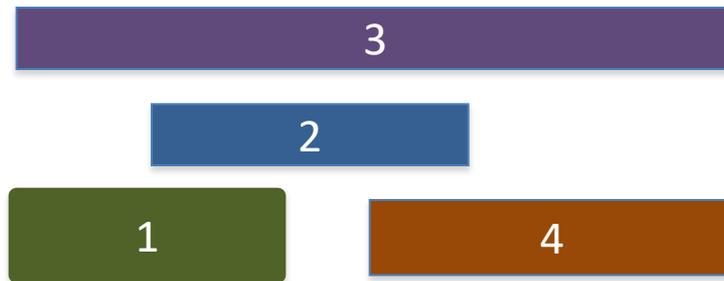
Overall:  
 $O(n) +$   
 $n * O(n) =$   
 $O(n^2)$

# Questions/Comments?



# Algorithm implementation

Go through the intervals in order of their finish time



Check if  $s[i] < f(1)$

with 1:

In general, if  $j$ th interval is the last one chosen

Pick smallest  $i > j$  such that  $s[i] \geq f(j)$

$O(n \log n)$  run  
time

# The final algo

$O(n \log n)$  time sort intervals such that  $f(i) \leq f(i+1)$

$O(n)$  time build array  $s[1..n]$  s.t.  $s[i]$  = start time for  $i$

Add 1 to  $S$  and set  $f = f(1)$

For  $i = 2 .. n$

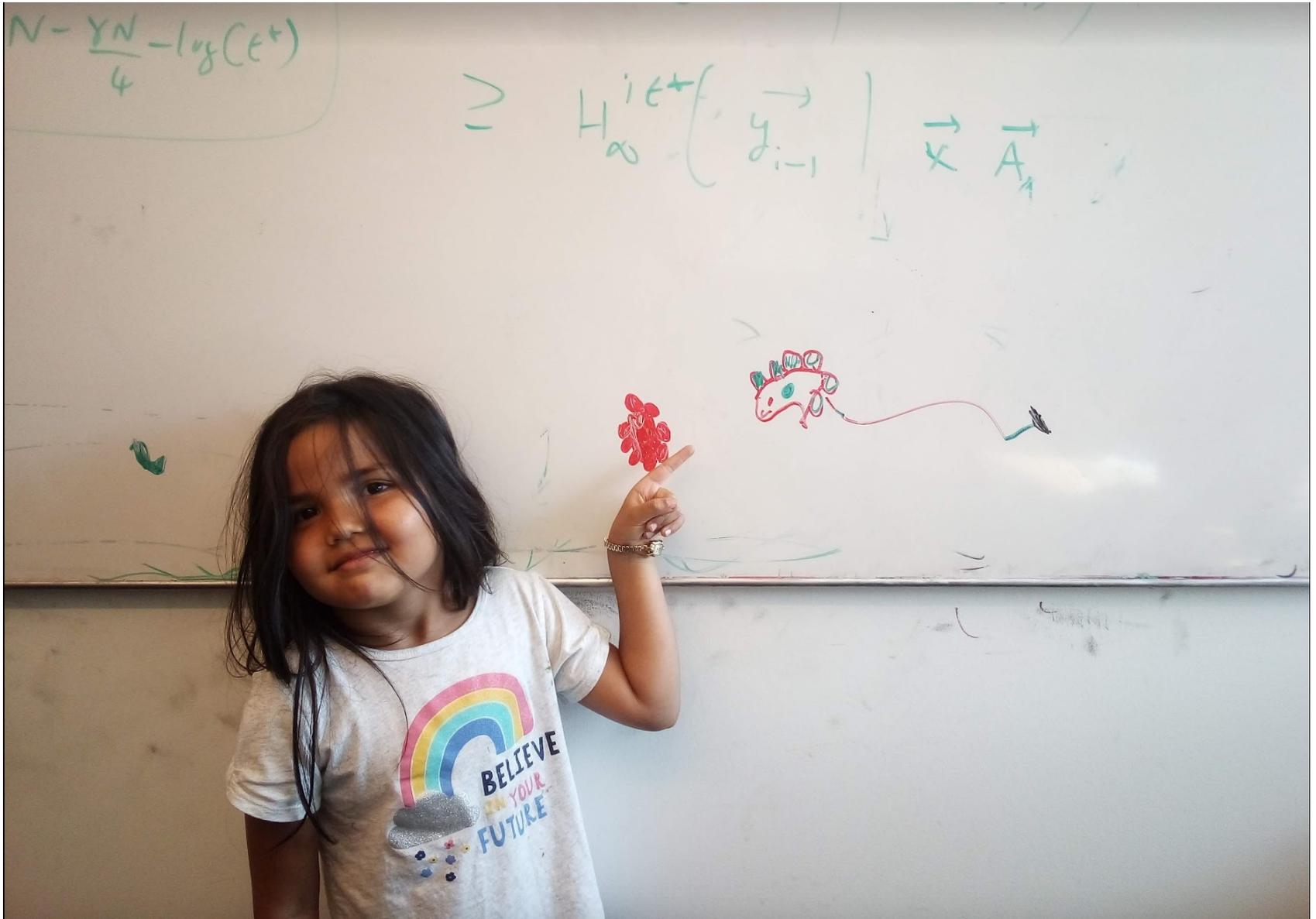
    If  $s[i] \geq f$

        Add  $i$  to  $S$

        Set  $f = f(i)$

Return  $S^* = S$

# Questions/Comments?



# Reading Assignment

Sec 4.1 of [KT]



# The “real” end of Semester blues

There are deadlines and durations of tasks



Write up a term paper

Party!

Exam study

331 HW

Project

Friday

Saturday

Sunday

Monday

Tuesday

# The “real” end of Semester blues

There are deadlines and durations of tasks



Write up a term paper

Exam study

Party!

331 HW

Project

Friday

Saturday

Sunday

Monday

Tuesday

# The algorithmic task

YOU decide when to start each task



Write up a term paper

Exam study

Party!

