

# Lecture 13

CSE 331

Sep 25, 2024

# Quiz 1 on Monday

note @126

stop following **0 views**

Actions

## Quiz 1 on Monday, Sep 30

The first quiz will be from **11:00-11:10am in class on Monday, September 30**. We will have a 5 mins break after the quiz and the lecture will start at 11:15am.

We will hand out the quiz paper at 10:55am but you will **NOT** be allowed to open the quiz to see the actual questions till 11:00am. However, you can use those 5 minutes to go over the instructions and get yourself in the zone.

There will be two T/F with justification questions (like those in the T/F polls.) I will post sample mid-terms by Wednesday night so that you'll be able to see the formatting of such T/F questions.

Also quiz 1 will cover all topics we cover in class until Friday, Sep 27.




































Also like the mid-term y'all can bring in one letter sized cheat-sheet (you can use both sides). But other than cheatsheet and writing implements nothing else is allowed.

quiz1

Edit good note | 0

Updated 1 second ago by Atri Rudra

# Busy 2 weeks ahead....

Mon, Sep 23	Breadth First Search  F23  F22  F21  F19  F18  F17 x <sup>2</sup>	[KT, Sec 3.2]
Tue, Sep 24		(HW 3 out, HW 2 in)
Wed, Sep 25	Explore algorithm  F23  F22  F21  F19  F118  F17 x <sup>2</sup>	[KT, Sec 3.3]
Fri, Sep 27	Runtime Analysis of BFS algorithm  F23  F22  F21  F19  F18  F17 x <sup>2</sup>	[KT, Sec 3.3, 3.6] <i>Reading Assignment:</i> [KT, Sec 3.3, 3.4, 3.5, 3.6] <i>Reading Assignment:</i> <a href="#">Care package on topological ordering</a>
Mon, Sep 30	More graph stuff  F23  F22  F21  F19  F18  F17 x <sup>2</sup>	[KT, Sec 3.3, 3.6] (Quiz 1) (Group Registration on Autolab due)
Tue, Oct 1		(HW 3 in)
Wed, Oct 2	Interval Scheduling Problem  F23  F22  F21  F19  F18  F17 x <sup>2</sup>	[KT, Sec 4.1] (Project out) <i>Reading Assignment:</i> [KT, Sec 4.1, 4.2]
Fri, Oct 4	Greedy Algorithm for Interval Scheduling  F23  F22  F19  F18  F17 x <sup>2</sup>	[KT, Sec 4.4] <i>Reading Assignment:</i> <a href="#">Care package on minimizing maximum lateness</a>
Mon, Oct 7	<b>Mid-term exam: I</b>	
Wed, Oct 9	<b>Mid-term exam: II</b>	

# HW 3 out

## Homework 3

Due by **11:30pm, Tuesday, October 1, 2024.**

Make sure you follow all the [homework policies](#).

All submissions should be done via [Autolab](#).

## Sample Problem

### The Problem

This problem is just to get you thinking about graphs and get more practice with proofs.

A **forest** with  $c$  components is a graph that is the union of  $c$  disjoint trees. The figure below shows for an example with  $c = 3$  and  $n = 13$  with the three connected components colored blue, red and yellow).



### ! For those of you who are feeling a little ambitious

For the top 3 submissions in the scoreboard in Python, the top 2 submissions in the scoreboard in Java and the top submission in the scoreboard in C++, we are offering 2.5 bonus points. But be warned! You should not be spending too much time on this. We rather you work on Questions 1 and 2 above.



Note that a tree is a forest with 1 component.



# Read the instruction carefully

## Autolab group registration for CSE 331 Project

- Project Overview
- Project Autolab page
- Group signup form

The lowdown on registering your [project group](#) on Autolab.

## Fill in the Group Composition form FIRST

Make sure you fill in [this Google form](#) to submit your group composition. Please see the [project overview page](#) for more details on this.

### You **HAVE** to submit the Google form

You **have** to submit [this Google form](#) by **11:30pm on Friday, September 20**. If you do not fill in the form on time, then you will not be able to register your group on Autolab and **will get a ZERO (0) on the ENTIRE project**.

