

# What we (and our students) can learn from radio-controlled flight?

Dr. John Cerne

Physics Department  
University at Buffalo



Interdisciplinary Science and Engineering Partnership  
and Division of Materials Research



**radio-controlled**

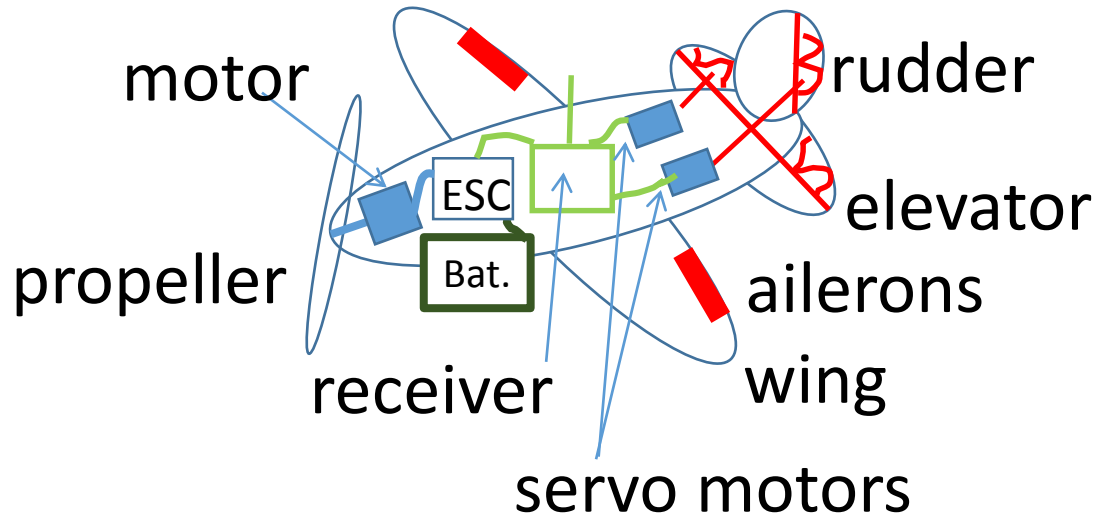
Radio waves, polarization, signal, AM/FM, digital...



**Flight**

Forces, work, power, electric motors, energy storage...

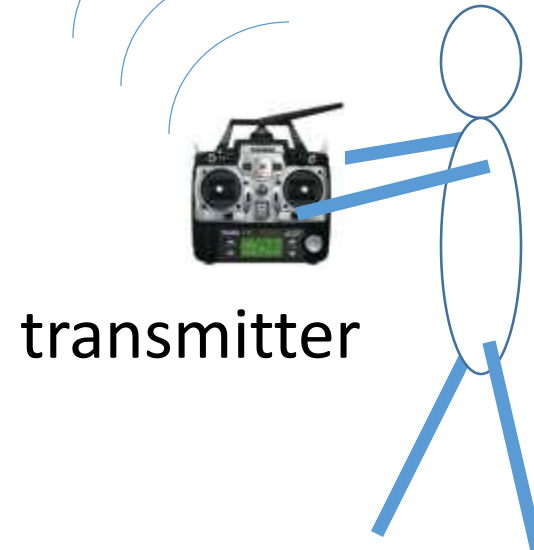
# What is a radio controlled (RC) airplane?



How does a plane gain altitude?

