

# Lecture 22

CSE 331

Oct 23, 2024

# UB Hacking!



@UBHacking @UBHacking @UBHacking

## UB HACKING

NOVEMBER 9TH & 10TH

Swag Networking Prizes Mentors

REGISTRATION OPEN NOW AT  
[UBHACKING.COM](http://UBHACKING.COM)

UB Hacking is University at Buffalo's student-run hackathon. Students from different backgrounds with any level of experience are welcome to join us as they build fun, innovative projects over 24 hours.

# Details on 1-on-1 meetings

note @217

stop following 3 views

Actions

## Meetings to discuss CSE 331 performance

By Sunday night, I will email those who have a D or below in their mid-term grade (for more details on the grade see @216) to setup a one-on-one meeting to talk with me but I figured I should post the information about meeting times now rather than later.

Of course you can also come and talk about your 331 performance even if you have a temp grade higher than D (though students with a D or below will get preference).

I have locked out certain times over next week or so for **15 mins** meetings. Please note that **these are NOT walk-ins**: if no one signs up for a slot, I will NOT be on zoom then. If you want to come and talk with me, **please EMAIL me with ALL the slots below that work for you**. (Private posts on piazza will not work: please email me!) *Slots will be assigned on a first-come-first-serve basis. Also I might only be able to confirm your time after 11pm on the day before your scheduled slot.*

**Note:** These are my current availabilities-- some of the slots might be used up in some other non-CSE 331 meetings. So please send multiple choices for when you can meet.

























































To make things easier, **ALL meeting will be on zoom** (<https://buffalo.zoom.us/j/95499374560?pwd=Srl2p86L6bl3PMI2uRtUjl1mplP6qM.1>)

Below are all the available slots (below the start times are listed: a slot that is already taken has a strike-through and italicized):

- **Tuesday (Oct 22):** 10:15am, 10:30am, 10:45am, 11:00am, 11:15am, 11:30am, 11:45am, 4:30pm, 4:45pm
- **Wednesday (Oct 23):** 12:45pm, 1:00pm, 1:15pm, 1:30pm, 1:45pm, 2:30pm, 2:45pm, 3:00pm, 3:15pm, 3:30pm, 3:45pm, 4:00pm, 4:15pm, 5:00pm, 5:15pm, 5:30pm, 5:45pm, 6:00pm, 6:15pm, 7:45pm, 8:00pm, 8:15pm, 8:30pm
- **Thursday (Oct 24):** 9:00am, 9:15am, 9:30am, 9:45am, 10:00am, 10:15am, 10:30am, 10:45am, 11:00am, 11:15am, 11:30am, 11:45am, 12:30pm, 12:45pm
- **Friday (Oct 25):** 9:00am, 9:15am, 9:30am, 9:45am, 12:30pm, 2:00pm, 2:15pm, 2:30pm, 2:45pm
- **Monday (Oct 28):** 12:30pm, 2:30pm, 2:45pm, 3:00pm, 3:15pm, 3:30pm, 3:45pm, 4:30pm, 4:45pm, 5:00pm, 5:15pm, 5:30pm, 5:45pm, 6:30pm, 6:45pm, 7:00pm, 7:15pm, 7:30pm, 7:45pm, 8:00pm, 8:15pm, 8:30pm

(If none of the times above work for you but you still want to meet, please email me and we can try and set up a time for the week of Oct 28.)

# Project deadlines coming up

Tue, Oct 15		(HW 4 out)
Wed, Oct 16	Dijkstra's algorithm     F24  F23  F22  F21  F19 $\times^2$	[KT, Sec 4.4] <a href="#">Week 8 recitation notes</a>
Fri, Oct 18	Correctness of Dijkstra's Algorithm  F23  F22  F21  F19  F18  F17 $\times^2$	[KT, Sec 4.4] <i>Reading Assignment:</i> [KT, Sec 4.4]
Mon, Oct 21	Minimum Spanning Tree  F23  F22  F21  F19  F18  F17 $\times^2$	[KT, Sec 4.5]
Tue, Oct 22		(HW 4 in, HW 5 out)
Wed, Oct 23	Cut Property Lemma  F23  F22  F21  F19  F18  F17 $\times^2$	[KT, Sec 4.5] <i>Reading Assignment:</i> [KT, Sec 4.5, 4.6]
Fri, Oct 25	Mergesort  F23  F22  F21  F19  F18  F17 $\times^2$	[KT, Sec 5.1]
Mon, Oct 28	Solving recurrence relations  F23  F22  F21  F19  F18  F17 $\times^2$	[KT, Sec 5.1]
Tue, Oct 29		(HW 5 in)
Wed, Oct 30	Counting Inversions  F23  F22  F21  F19  F18  F17 $\times^2$	[KT, Sec 5.3]
Fri, Nov 1	Multiplying large integers  F23  F22  F21  F19  F18  F17 $\times^2$	[KT, Sec 5.5] (Project (Problems 1 & 2 <b>Coding</b> ) in) <i>Reading Assignment:</i> <a href="#">Unraveling the mystery behind the identity</a>
Mon, Nov 4	Closest Pair of Points  F23  F22  F21  F19  F18  F17 $\times^2$	[KT, Sec 5.4] (Project (Problems 1 & 2 <b>Reflection</b> ) in)