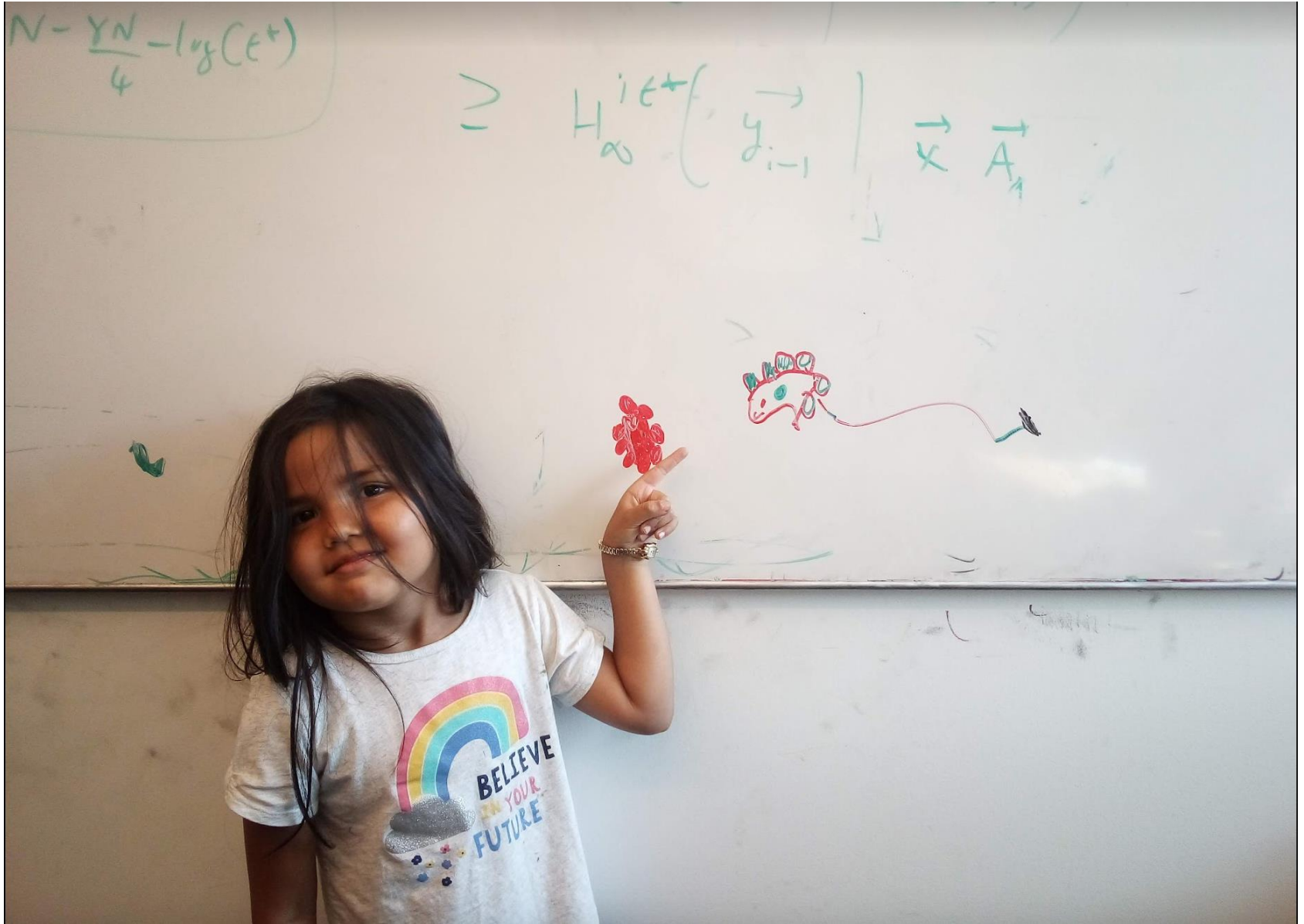
## Register your group on Autolab

### Groups on Autolab will **NOT** be automatically registered

Even after filling the Google form for your group composition you will have to register your group on Autolab by yourself (as a group). Read on for instructions on how to go about this.

However, once you register your group on Autolab you will **not** have to form your group for the coding and reflections submissions.

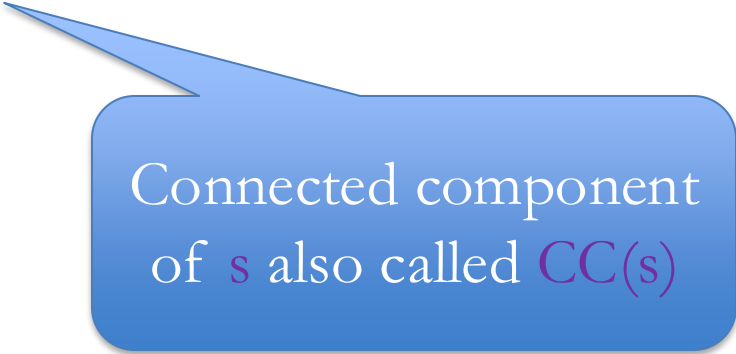
# Questions/Comments?



# Connectivity Problem

*Input:* Graph  $G = (V, E)$  and  $s$  in  $V$

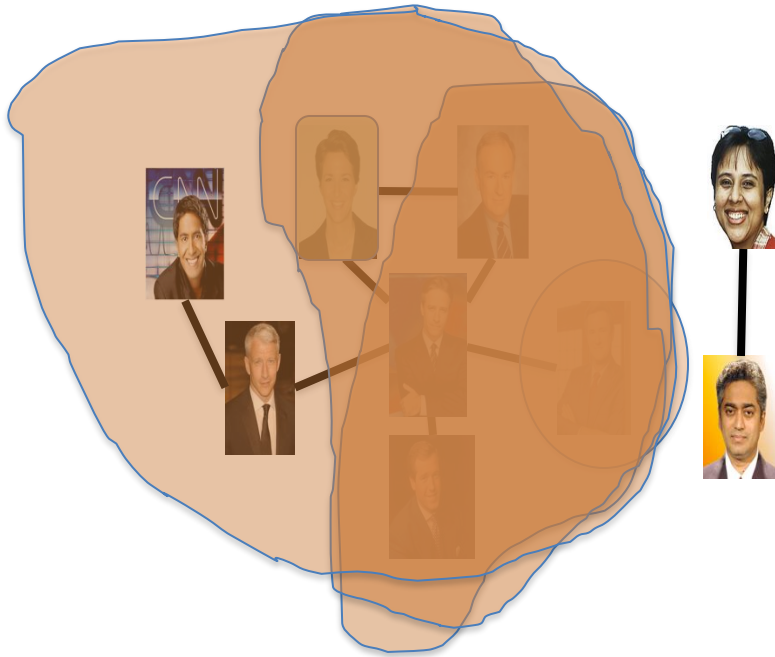
*Output:* All  $t$  connected to  $s$  in  $G$



Connected component  
of  $s$  also called  $CC(s)$



# Computing Connected Component



Explore( $s$ )

Start with  $R = \{s\}$

While exists  $(u,w)$  edge  $w$  not in  $R$  and  $u$  in  $R$

Add  $w$  to  $R$

Output  $R^* = R$

BFS (Build layers of vertices)