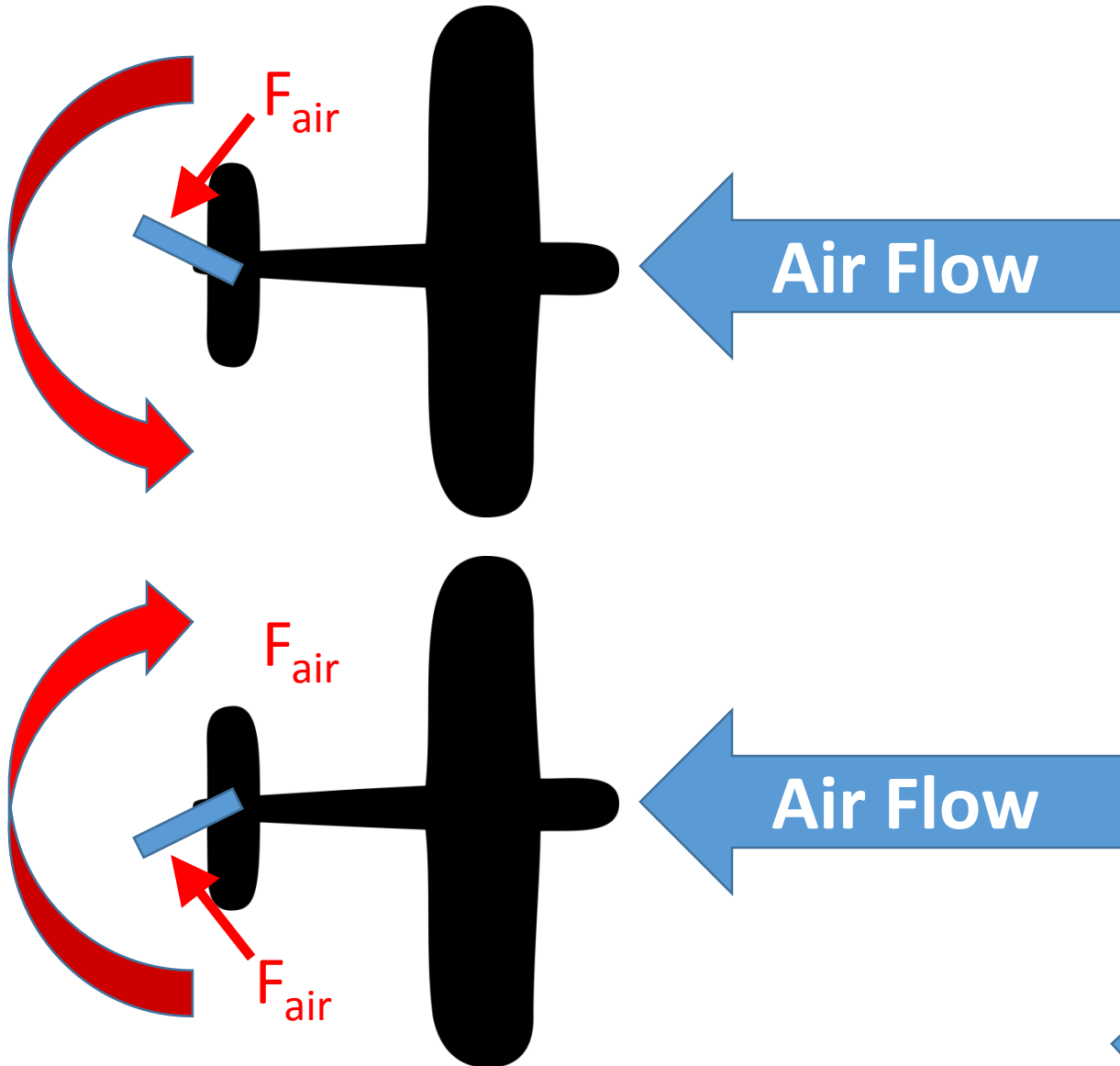
radio waves

Demo 1: Using a radio to move control surfaces

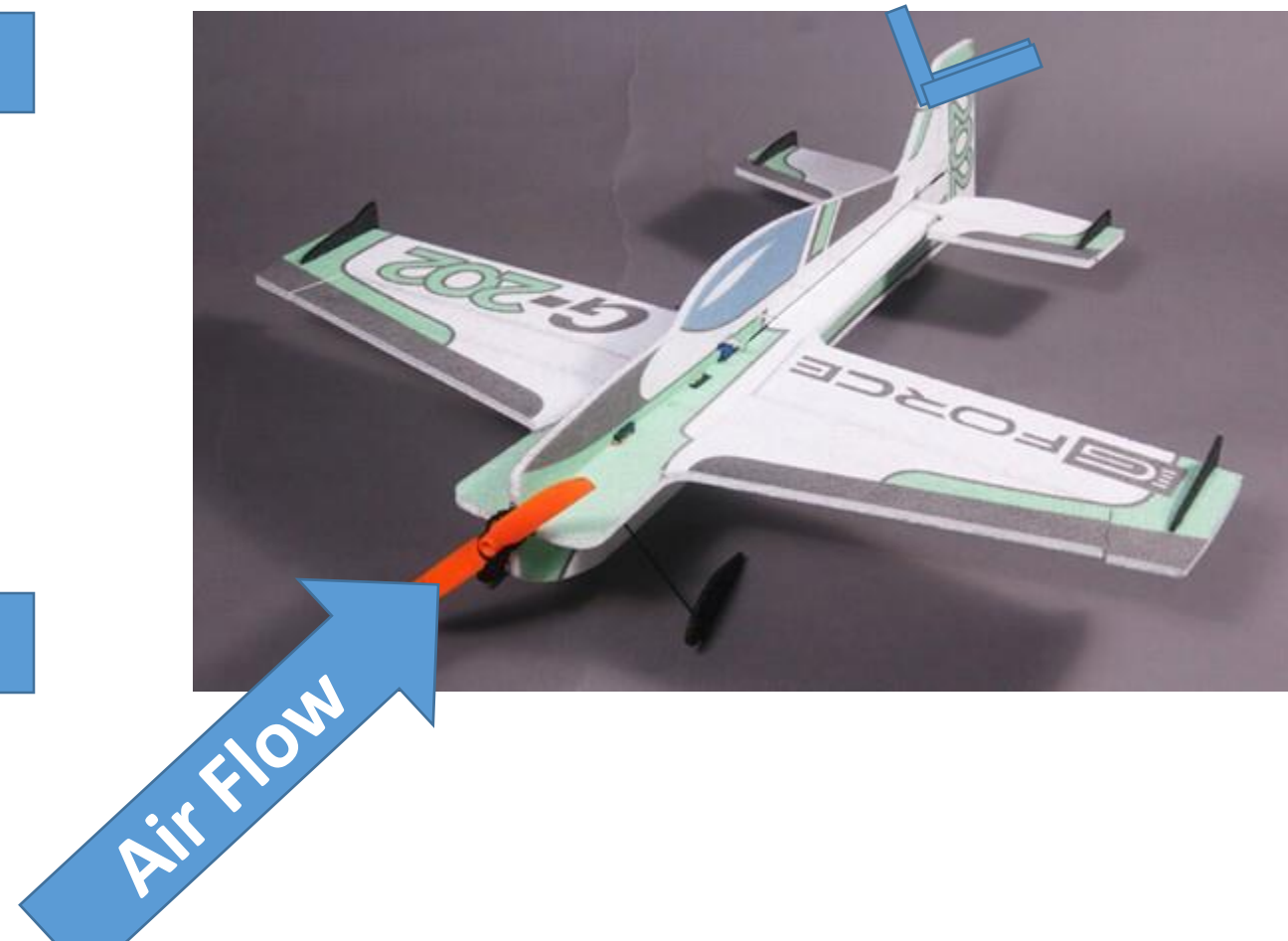


transmitter

# How control surfaces work



Demo 2: Using rudder on model airplane



# Types of RC planes:

Gas powered



Hobby  
1m wingspan  
1 kg (2 lbs)



Hobby, Jet turbine, 340 mph!



Military  
15 m wingspan  
500 kg (1100 lbs)



1900 mile flight  
across the Atlantic  
Ocean! 11 lb model  
took 38 hours to  
cross.



Commercial/law enforcement (aerial photography, surveillance, crop/drought monitoring,...)

# Types of RC planes:

Electric powered



Hobby  
1m wingspan  
2.6 g (a raisin has a mass of ~1g!)



Hobby  
Electric ducted fan  
0.5 kg and up



Hobby  
Propeller driven  
0.5 kg and up



Military  
1 m wingspan  
2 kg (4 lbs)



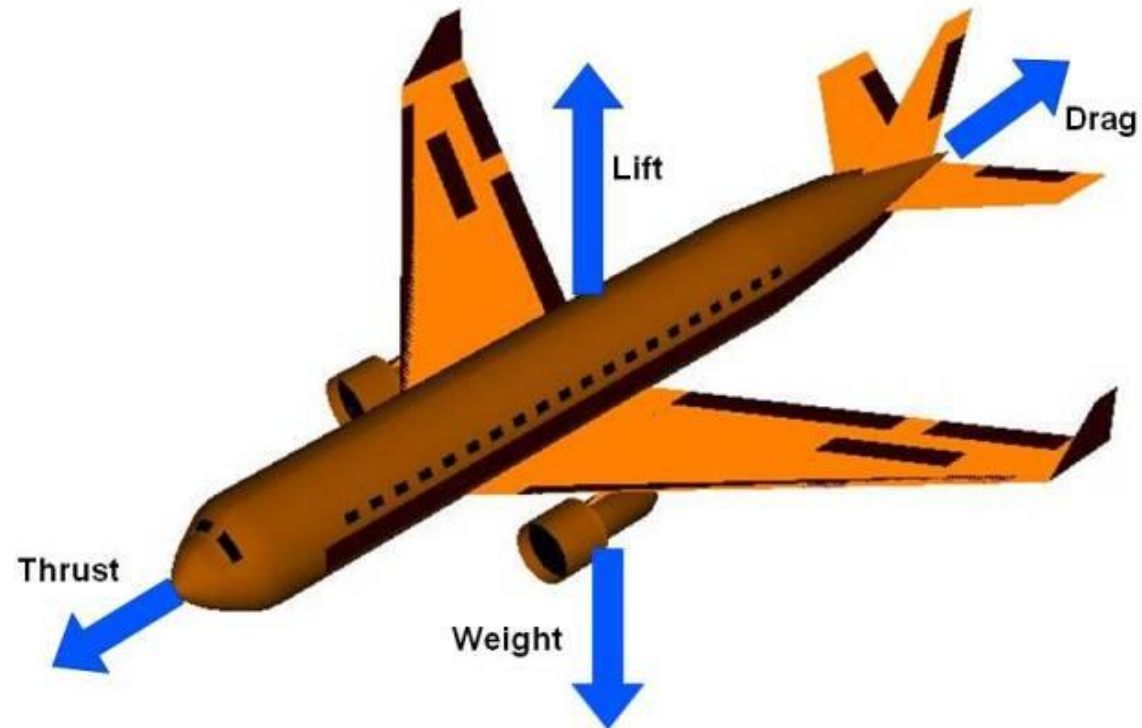
400 mph  
glider  
without a  
motor!

