

CSE241

Feb 20, 2017

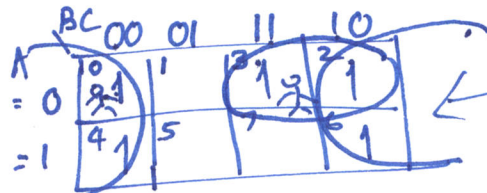
Midterm Exam: 3/13/2017

Lecture recordings are available on Ulearn.

~~Lab 4~~  
Please demo Lab 1 to TAs in recitation to get your grade: Deadline: 3/3/2017 (However demo it before the deadline)

1.  $f(A, B, C) = \sum (0, 2, 3, 4, 6)$   
Simplify to minimum number of terms and min number of literals.

step 1: draw empty K-map  
3-variable map



- step 2: ~~step 2~~. Label the map
- step 3: fill-in the minterms of the problem to be minimized
- step 4: Cover the 1's with (i) minimal # of groups  
"rectangular adjacent"  
(ii) as large a group as possible

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group of 4 1's using wrap-around

Have I covered all the 1's? No

~~#~~  
Is there a group of 2 1's? Yes  
with overlap ...

steps: ~~#~~ 1 group of 4 1's  
1 group of 2 1's  
write the terms for these groups

group 1 ~~term~~  $\rightarrow C'$

A changes, B changes  
and  $c = 0$  for all 1's  
in the group

group 2  $\rightarrow A'B$

$A = 0$   $B = 1$

C changes

simplified ~~for~~ expression is

$$f(A, B, C) = C' + A'B$$

we started with 5 terms, 3 literals each

$$5 \times 3 = 15$$

we simplified it to 2 terms of 3 literals

15	$\rightarrow$	3
5	$\rightarrow$	2

4 - variable problem.

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$$f(w, x, y, z) = \sum (0, 1, 2, 3, 4, 6, 8, 12)$$

	yz=00	01	11	10
wx=00	0 1	1 1	3 1	2 1
= 01	4 1	5	7	6 1
= 11	12 1	13	15	14
= 10	8 1	9	11	10

Is there a group of 16 1's? No

Is there a group of 8 1's? rectangular adjacent No

Is there a group of 4 1's?

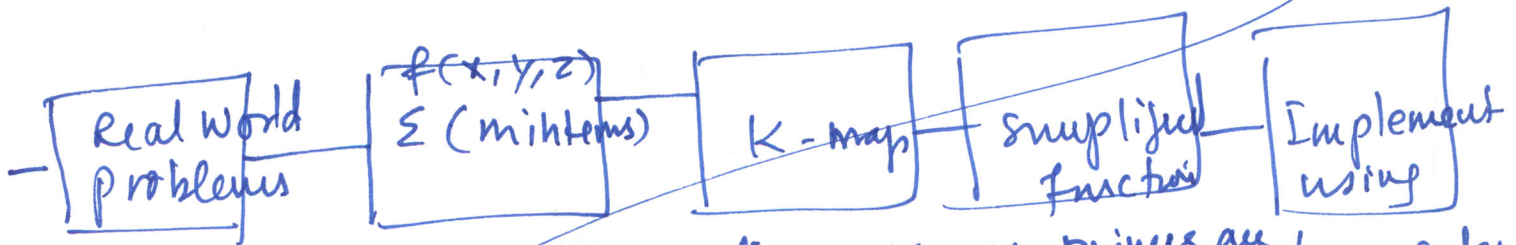
all 1's — covered. 3 groups of 4 1's

group 1:  $y=0 \ z=0$  are constant/common  
 $y'z'$

group 2:  $w=0 \ x=0$  are constant/  
 $w'x'$

group 3:  $w=0 \ z=0$  are constant/  
 $w'z'$

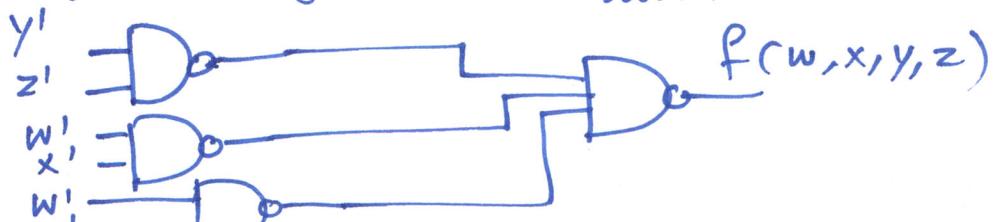
Simplified:  $f(w, x, y, z) = \underline{y'z' + w'x' + w'z'}$



Ex:

7-Segment LED Driver

NAND gates. assume primes are available.



3.  $f(w, x, y, z) = \sum (0, 2, 8, 10)$  Feb 20, 2017

	$yz$	00	01	11	10
$wx$	00	0 1	1	3	2 1
	01	4	5	7	6
	11	12	13	15	14
	10	8 1	9	11	10 1

$$f(w, x, y, z) = \underline{x'z}$$

$f = 0$

$$(f \cdot 1)' = f + 0 = f$$



4.

	$yz$	00	01	11	10
$wx$	00	0	1	3	2 1
	01	4	5 1	7 1	6
	11	12 1	13 1	15 1	14
	10	8	9	11	10

$$f(w, x, y, z) = \sum (2, 5, 7, 13, 15, 12)$$

Don't forget singletons.

$$f(w, x, y, z) = \underline{xz + wx'y' + w'x'y'z'}$$