$L_0 = \{s\}$

Assume  $L_0, \dots, L_j$  have been constructed

$L_{j+1}$  set of vertices not chosen yet but are connected to  $L_j$

Stop when new layer is empty

# Explore is correct

Theorem:  $CC(s) = R^*$

Lemma 1:  $R^* \subseteq CC(s)$

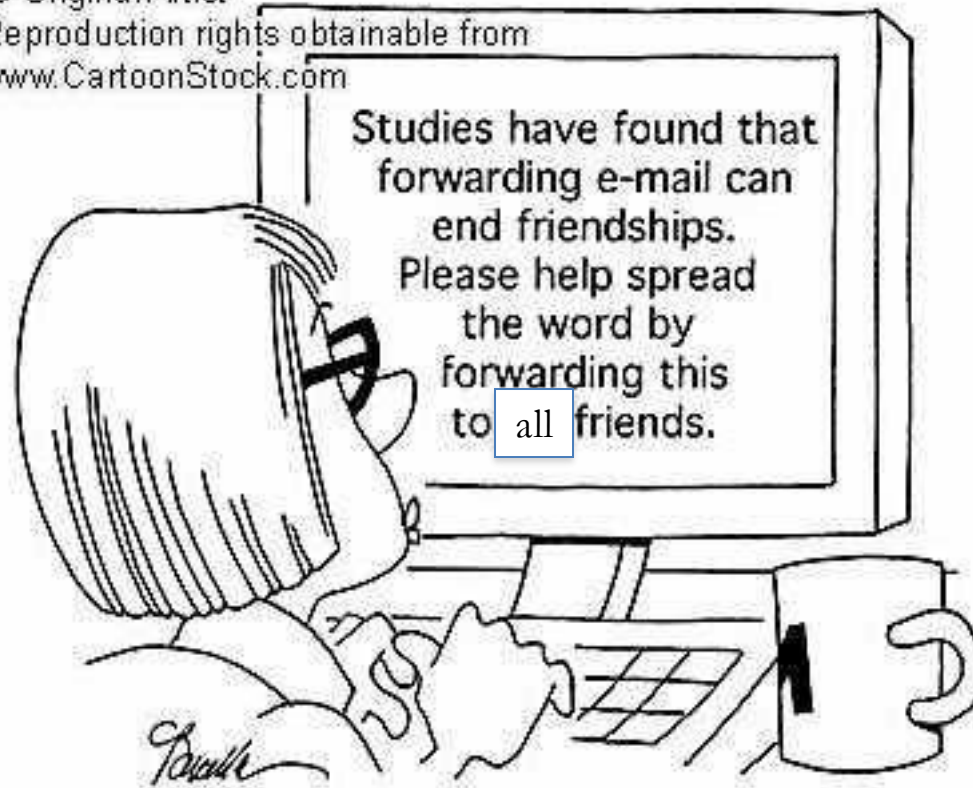
Lemma 2:  $CC(s) \subseteq R^*$

# Argue Lemma 2 on the board...



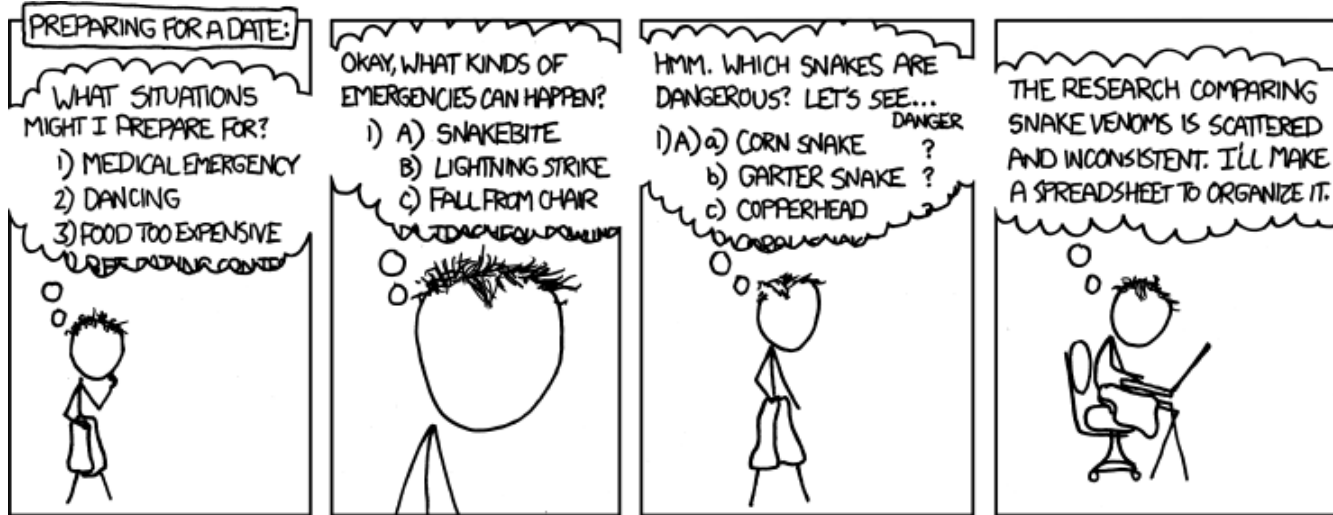
# BFS

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search ID: mbcn800

# Depth First Search (DFS)



<http://xkcd.com/761/>



I REALLY NEED TO STOP USING DEPTH-FIRST SEARCHES.