Commercial/law enforcement (aerial photography, surveillance, crop/drought monitoring,...)

# How does a plane fly? Forces on a plane?

National Aeronautics and Space Administration

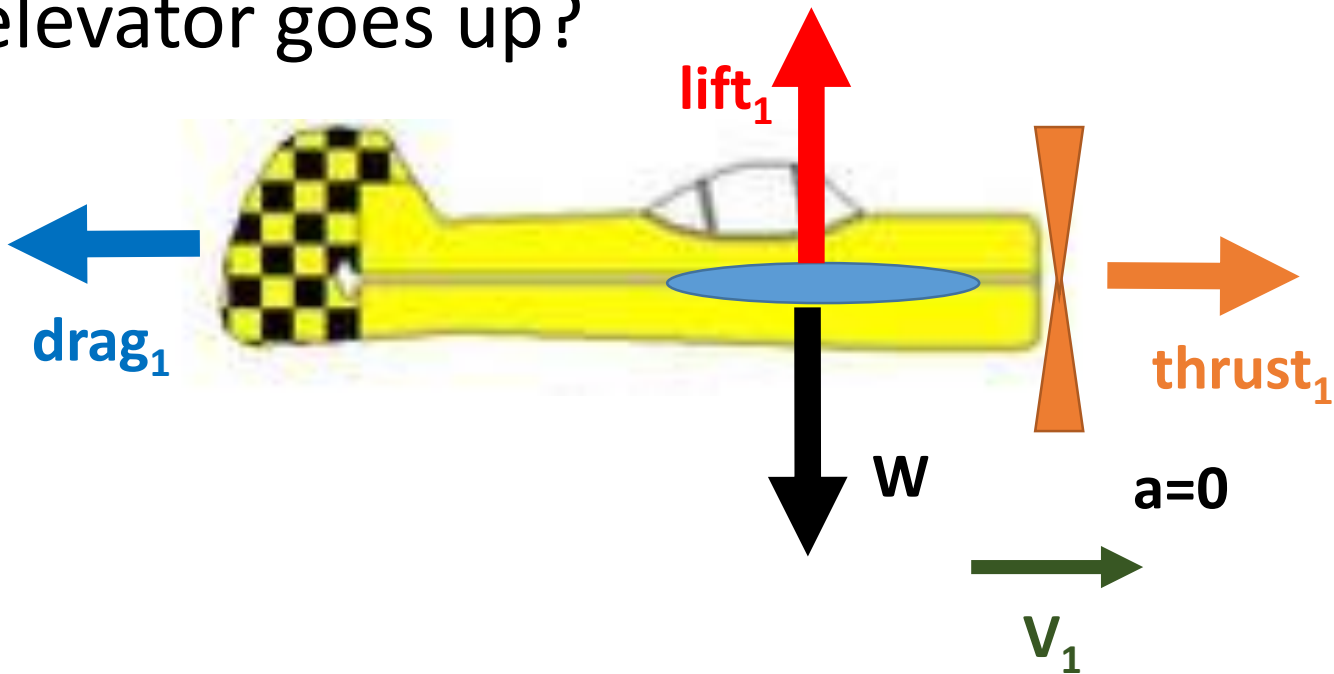
## *Four Forces on an Airplane*



# Increasing throttle?

Demo 3: Vapor flight at constant velocity

What happens if throttle increases? If elevator goes up?



What's another example of drag increasing as speed increases until drag matches the accelerating force (canceling it) and speed becomes constant?

# What are FORCE, WORK, and POWER

Force (F) causes an object to accelerate

Work (W) is energy expended by a force to move an object a certain distance

$$W = F d$$

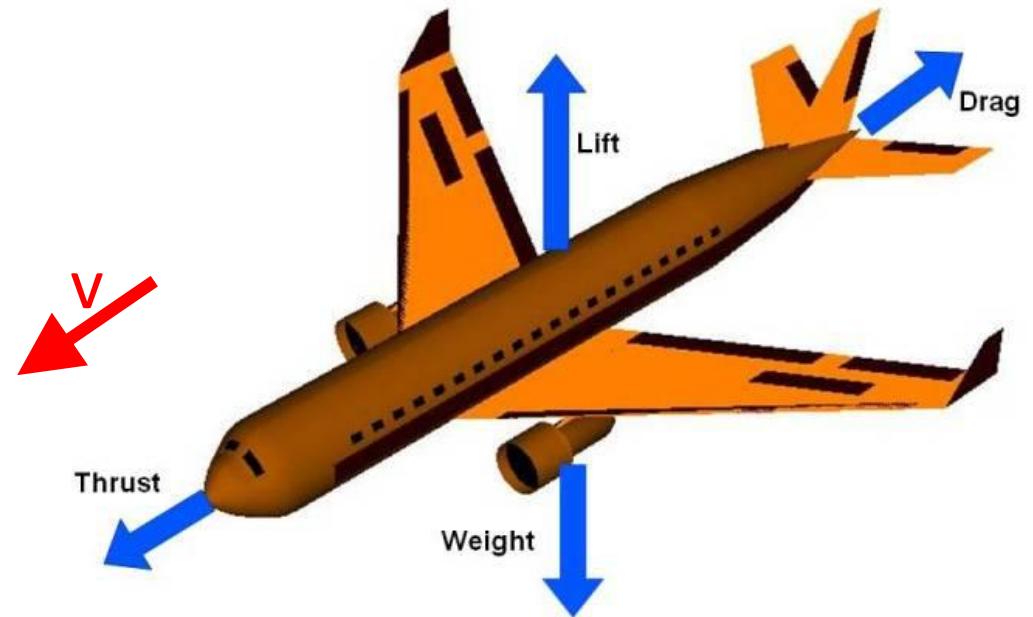
Power (P) is the RATE at which energy is expended by a force to move an object

$$P = W/T = (F d)/T = F (d/T) = F V$$

What is the power that a motor must supply to keep the airplane flying a constant speed? Assume V is large enough so the Lift cancels Weight.

