

**Topics for mid-term exam: You will have 6 questions covering these topics: closed book**

Topic	Section	material
Number system	1.1-1.6, Hwk1	Radix conversion; 2's complement & signed arithmetic
Boolean algebra	2.4-2.8, Hwk2	Sum of products; Simplify the function to minimum number of literals
Complete problem statement to gate implementation	Hwk4	Implementation of logic expression using NAND gates
Karnaugh maps	3.2-3.6 Up to p.94 Hwk3	3 and 4 variable maps, don't cares (x's)
MSI circuits; Combinational circuit building blocks	4.1-4.3; 4.9, 4.11; Hwk5	Multiplexers and decoders: block diagram; implementation of combinational circuits using MUX and Decoders

**Sample questions:****1. (4 X 5 = 20 points) Number system and Radix Conversion**

For the numbers given below convert the radix as specified.

- 1234 decimal to binary  $(1234)_{10} \rightarrow ( ? )_2$
- 1011.11 to decimal  $(1011.11)_2 \rightarrow ( ? )_{10}$
- 1011.11 to octal  $(1011.11)_2 \rightarrow ( ? )_8$
- 1011.11 to hexadecimal  $(1011.11)_2 \rightarrow ( ? )_{16}$

**2. (20 points) Boolean Algebraic Simplification**

Simplify using only Boolean algebraic laws and theorems. Clearly show all the intermediate steps. Provide the result in sum of products form.

$$F(A, B, C) = A.B.C + A'.B.C + A'.B.C' + A.B'.C + A.C'$$

**3. (4 + 2 + 9 + 5 = 20 points) Word Problem to Gate implementation**

Consider a 4-input (**W, X, Y, Z**) and 1-output function that has logic-1 output whenever the majority of the inputs are logic-0.

- Draw the truth table representing this function.
- Express the function in sum of minterms format.
- Simply the expression from above using algebraic simplification method.
- Draw the combinational circuit for the simplified expression.

**4. (10 + 10 = 20 points) NAND only implementations**

Draw the **NAND only** implementations for the Boolean expression given below:

$$F(A, B, C, D) = A.B + B'.C' + B.(C'+D)$$

**5. (20 points) Signed Binary Arithmetic**

Consider 8-bit binary containers with 1 bit for sign and 7 bits for magnitude. Consider numbers  $A = 65$  and  $B = 72$ . Assume negative numbers are represented as 2's complement and the operations are in 2's complement. Perform the operations below in binary. **Specify if the result is positive, negative or overflow and explain your answer.**

- $X = A + B$
- $Y = A - B$
- $Z = -A - B$
- $W = -A + B$

**6. (20 points) MSI Circuits**

Obtain a 4X16 decoder using 2 3X8 decoders. Implement  $\Sigma(2,5,6,8,11)$  using (i) 4X16 decoder and (ii) 16X1 MUX.