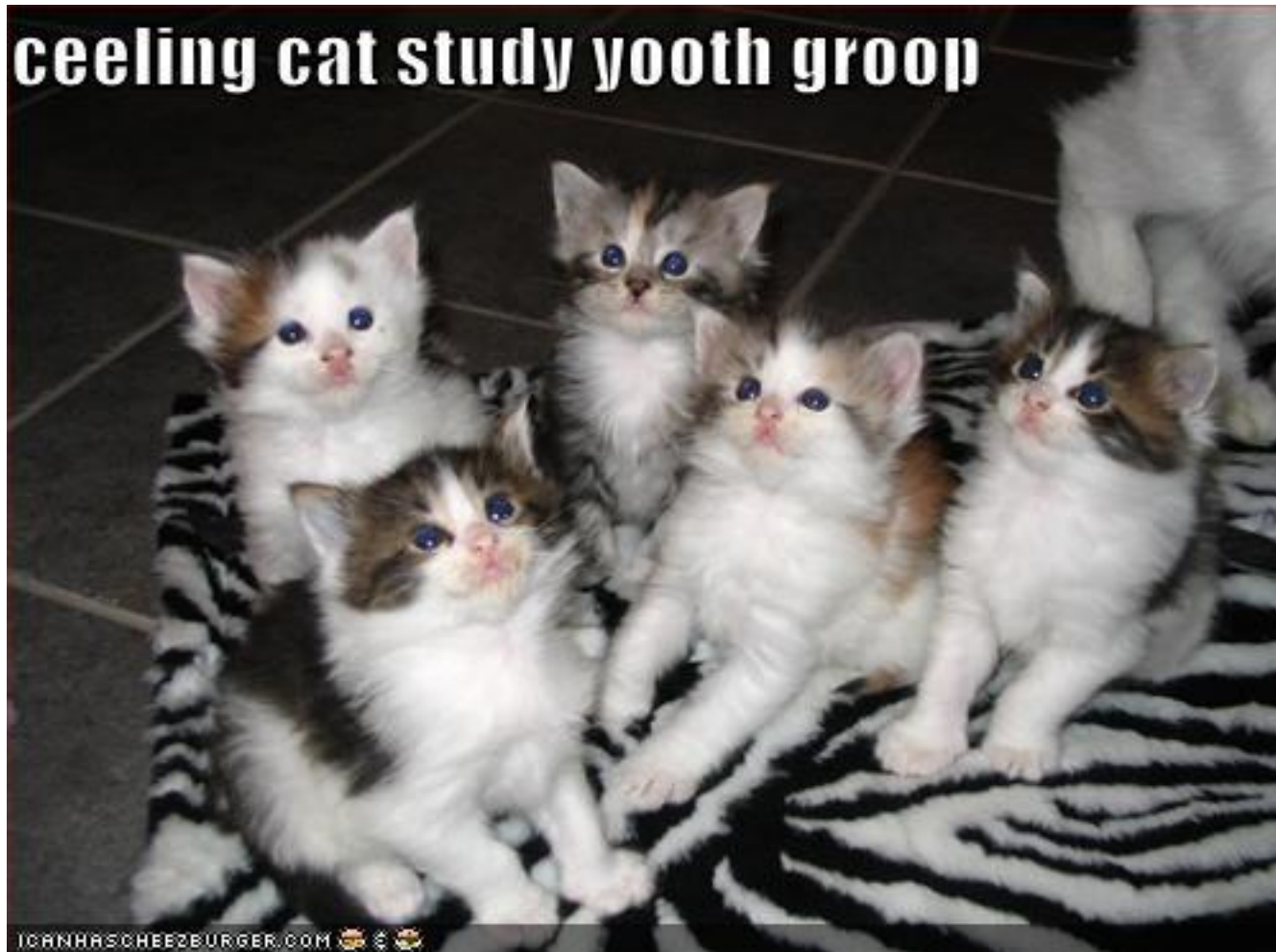
# DFS(**u**)

Mark **u** as explored and add **u** to **R**

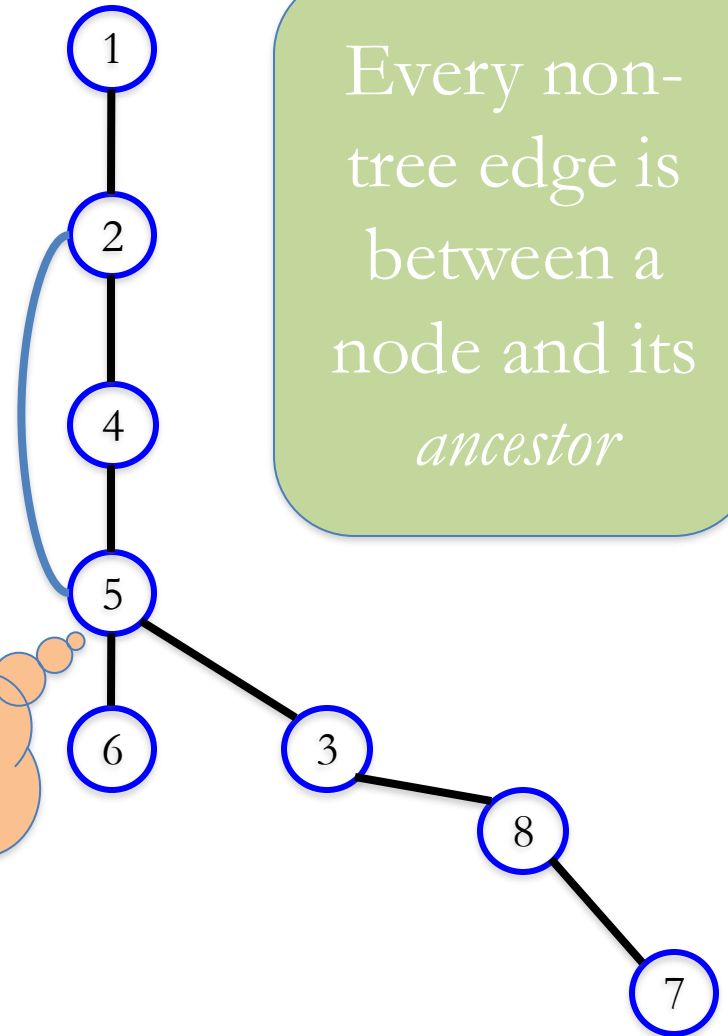
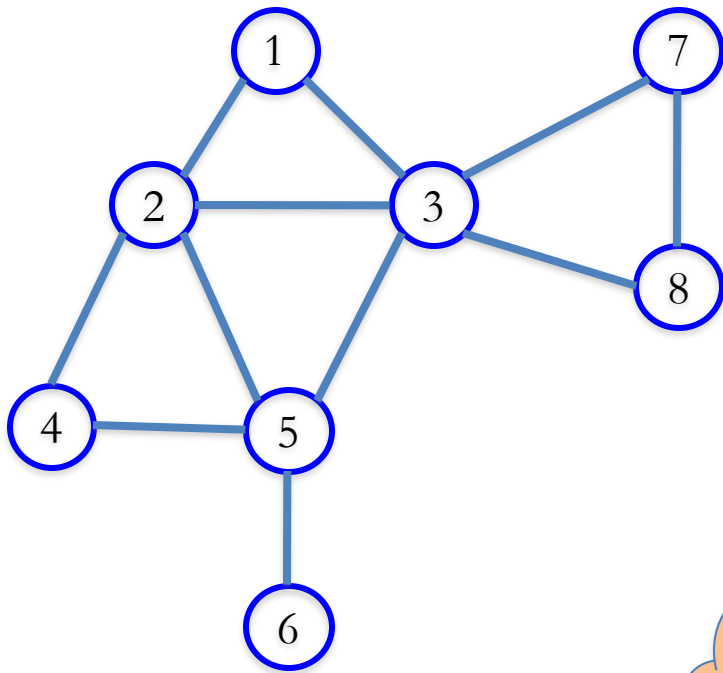
For each edge (**u,v**)