National Aeronautics and Space Administration

## Four Forces on an Airplane



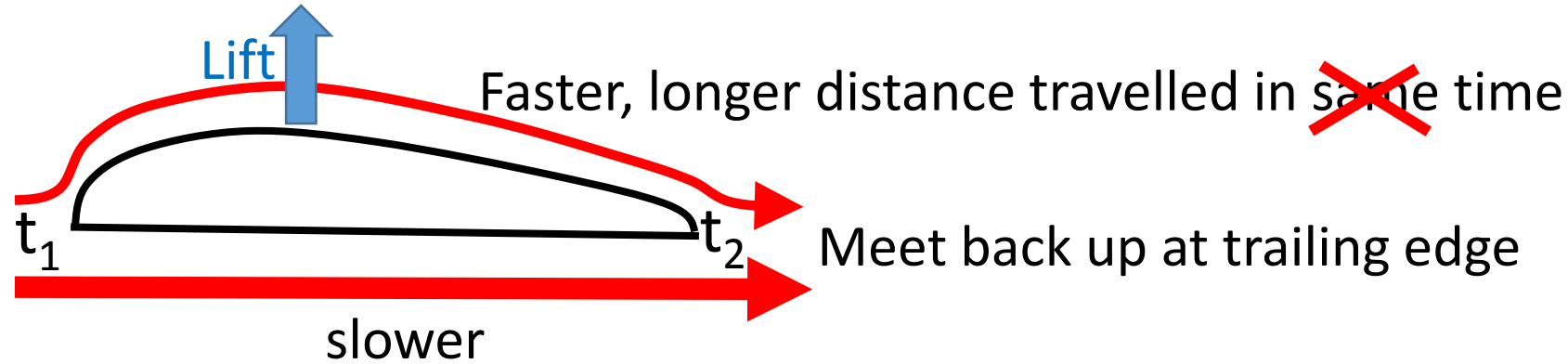
www.nasa.gov



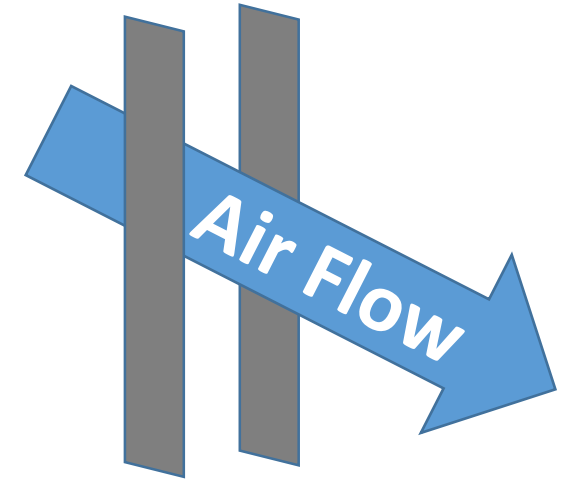
# Where does lift come from?

Demo 4: inverted flight, other modes (KE, hover)?

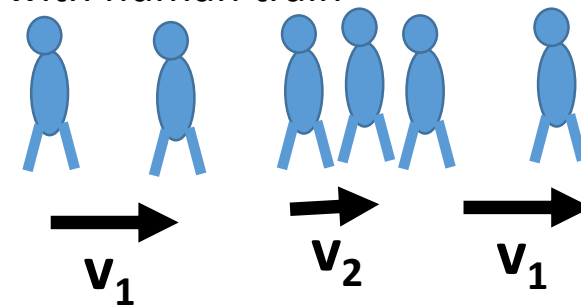
Traditional explanation:



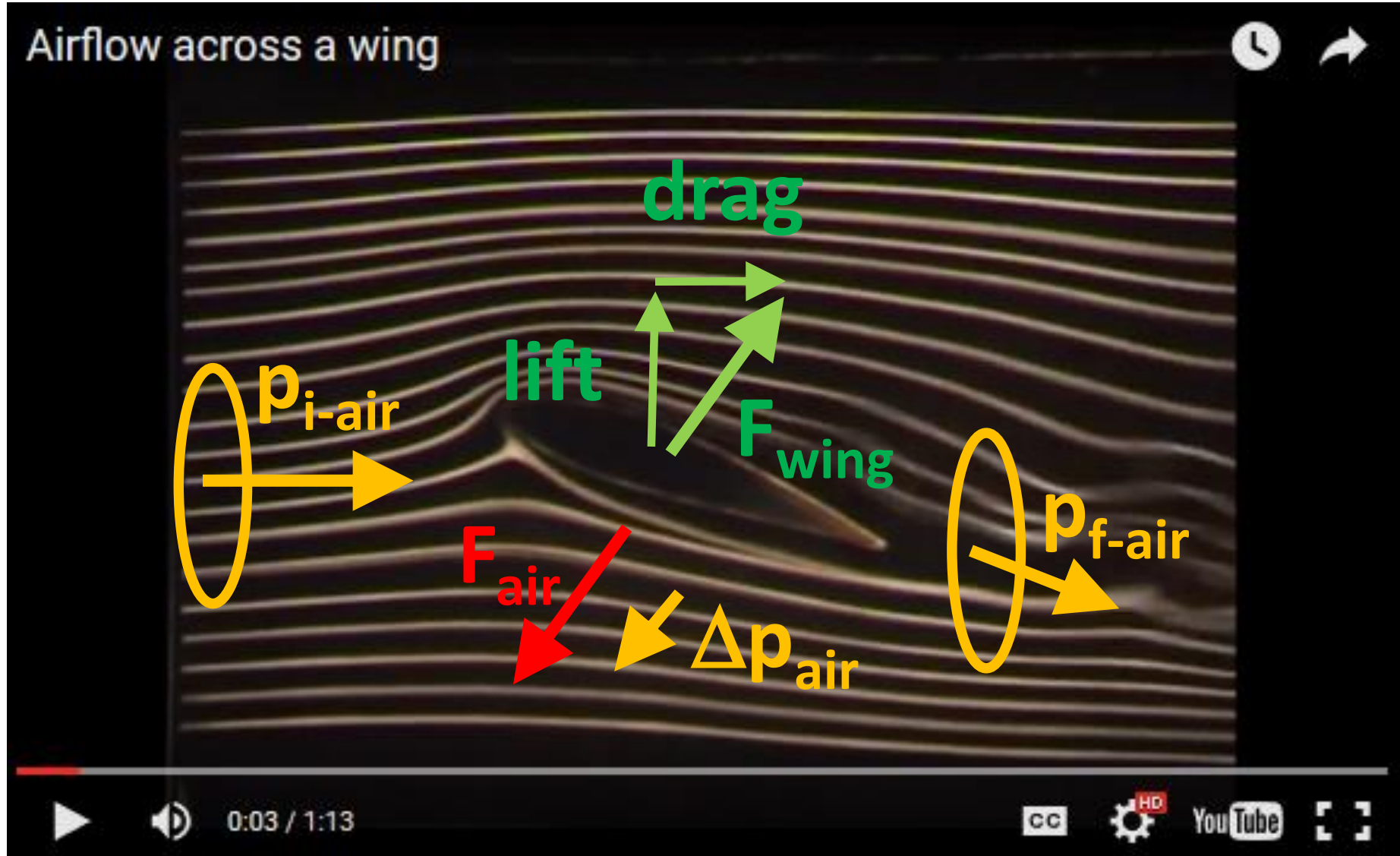
Demo 5: Bernoulli effect using two strips of paper



Demo 6: Bernoulli effect with human train



Wing deflects the airstream → lift



$$\vec{F} = \frac{\Delta \vec{p}}{\Delta t}$$

$$\vec{F}_{AB} = -\vec{F}_{BA}$$

# Audience Participation Question:

What physical parameters are involved in lift?