# HW 5 out

## Homework 5

Due by **11:30pm, Tuesday, October 29, 2024.**

Make sure you follow all the [homework policies](#).

All submissions should be done via [Autolab](#).

Check the [week 9 recitation notes](#) for this homework.

## Question 1 (Computing Set Intersection on a Network) [50 points]

### The Problem

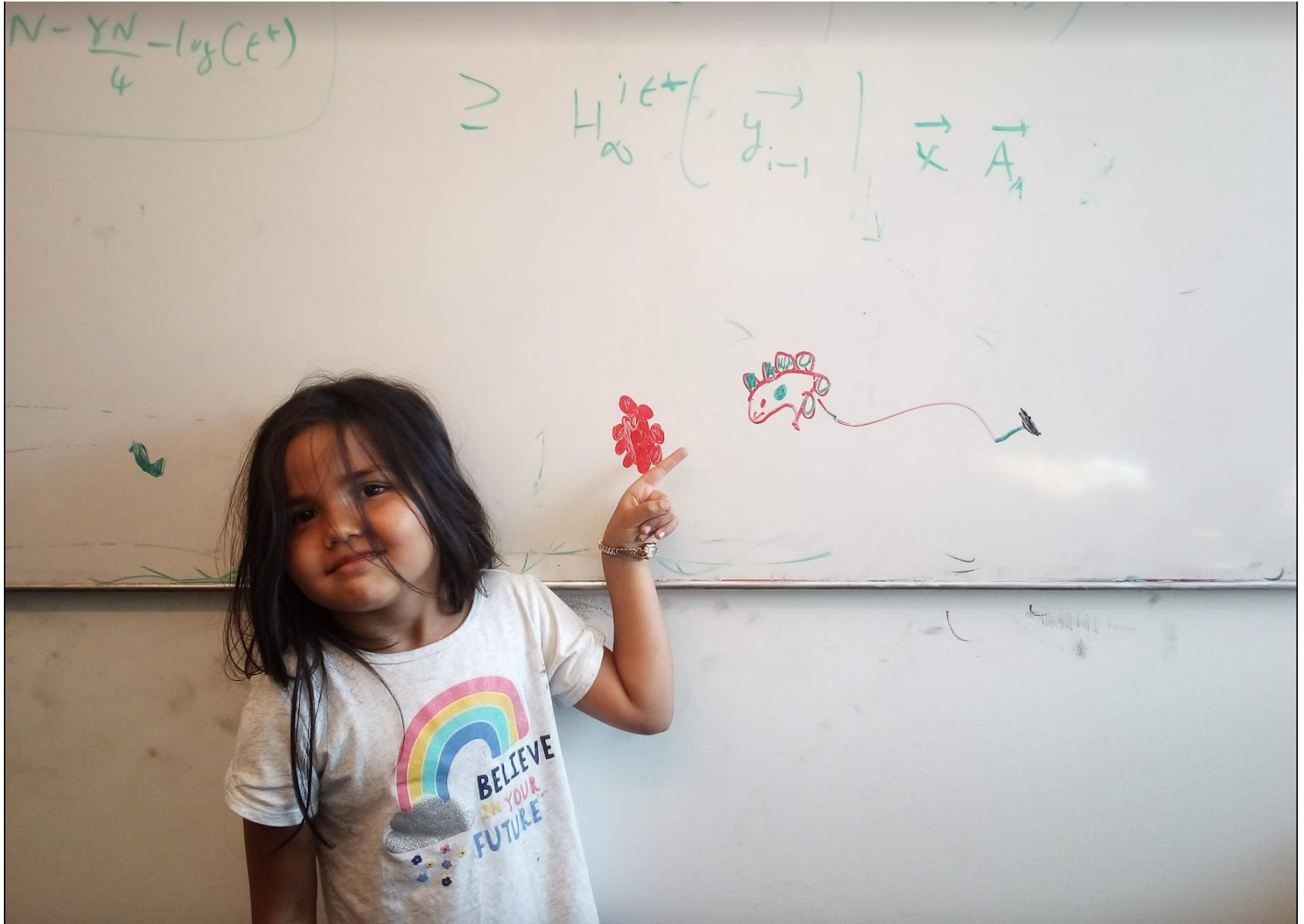
In this problem, we will take a break from trying to minimize the runtime of the algorithm and focus on an important resource in distributed computing: the total number of bits communicated over a network by the algorithm.