    If **v** is not explored then DFS(**v**)

# Why is DFS a special case of Explore?



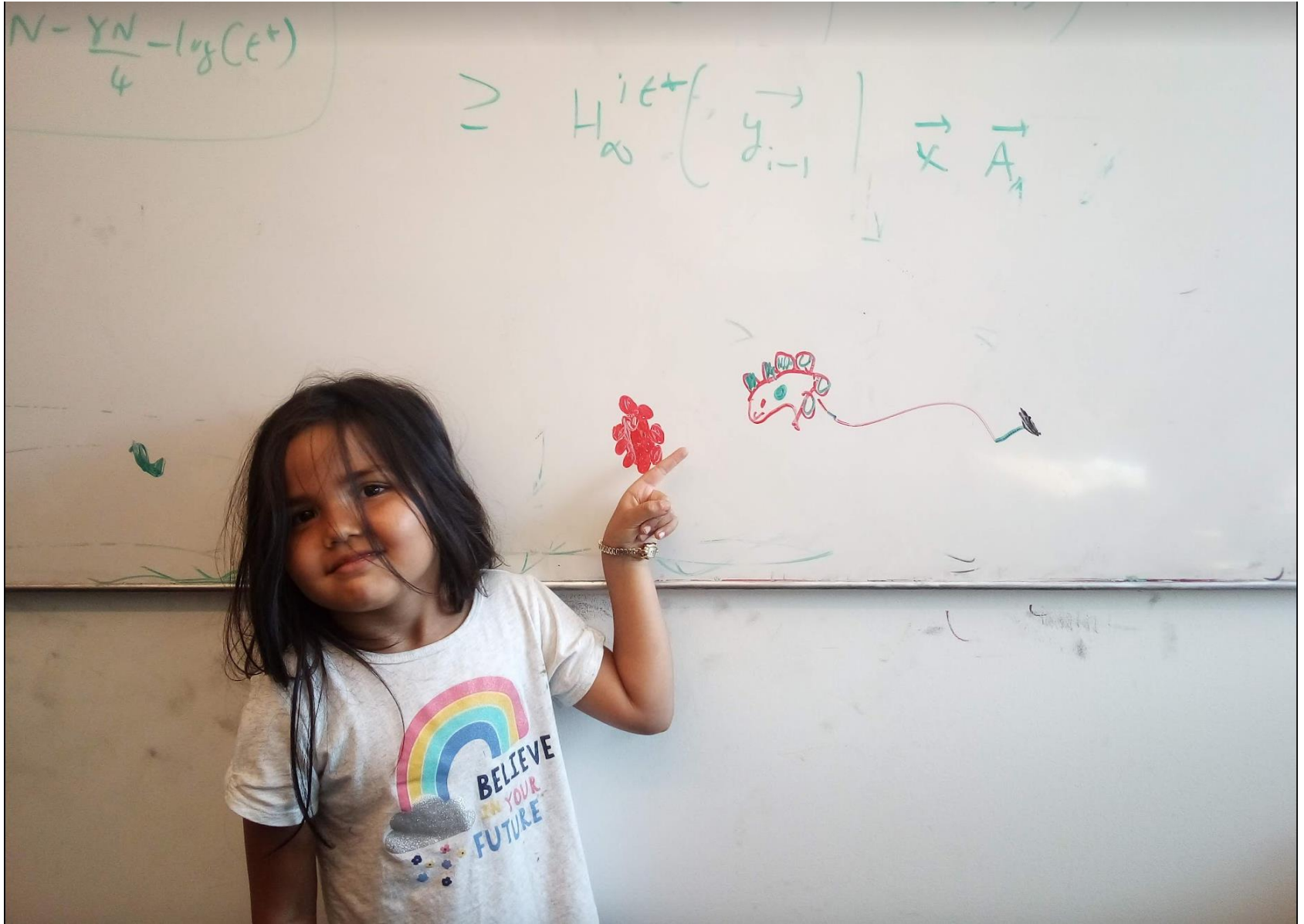
# A DFS run



Every non-tree edge is between a node and its *ancestor*

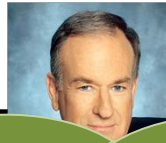