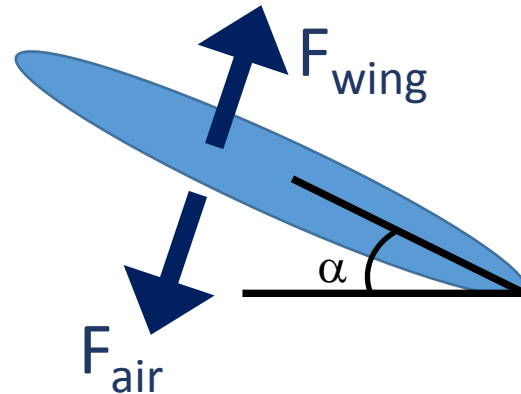
Hint: there are four

Speed  $V$ , air density  $\rho$ , wing area  $S$ , angle of attack  $\alpha$

What good and bad things happen as angle of attack  $\alpha$  increases?

$$\frac{\Delta M}{\Delta t} = \rho V S$$

$$\text{units: } \left[ \frac{\text{kg}}{\text{m}^3} \right] \left[ \frac{\text{m}}{\text{s}} \right] \left[ \text{m}^2 \right] = \frac{\text{kg}}{\text{s}}$$



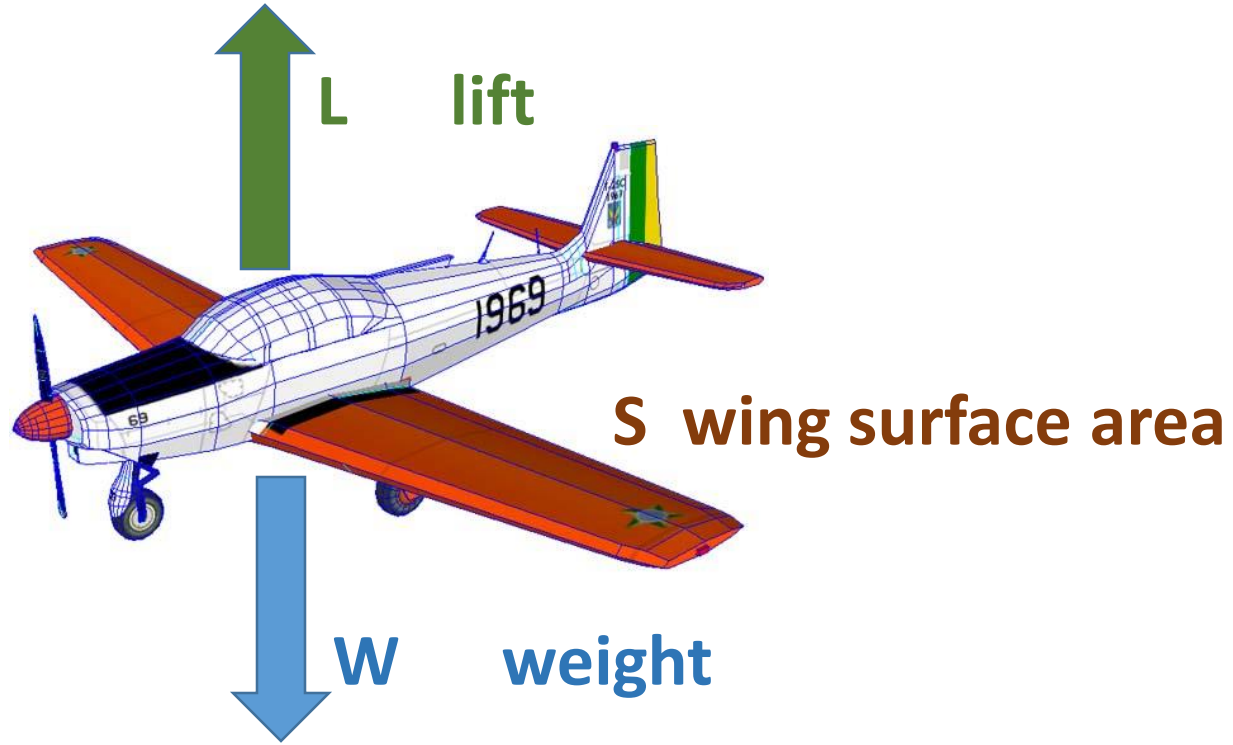
More lift (up to a point), more drag, airflow disturbed  
→ stall and control surfaces don't work → Colgan Flight 3407 2/12/09

$$F = \frac{\Delta p}{\Delta t} = \left( \frac{\Delta M}{\Delta t} \right) (\alpha V) = \alpha \rho V^2 S$$

$$\text{units: } \left[ \frac{\text{kg}}{\text{m}^3} \right] \left[ \frac{\text{m}}{\text{s}} \right]^2 \left[ \text{m}^2 \right] = \frac{\text{kg m}}{\text{s}^2} = \text{N} = \text{Force}$$

# Do larger planes fly faster?

Wing loading  
 $W/S$



How does wing area and plane weight scale with size?

# Aviation educational resources

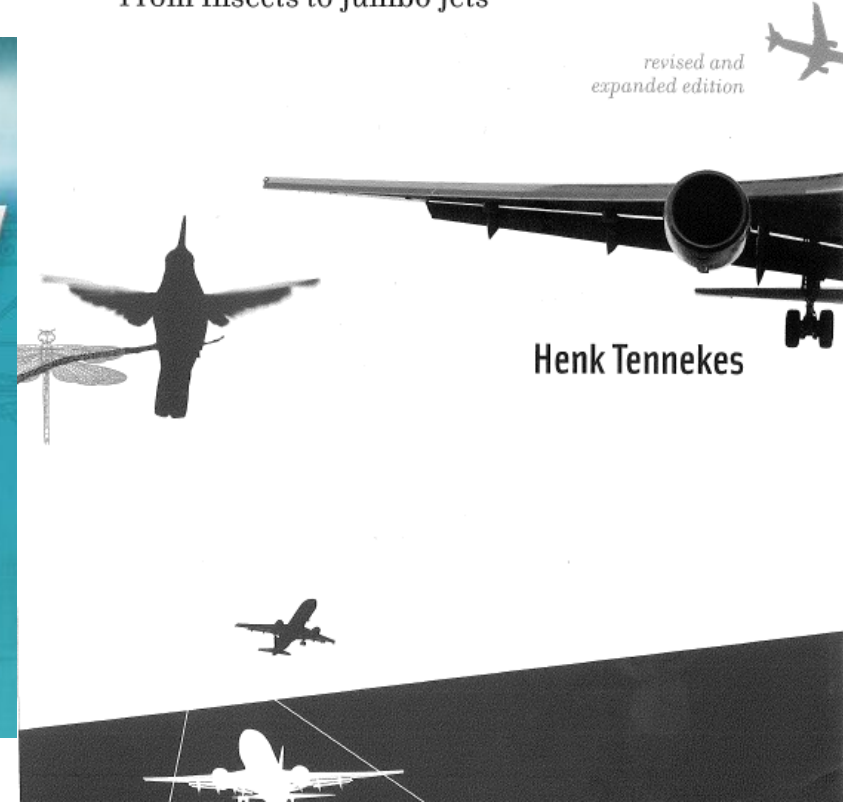


[www.acsupplyco.com](http://www.acsupplyco.com)

## The Simple Science of Flight

From Insects to Jumbo Jets

*revised and expanded edition*



Henk Tennekes



Home

Programs

DIY/Activities

Clubs

How do I?

Video

Learn sUAS

Contact us



FEATURED

### PROGRAM

#### UAS4STEM: Search and Rescue Challenge

Introducing a new STEM program from the Academy of Model Aeronautics, UAS4STEM!

