

# Lecture 30

CSE 331

Nov 11, 2024

# Final exam conflict

note @274

stop following **0 views**

Actions

## Final exam conflicts

I know some of you have an exam conflict with CSE 331 final exam. Since I'm not sure if I know the exact set of students with conflict, I figured I'll do a piazza post.

**If you have an exam conflict with the CSE 331 final please EMAIL me by 5pm on Friday, Nov 15.** If you email me after this deadline, I cannot promise to be able to give you a makeup option that works with your schedule.

Please note that the makeup final will be on *Monday, Dec 16* (i.e. a day before the scheduled final exam). My goal is to pick a time that works for everyone on Dec 16.

*So if you email me for a makeup final exam, please send me all the time(s) that you do a makeup on Monday, Dec 16 between 9am-5pm.*

final

Edit good note | 0

Updated 41 seconds ago by Atri Rudra

# Reflections 2+1 grading timeline

note @281

stop following **11 views**

Actions

## Timeline on project reflections grading

As a heads up, I'll be manually grading all the reflections 1+2 grading so it'll take a bit of time. Since reflection 2 in structure is closer to reflections 3-5, I'll grade reflection 2 first and then reflection 1. My hope is to get reflection 2 graded within 2 weeks.

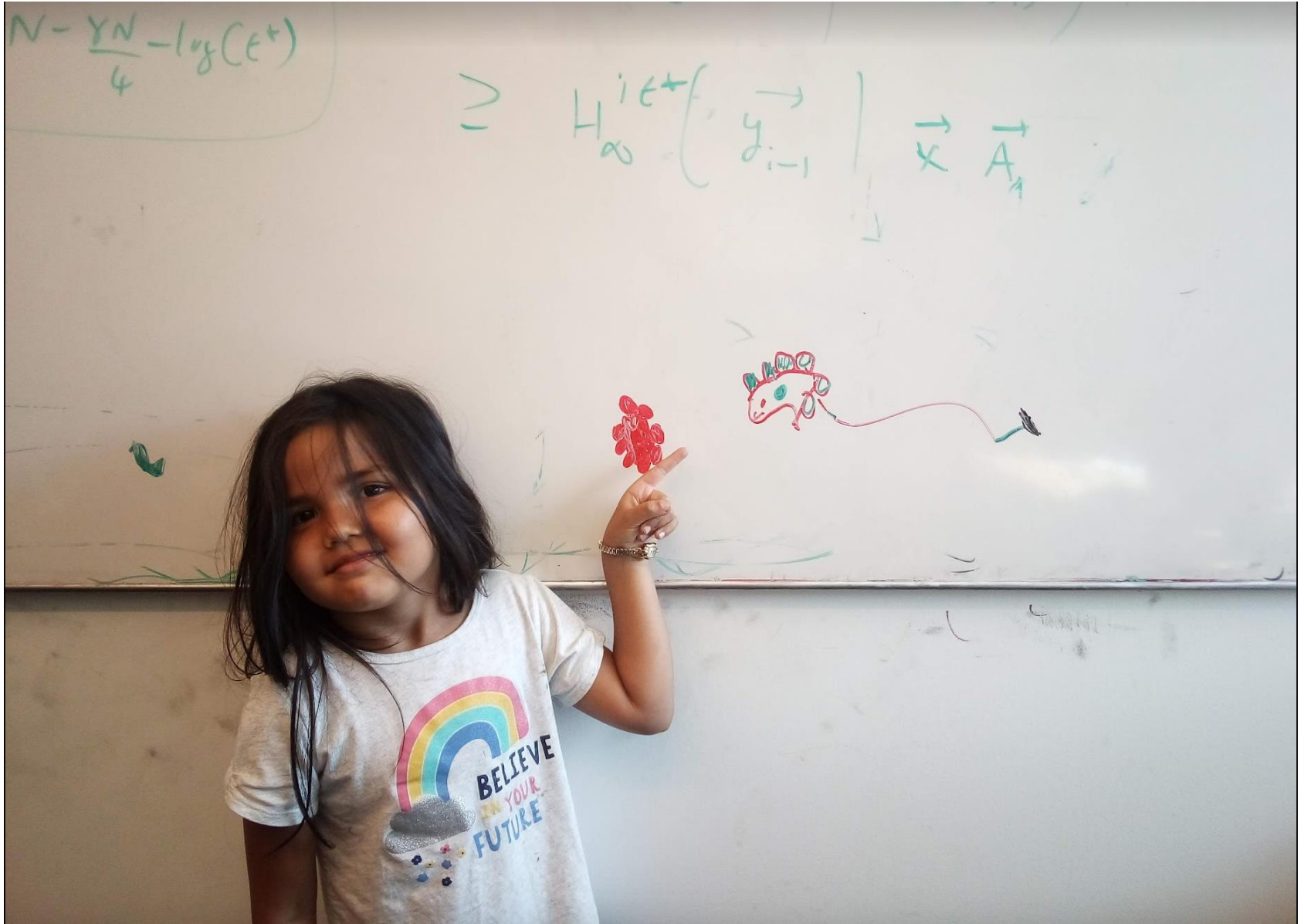
Figured should y'all a heads up as y'all work on the rest of the project.