# Questions/Comments?



# Connected components are disjoint

Either connected components of  $s$  and  $t$  are the same or are disjoint

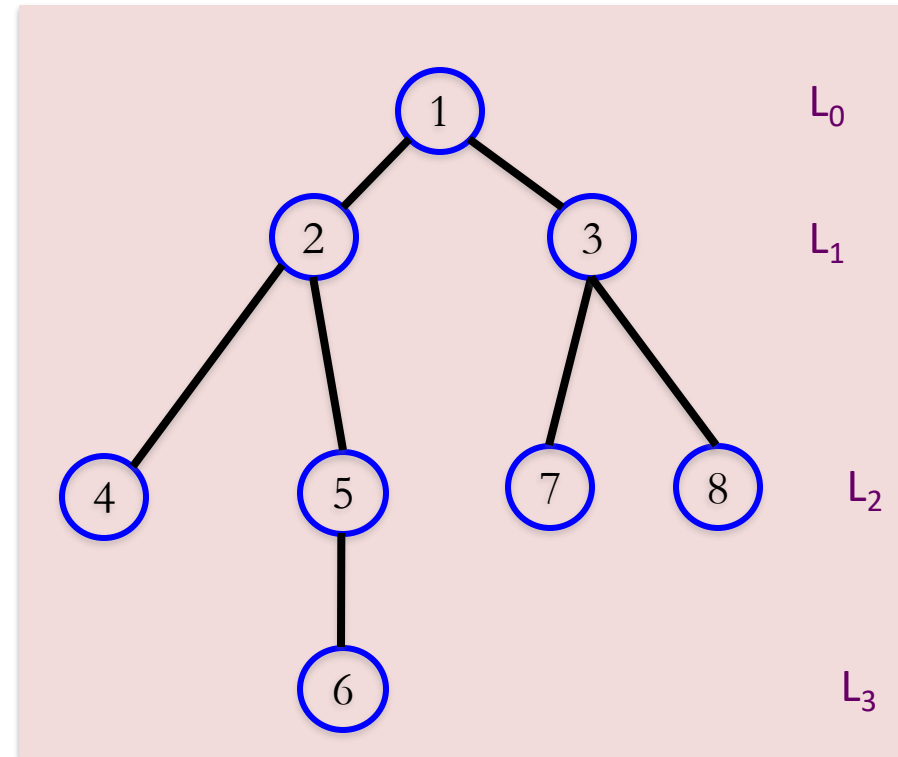
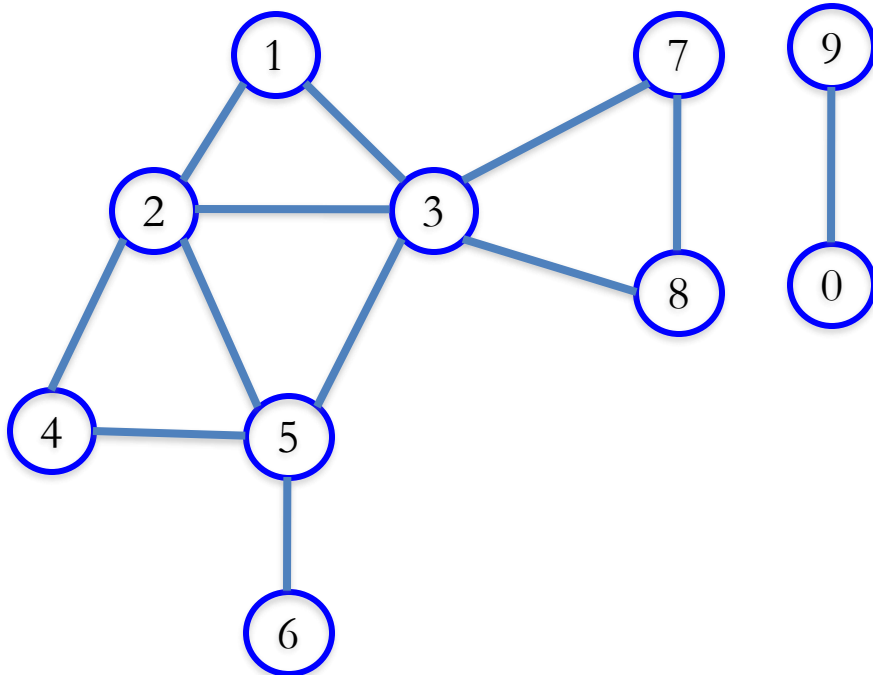
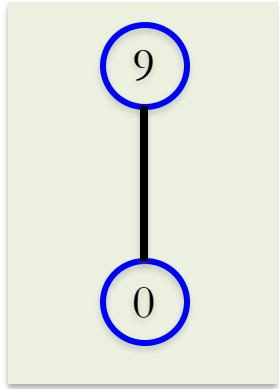


Algorithm to compute  
**ALL** the connected  
components?