Education

Youth Newsletter

Education Committee

Partners

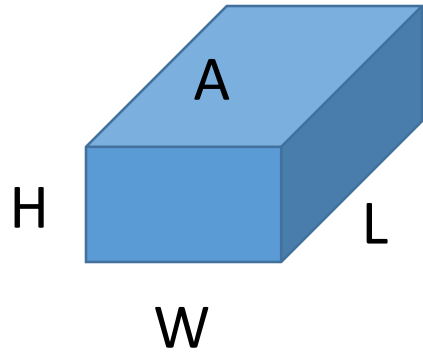
Contact Education

# AEROLAB

[jcerne@buffalo.edu](mailto:jcerne@buffalo.edu)

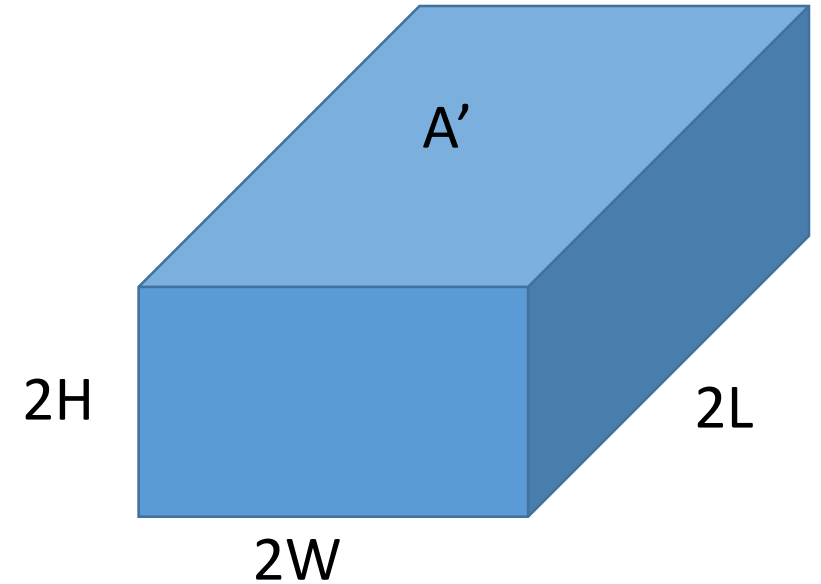
for waves and polarization [claw.physics.buffalo.edu](mailto:claw.physics.buffalo.edu)

# How does wing area and plane weight scale with size?



$$A = WL$$

$$M = \rho WLH$$



$$A' = (2W)(2L) = 4WL = 4A$$

$$\text{Mass} = \rho(2W)(2L)(2H) = 8WLH = 8M$$

Assuming a constant density, if all dimensions scaled up by a factor  $G$ , then  $A = G^2 A_0$  and  $M' = G^3 M_0$



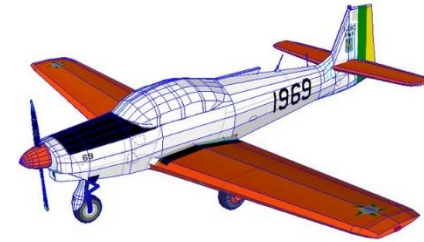
$$\frac{W}{S} \propto \frac{M}{A} = \frac{G^3 M_0}{G^2 A_0} = G \frac{M_0}{A_0} \propto G$$



# How does wing area and plane weight scale with size?



$$\frac{W}{S} \propto G$$



$$W \propto \text{Volume} \propto G^3 \rightarrow W^{\frac{1}{3}} \propto G$$

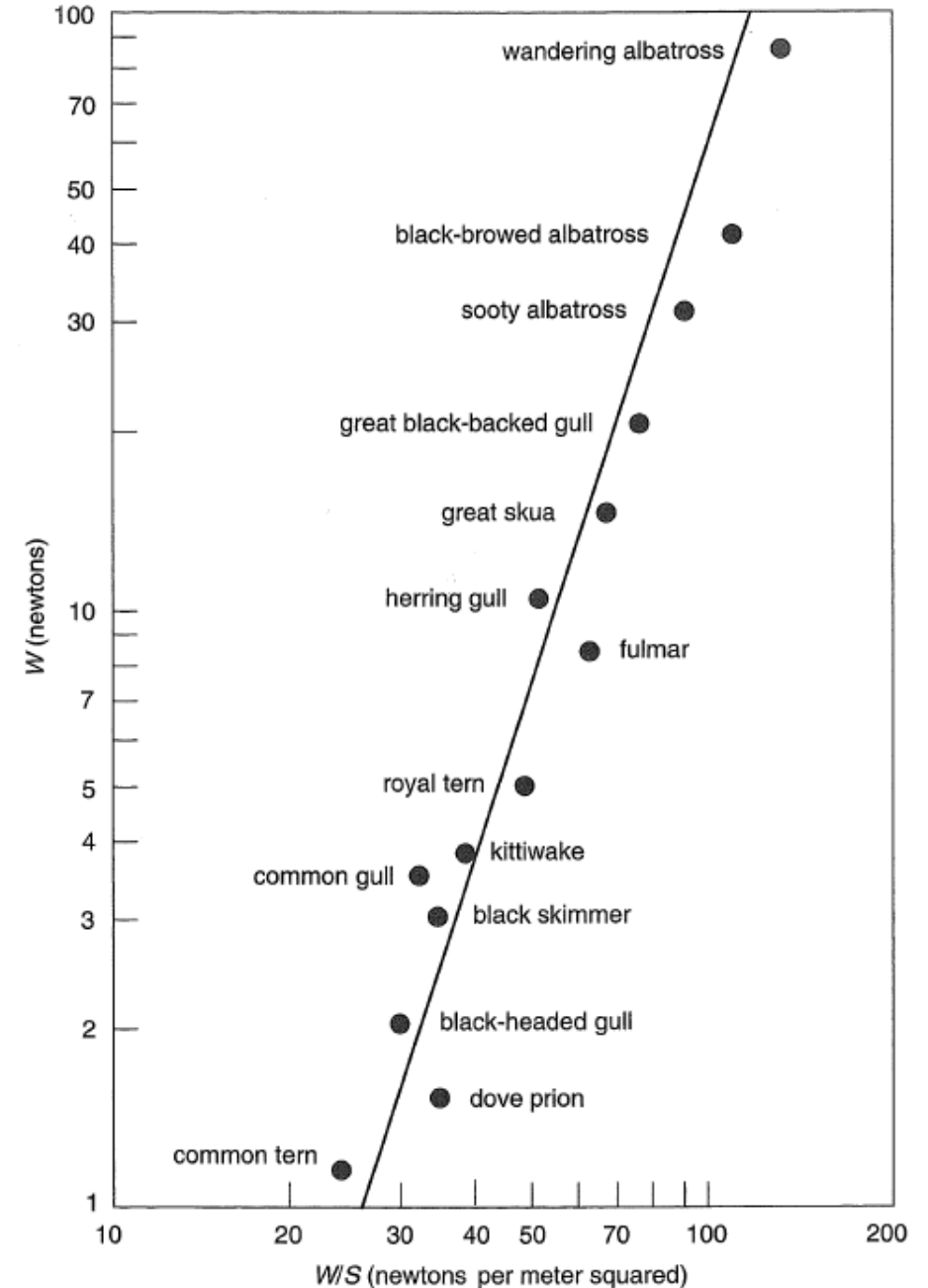
$$\frac{W}{S} \propto G \propto W^{\frac{1}{3}}$$