Given a graph  $G = (V, E)$ , which is the underlying *network topology*, we want to compute the intersection of  $n = |V|$  sets over the network  $G$ . More precisely, every node  $u \in V$ , gets a set  $S_u \subseteq [M]$  for some integer  $M \geq 1$ . (Note that  $M$  has *nothing* to do with the number of edges in  $G$ .) Further we are given a special node  $t \in V$ . The goal of this problem is to design an algorithm such that when the algorithm terminates, the node  $t$  knows the intersection of all sets:

$$\bigcap_{u \in V} S_u.$$

Moreover, we want to design such an algorithm that minimizes the total communication over  $G$ .

# Questions/Comments?



# Minimum Spanning Tree Problem

**Input:** Undirected, connected  $G = (V, E)$ , edge costs  $c_e$

**Output:** Subset  $E' \subseteq E$ , s.t.  $T = (V, E')$  is connected  
 $C(T)$  is minimized

If all  $c_e > 0$ , then  $T$  is indeed a tree



# Kruskal's Algorithm

Input:  $G=(V,E)$ ,  $c_e > 0$  for every  $e$  in  $E$

$T = \emptyset$

Sort edges in increasing order of their cost

Consider edges in sorted order

If an edge can be added to  $T$  without adding a cycle then add it to  $T$



Joseph B. Kruskal



# Prim's algorithm

Similar to Dijkstra's algorithm



Robert Prim

Input:  $G=(V,E)$ ,  $c_e > 0$  for every  $e$  in  $E$

$S = \{s\}$ ,  $T = \emptyset$

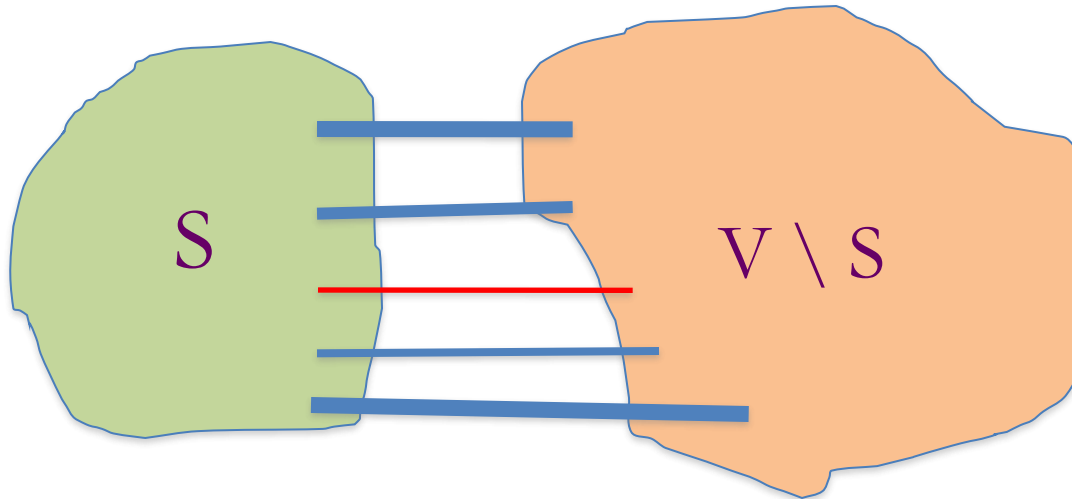
While  $S$  is not the same as  $V$

Among edges  $e = (u,w)$  with  $u$  in  $S$  and  $w$  not in  $S$ , pick one with minimum cost