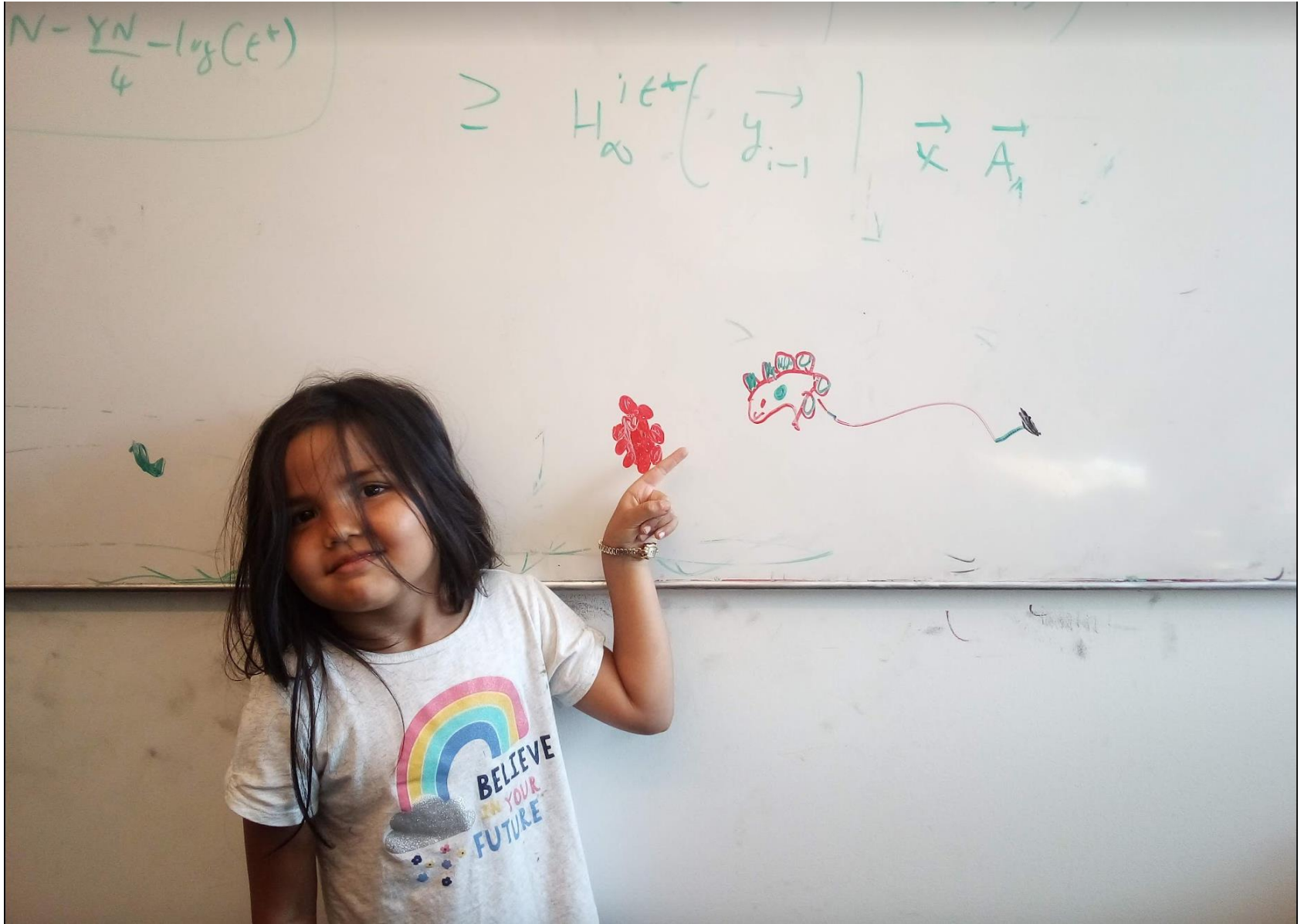
Can run Explore  
instead of BFS

Run BFS on some node  $s$ . Then run BFS on  $t$  that is not connected to  $s$

# Computing all CCs



# Questions/Comments?



# Rest of today's agenda

Run-time analysis of BFS (DFS)





# Stacks and Queues



Last in First out

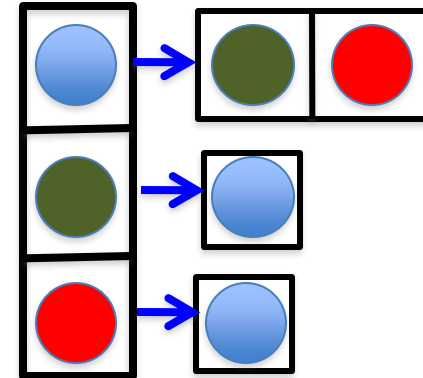
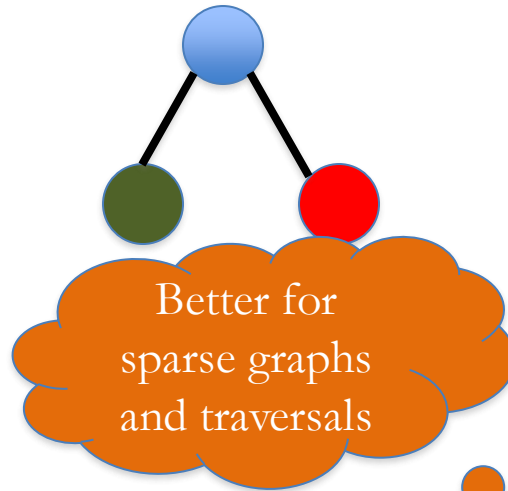
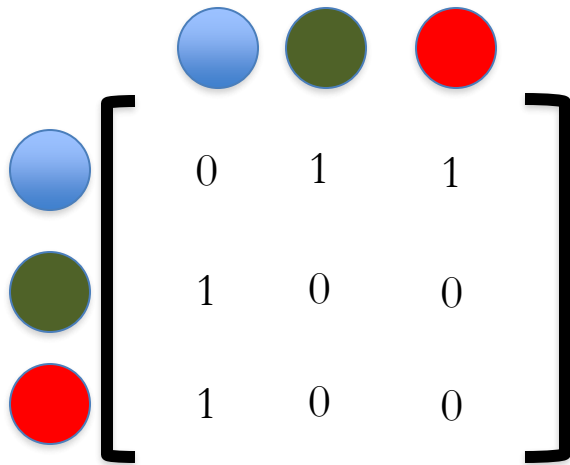


First in First out

# But first...

How do we represent graphs?