# Relationship between W and W/S

$$\frac{W}{S} \propto W^{\frac{1}{3}}$$

$$\rightarrow W \propto \left(\frac{W}{S}\right)^3$$

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Jets, H. Tennekes-





# Relationship between W and V

$$\text{Lift} \propto F = \alpha \rho V^2 S$$

$$\text{Lift} = W \propto F = \alpha \rho V^2 S$$

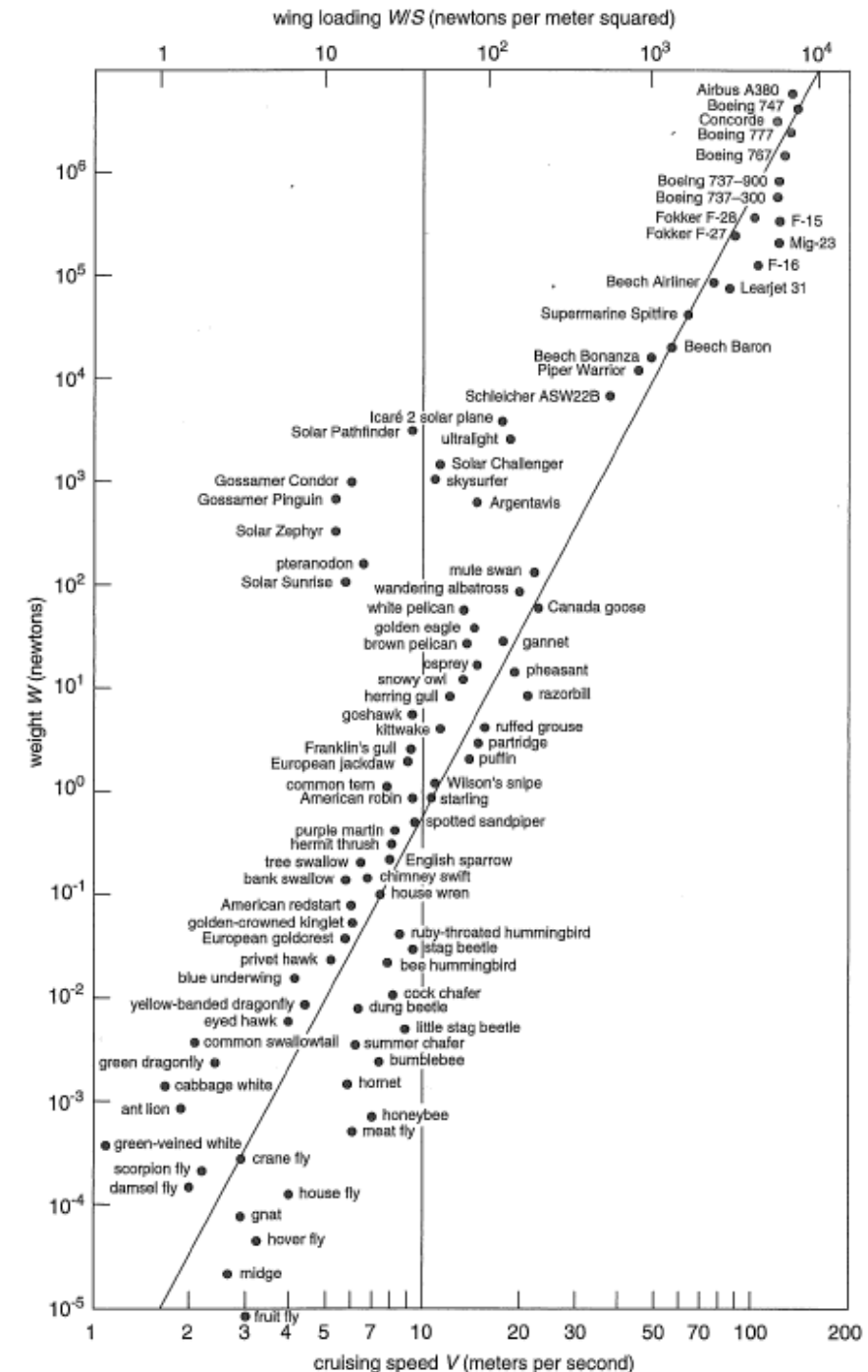
$$W = 0.3V^2 S \rightarrow \frac{W}{S} = 0.3V^2$$

$$\frac{W}{S} \propto G \propto W^{\frac{1}{3}} \text{ (from previous slide)}$$

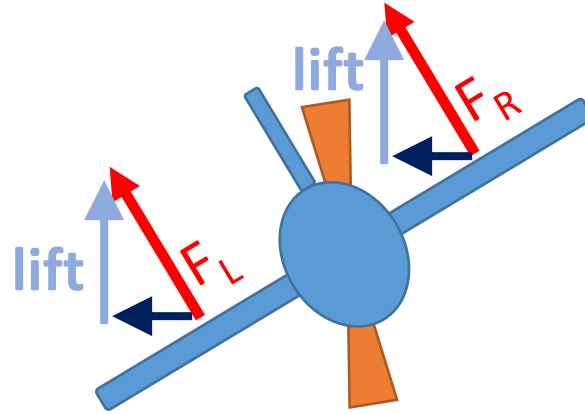
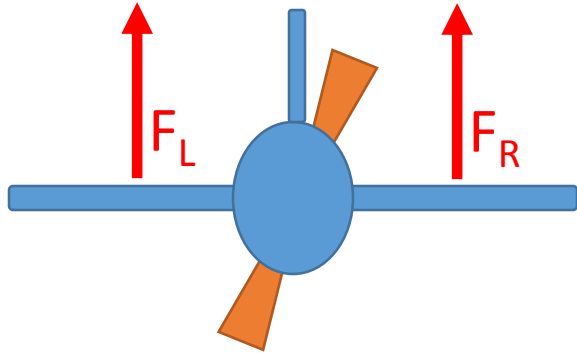
$$\rightarrow \frac{W}{S} = 0.3V^2 \propto W^{\frac{1}{3}}$$

$$\rightarrow W \propto V^6$$

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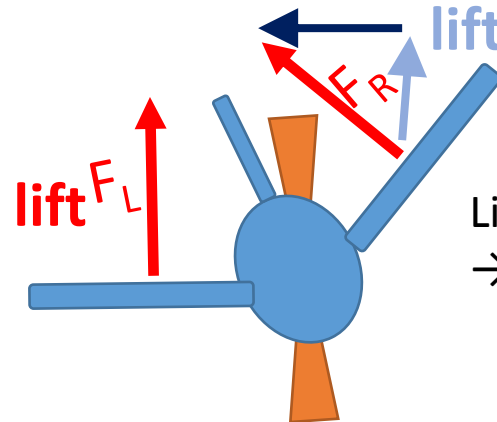
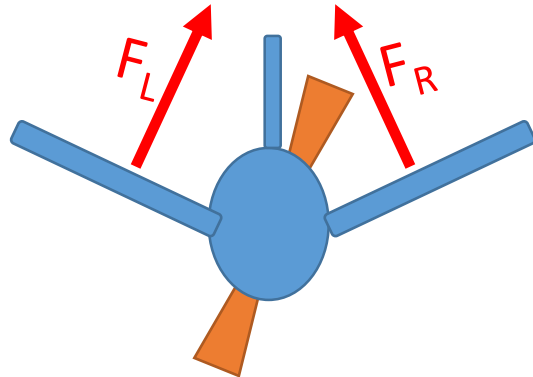