Add  $w$  to  $S$ ,  $e$  to  $T$

# Cut Property Lemma for MSTs

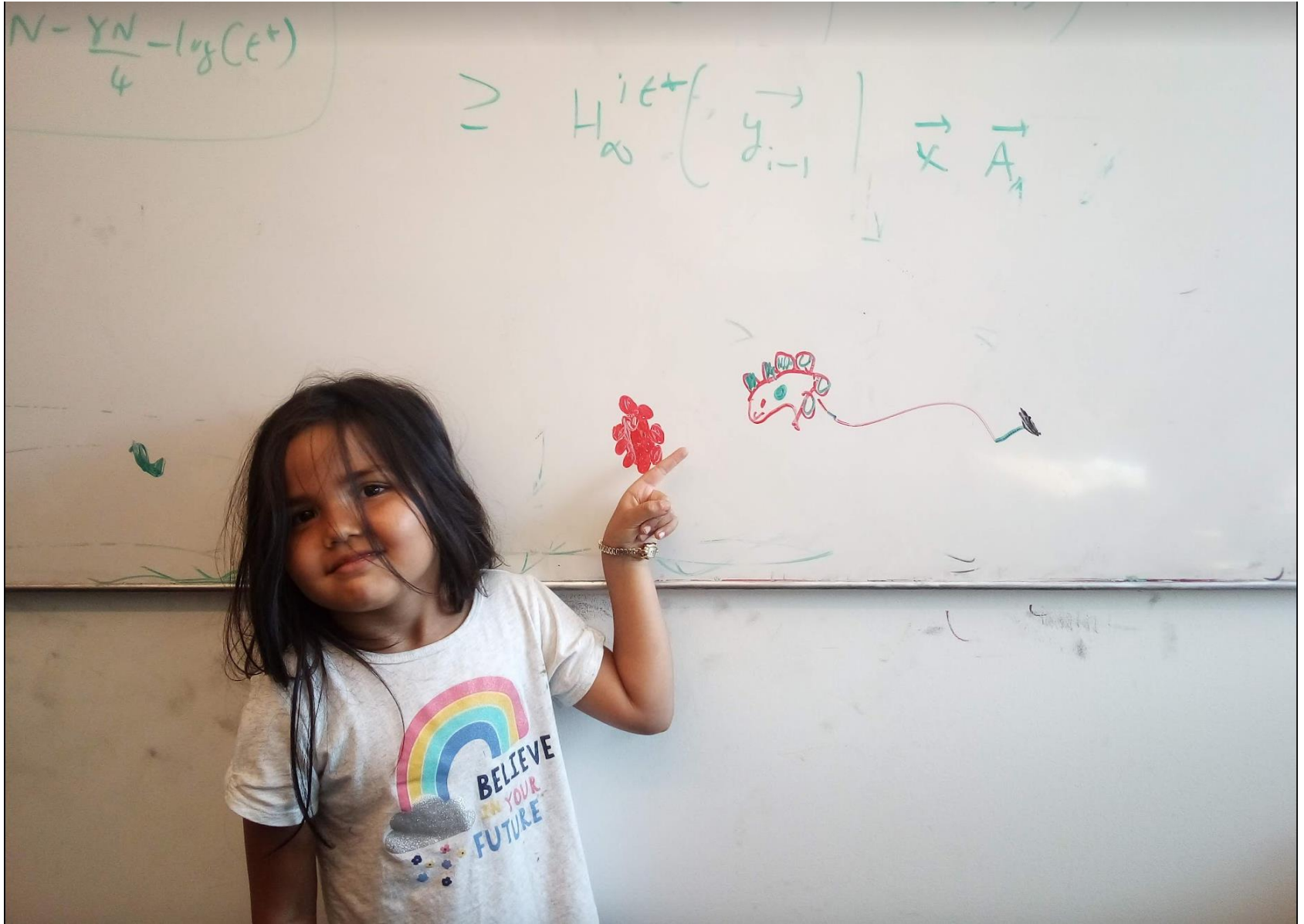
Condition:  $S$  and  $V \setminus S$  are non-empty



Cheapest crossing edge is in **all** MSTs

Assumption: All edge costs are distinct

# Questions/Comments?



# Today's agenda

Optimality of Prim's algorithm

Prove Cut Property Lemma

Optimality of Kruskal's algorithm

Remove distinct edge weights assumption

# On to the board...

