

# Lecture 30

CSE 331

Nov 13, 2023

# HW 6 Q1+2 templates buggy

question @461 ⊞ ★ 🔒 stop following 32 views Actions ▾

## Question of subsections in LaTeX

It seems that Collaborator and Sources have disappeared from latex template since HW5. Even though I can type them by myself, may I ask that is there any chance we'll see them back in the rest of HWs (I'm a bit lazy)?

Thank you!

*(Making this public. --Atri)*

homework6

~ An instructor (Atri Rudra) endorsed this question ~

# Reflections 1+2 grading

note @466   

stop following **16 views**

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## Reflections 1+2 grading timeline

I'll be grading all the reflections for the project.

I'm hoping to get both the reflections graded in 1-2 weeks time but in the worst-case I'll get them done around a week before reflections 3 is done (so worst-case a day or two after the Thanksgiving break).

project

Edit good note | 1

Updated 3 minutes ago by Atri Rudra

# Final exam conflict

note @447

stop following 19 views

Actions

## Final exam conflicts

I know some of you have an exam conflict with CSE 331 final exam. Since I'm not sure if I know the exact set of students with conflict, I figured I'll do a piazza post.

**If you have an exam conflict with the CSE 331 final please EMAIL me by 5pm on Friday, Nov 17.** If you email me after this deadline, I cannot promise to be able to give you a makeup option that works with your schedule.

Please note that the makeup final will be on *Tuesday, Dec 12* (i.e. a day before the scheduled final exam). My goal is to pick a time that works for everyone on Dec 12.

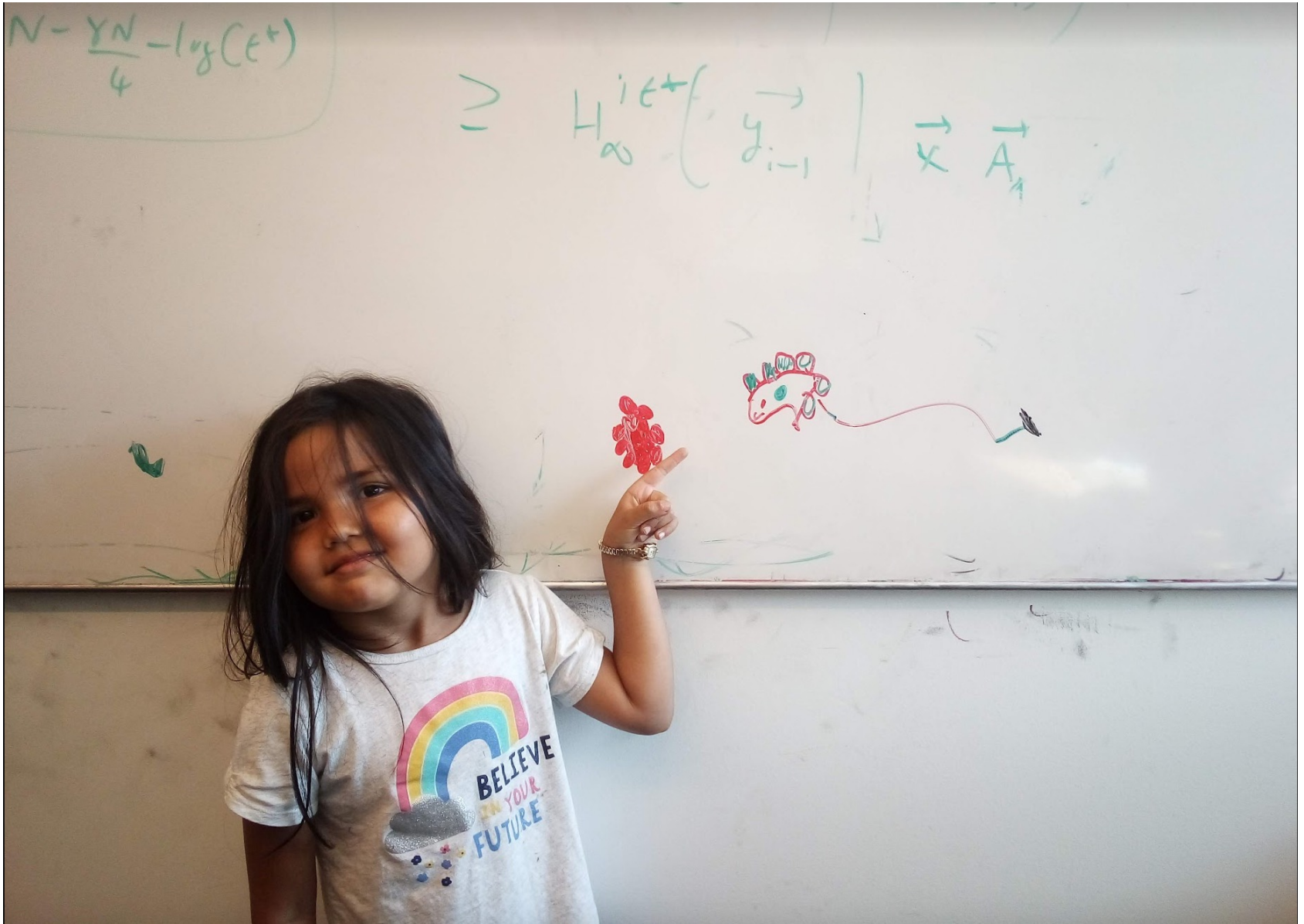
So if you email me for a makeup final exam, please send me all the time(s) that you do a makeup on Tuesday, Dec 12 between 9am-5pm.