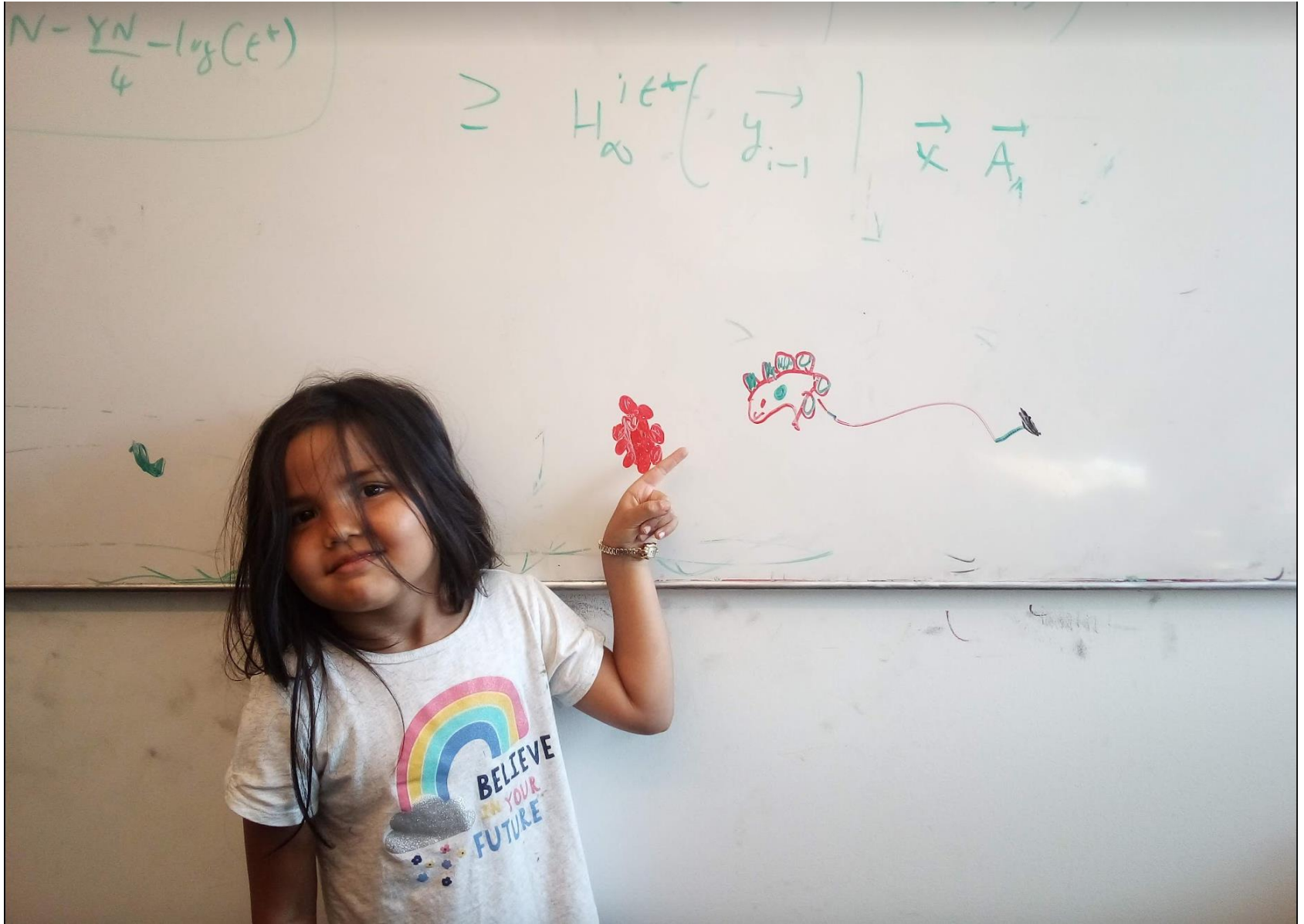
# Graph representations



Adjacency matrix		Adjacency List
$O(1)$	$(u,v) \in E?$	$O(n) [ O(n_v) ]$
$O(n)$	All neighbors of $u$ ?	$O(n_u)$
$O(n^2)$	Space?	$O(m+n)$



# Questions/Comments?

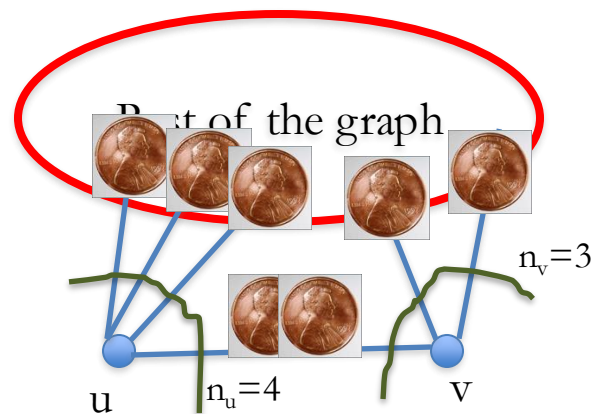


2 # edges = sum of # neighbors

$$2m = \sum_{u \text{ in } V} n_u$$

Give 2 pennies to each edge

Total # of pennies =  $2m$



Each edges gives one penny to its end points

# of pennies  $u$  receives =  $n_u$