project

Edit good note | 0

Updated 8 minutes ago by Atri Rudra

# Questions/Comments?



# End of Semester blues

Can only do one thing at any day: what is the optimal schedule to obtain maximum value?



Write up a term paper (10)

Party! (2)

Exam study (5)

331 HW (3)

Project (30)

Friday

Saturday

Sunday

Monday

Tuesday

# Previous Greedy algorithm

Order by end time and pick jobs greedily

Greedy value =  $5+2+3=10$



Write up a term paper (10)

Party! (2)

Exam study (5)

331 HW (3)

Project (30)

OPT = 30

Friday

Saturday

Sunday

Monday

Tuesday

# Weighted Interval Scheduling

Input:  $n$  jobs  $(s_i, f_i, v_i)$

Output: A schedule  $S$  s.t. no two jobs in  $S$  have a conflict

Goal:  $\max \sum_{i \in S} v_j$

Assume: jobs are sorted by their finish time

# Today's agenda

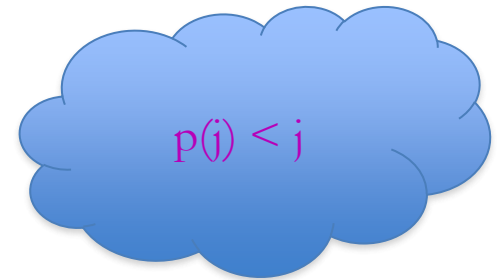
Finish designing a recursive algorithm for the problem





# Couple more definitions

$p(j)$  = largest  $i < j$  s.t.  $i$  does not conflict with  $j$   
= 0 if no such  $i$  exists



$OPT(j)$  = optimal value on instance  $1, \dots, j$

# Moving to the board...



# Property of OPT

$j$  in  $\text{OPT}(j)$

$j$  not in  $\text{OPT}(j)$

$$\text{OPT}(j) = \max \{ v_j + \text{OPT}(p(j)), \text{OPT}(j-1) \}$$

Given  $\text{OPT}(1), \dots, \text{OPT}(j-1)$ ,  
how can one figure out if  $j$  in  
optimal solution or not?



ICANHASCHEEZBURGER.COM 🍷 🍷

# A recursive algorithm

Compute-Opt( $j$ )

Correct for  $j=0$

Proof of correctness by induction on  $j$

If  $j = 0$  then return 0

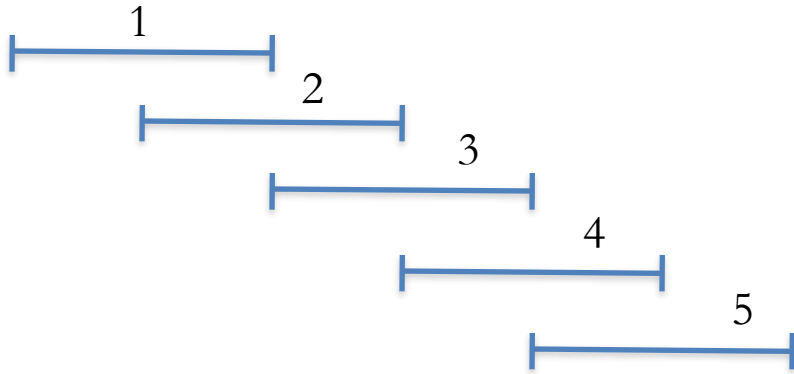
return max {  $v_j + \text{Compute-Opt}(p(j))$ ,  $\text{Compute-Opt}(j-1)$  }