final

Edit good note 1

Updated 60 minutes ago by Atri Rudra

# Questions/Comments?



# End of Semester blues

Can only do one thing at any day: what is the optimal schedule to obtain maximum value?



Write up a term paper (10)

Party! (2)

Exam study (5)

331 HW (3)

Project (30)

Friday

Saturday

Sunday

Monday

Tuesday

# Previous Greedy algorithm

Order by end time and pick jobs greedily

Greedy value =  $5+2+3=10$

Write up a term paper (10)

Party! (2)

Exam study (5)

331 HW (3)

Project (30)

OPT = 30



Friday

Saturday

Sunday

Monday

Tuesday

# Weighted Interval Scheduling

Input:  $n$  jobs  $(s_i, f_i, v_i)$

Output: A schedule  $S$  s.t. no two jobs in  $S$  have a conflict

Goal:  $\max \sum_{i \in S} v_j$

Assume: jobs are sorted by their finish time



# Today's agenda

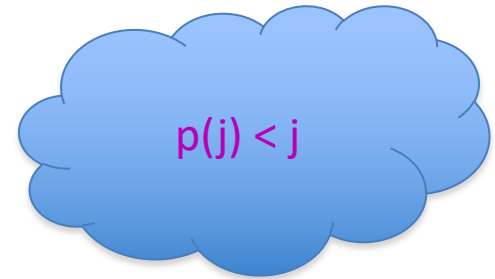
Finish designing a recursive algorithm for the problem



# Couple more definitions

$p(j)$  = largest  $i < j$  s.t.  $i$  does not conflict with  $j$

= 0 if no such  $i$  exists



$OPT(j)$  = optimal value on instance  $1, \dots, j$

# Moving to the board...



# Property of OPT

$j$  in  $\text{OPT}(j)$

$j$  not in  $\text{OPT}(j)$

$$\text{OPT}(j) = \max \{ v_j + \text{OPT}(p(j)), \text{OPT}(j-1) \}$$

Given  $\text{OPT}(1), \dots, \text{OPT}(j-1)$ ,  
how can one figure out if  $j$   
in optimal solution or not?



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# A recursive algorithm

Compute-Opt( $j$ )

Correct for  $j=0$

Proof of correctness by induction on  $j$

If  $j = 0$  then return 0

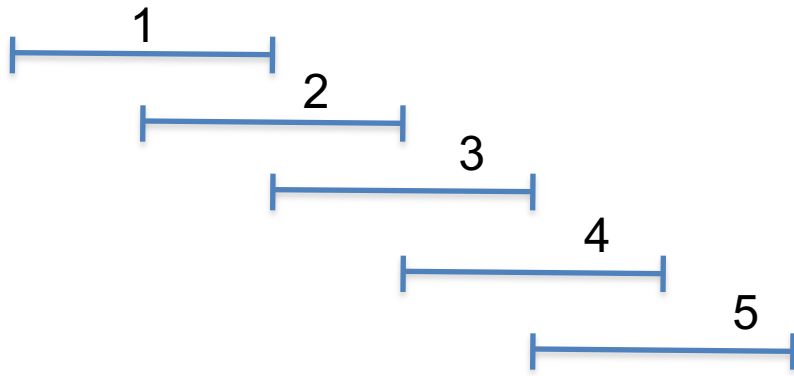
return  $\max \{ v_j + \text{Compute-Opt}(p(j)), \text{Compute-Opt}(j-1) \}$