331 HW

Project

You have to do ALL the tasks

Friday

Saturday

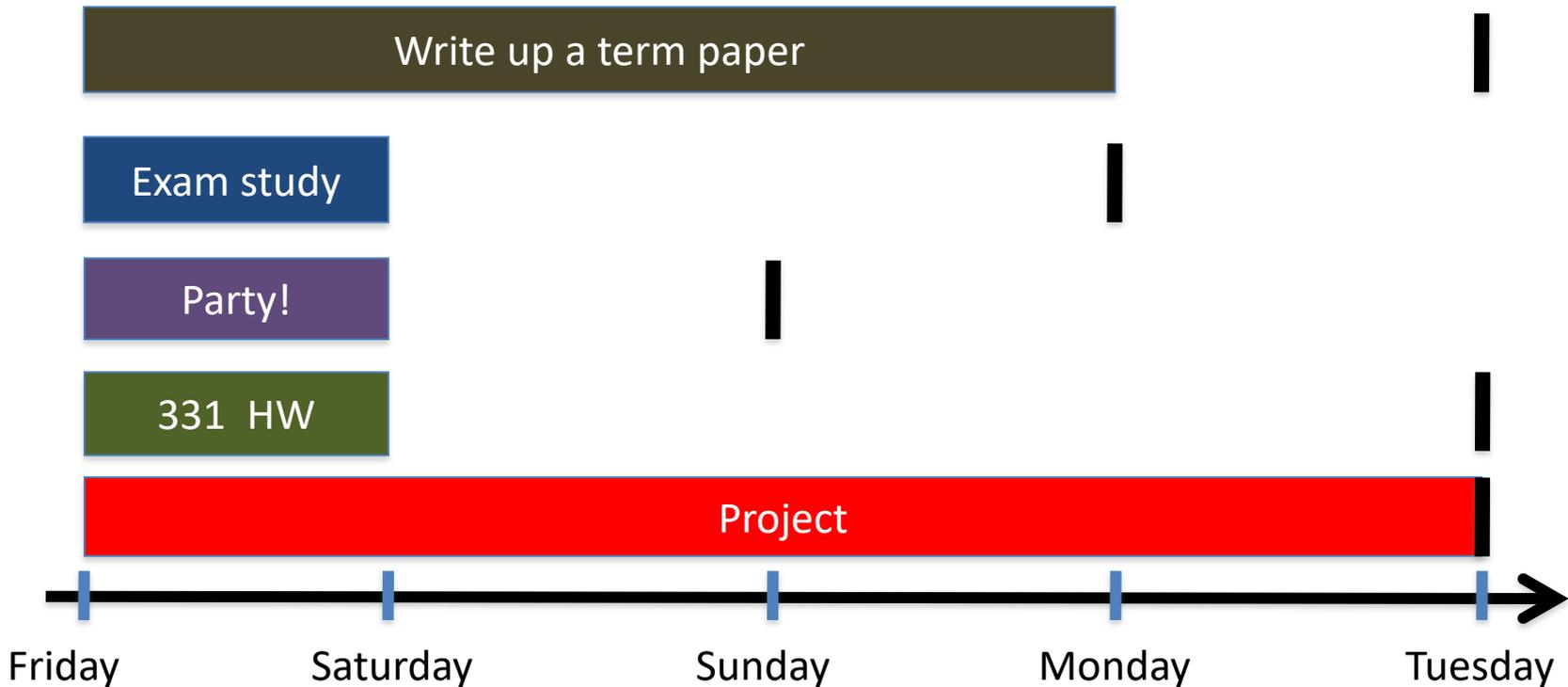
Sunday

Monday

Tuesday

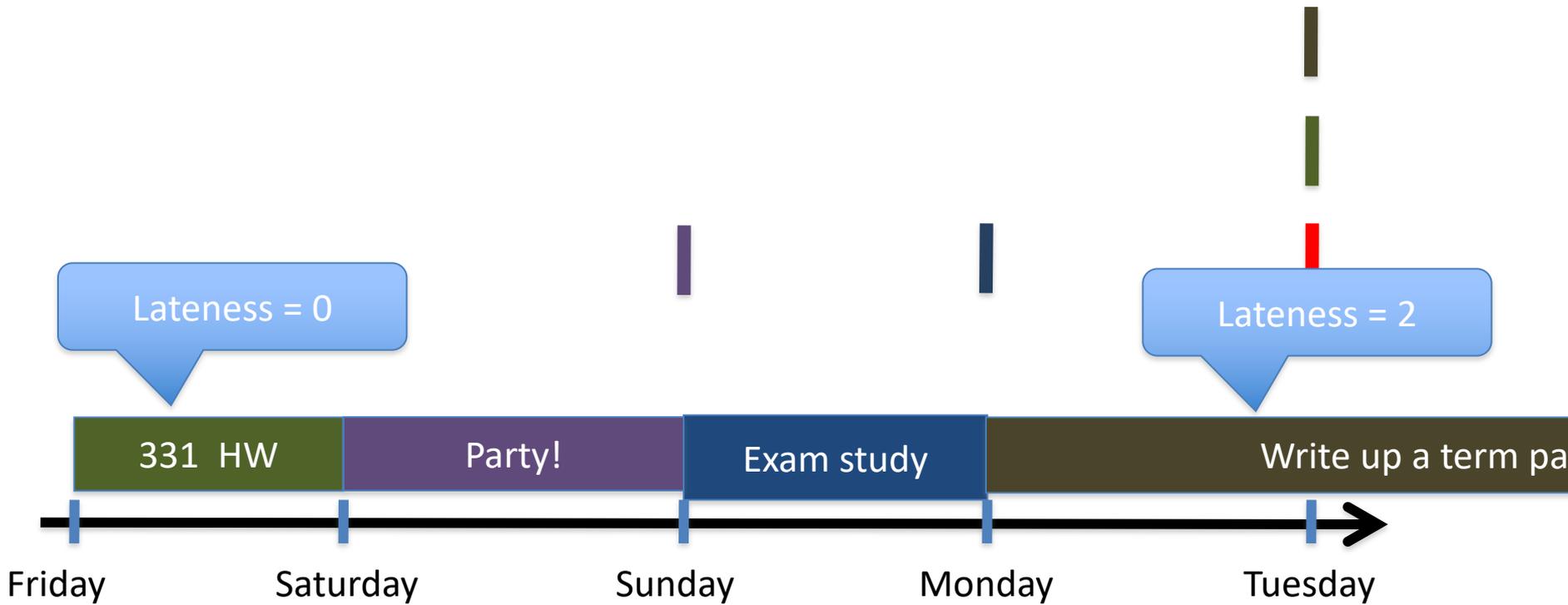
# Scheduling to minimize lateness

All the tasks have to be scheduled  
GOAL: minimize maximum lateness



# One possible schedule

All the tasks have to be scheduled  
GOAL: minimize maximum lateness



# Minimizing Max Lateness

## Minimizing Maximum Lateness

This page collects material from previous incarnations of CSE 331 on scheduling to minimize maximum lateness.

### Where does the textbook talk about this?

[Section 4.2](#) in the textbook has the lowdown on the problem of scheduling to minimize maximum lateness.