= OPT( $p(j)$ )

= OPT( $j-1$ )

$$\text{OPT}(j) = \max \{ v_j + \text{OPT}(p(j)), \text{OPT}(j-1) \}$$

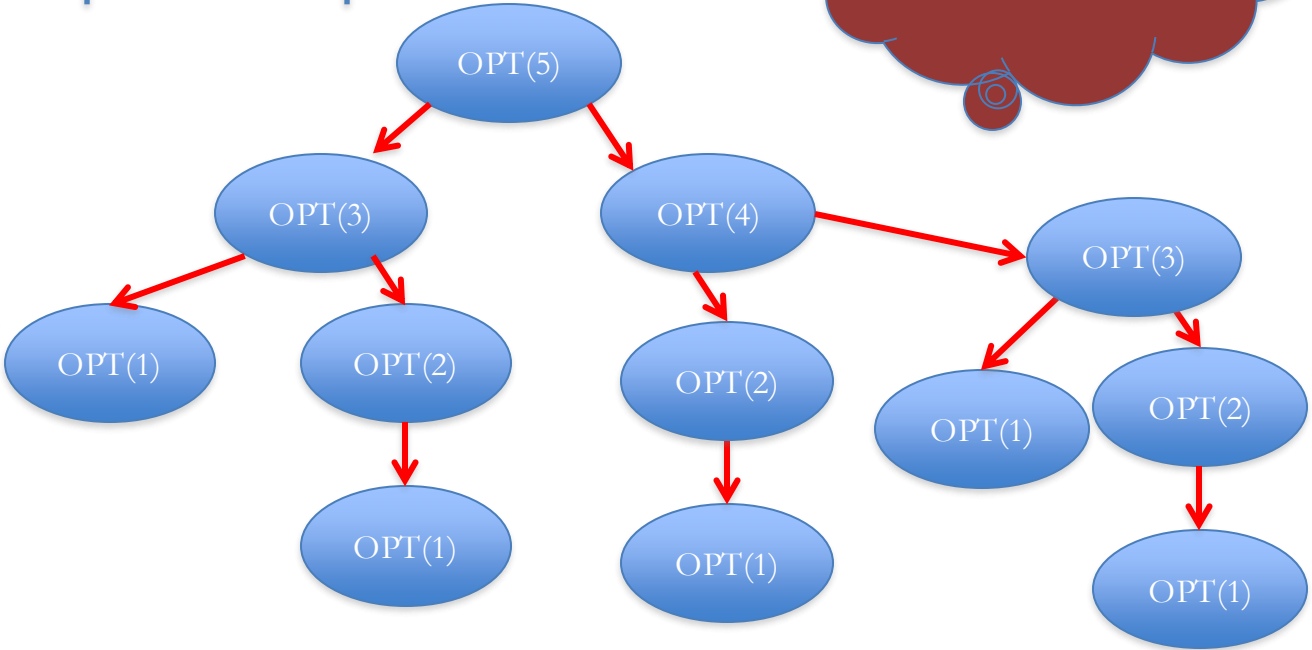
# Exponential Running Time



$$p(j) = j-2$$

Only 5 OPT values!

Formal proof: Ex.





# Using Memory to be smarter

Using more space can reduce runtime!



How many distinct OPT values?

# A recursive algorithm

M-Compute-Opt(j)

If  $j = 0$  then return 0

If  $M[j]$  is not null then return  $M[j]$

$M[j] = \max \{ v_j + \text{M-Compute-Opt}(p(j)), \text{M-Compute-Opt}(j-1) \}$

return  $M[j]$

M-Compute-Opt(j)  
= OPT(j)

Run time =  $O(\# \text{ recursive calls})$