$= \text{OPT}(p(j))$

$= \text{OPT}(j-1)$

$$\text{OPT}(j) = \max \{ v_j + \text{OPT}(p(j)), \text{OPT}(j-1) \}$$

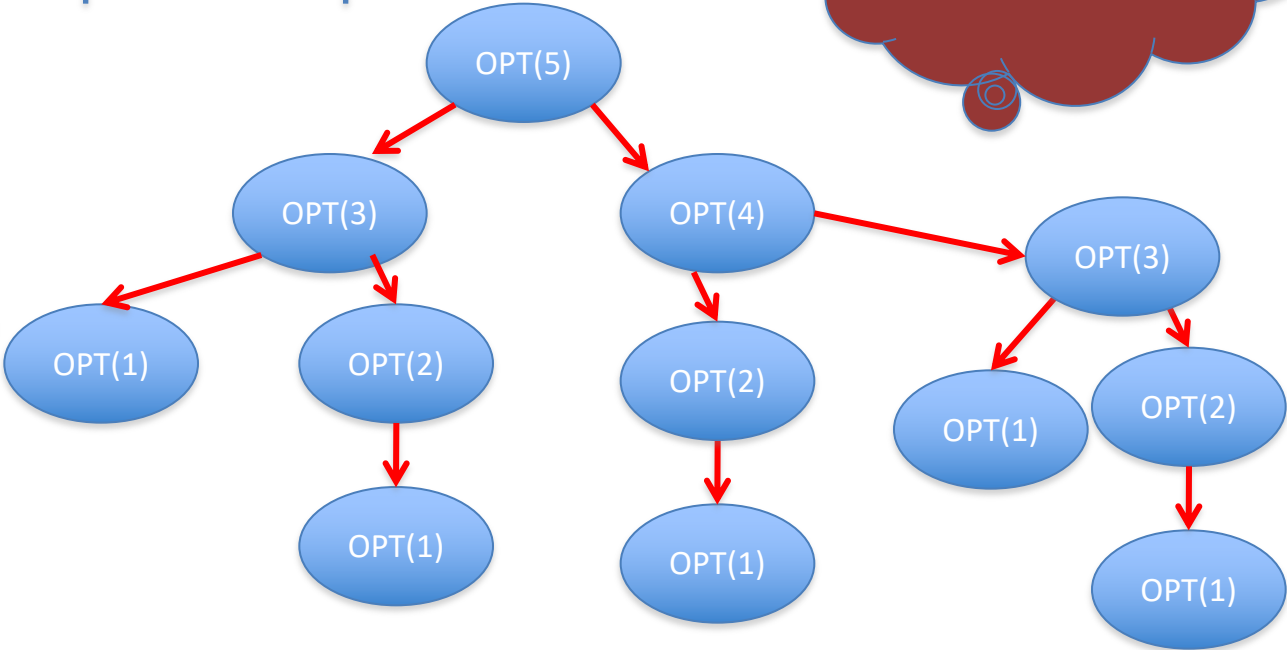
# Exponential Running Time



$$p(j) = j - 2$$

Only 5 OPT values!

Formal proof: Ex.





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# Using Memory to be smarter

Using more space can reduce runtime!

How many distinct OPT values?

# A recursive algorithm

M-Compute-Opt(j)

If  $j = 0$  then return 0

If  $M[j]$  is not null then return  $M[j]$

$M[j] = \max \{ v_j + \text{M-Compute-Opt}(p(j)), \text{M-Compute-Opt}(j-1) \}$

return  $M[j]$

M-Compute-Opt(j)  
= OPT(j)

Run time =  $O(\# \text{ recursive calls})$