### Fall 2018 material

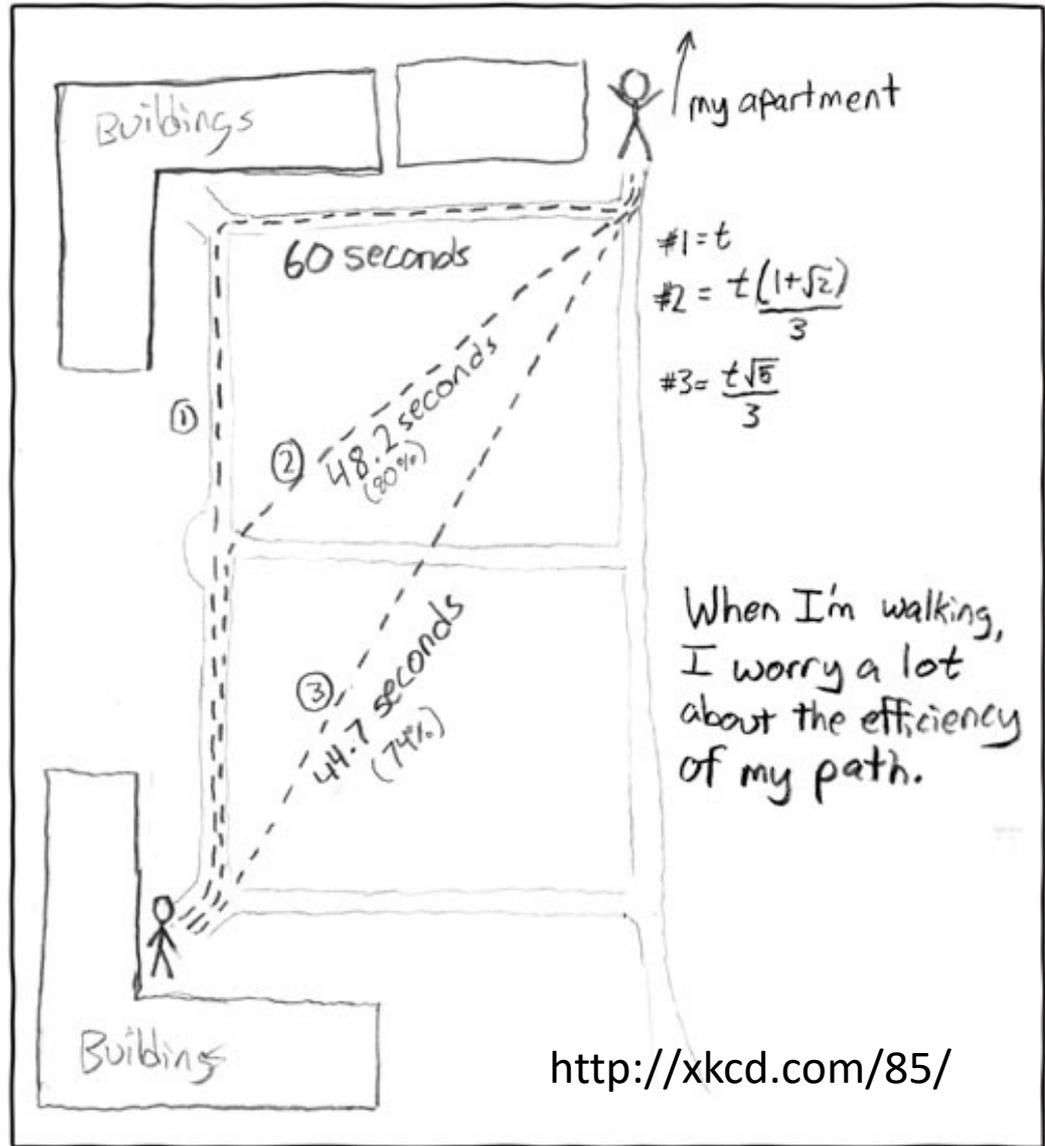
#### First lecture

Here is the lecture video:



# Rest of today

## Shortest Path Problem



# Reading Assignment

Sec 2.5 of [KT]

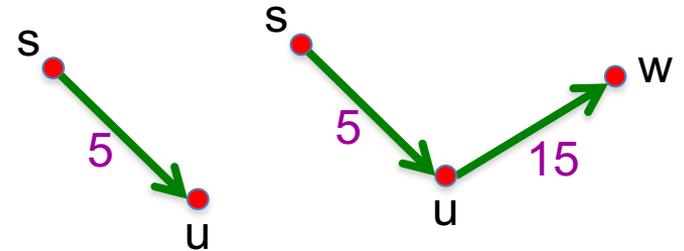
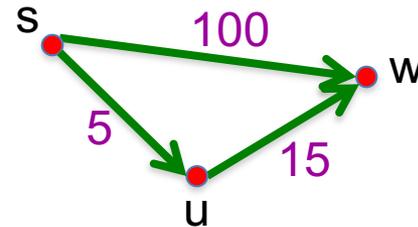


# Shortest Path problem

**Input:** *Directed* graph  $G=(V,E)$

Edge lengths,  $\ell_e$  for  $e$  in  $E$

“start” vertex  $s$  in  $V$



**Output:** All shortest paths from  $s$  to all nodes in  $V$

# Naïve Algorithm

$\Omega(n!)$  time

# Dijkstra's shortest path algorithm