# Inherent Airframe Stability: Roll stability



Less lift and net force to left  
→ no tendency to roll back

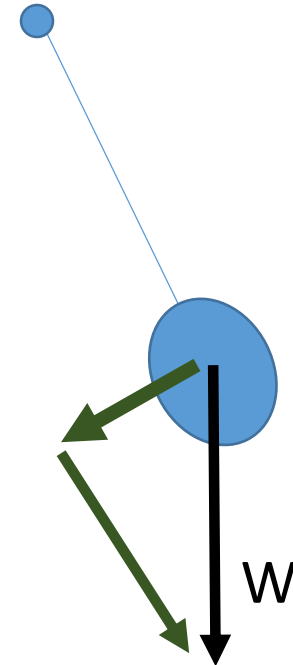
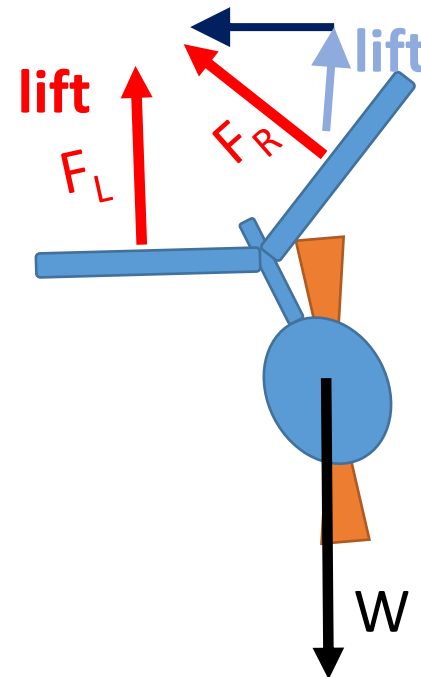
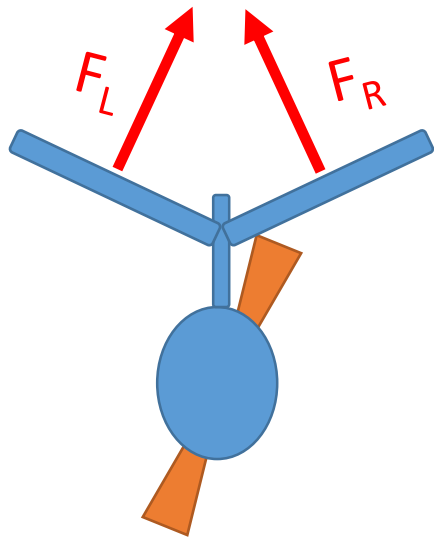
Dihedral wing



Lift on right wing less than on left wing  
→ plane will roll back to level

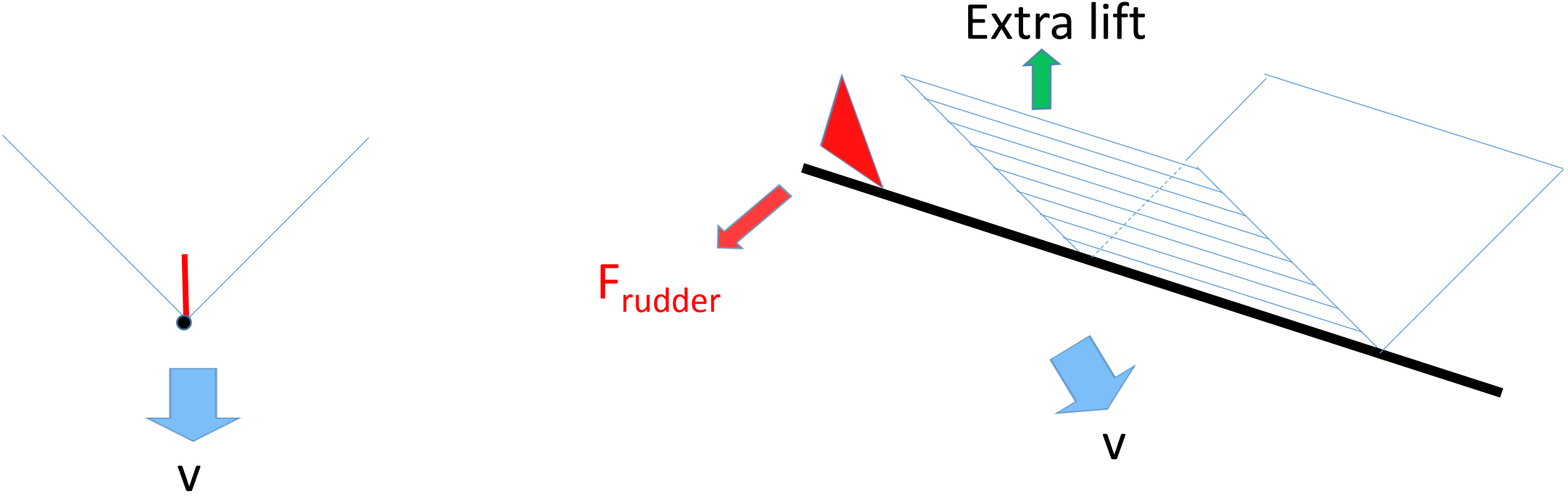
# Inherent Airframe Stability: more roll stability

Dihedral high wing



Lift on right wing less than on left wing AND mass of fuselage/motor tends to swing back to be centered on wing (like a pendulum)  
→ plane will roll back to level

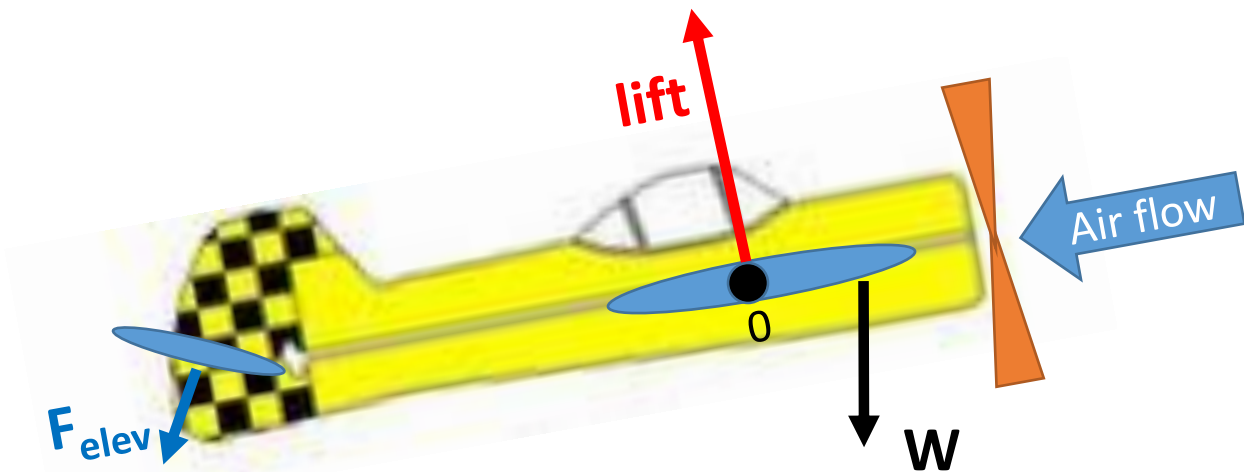
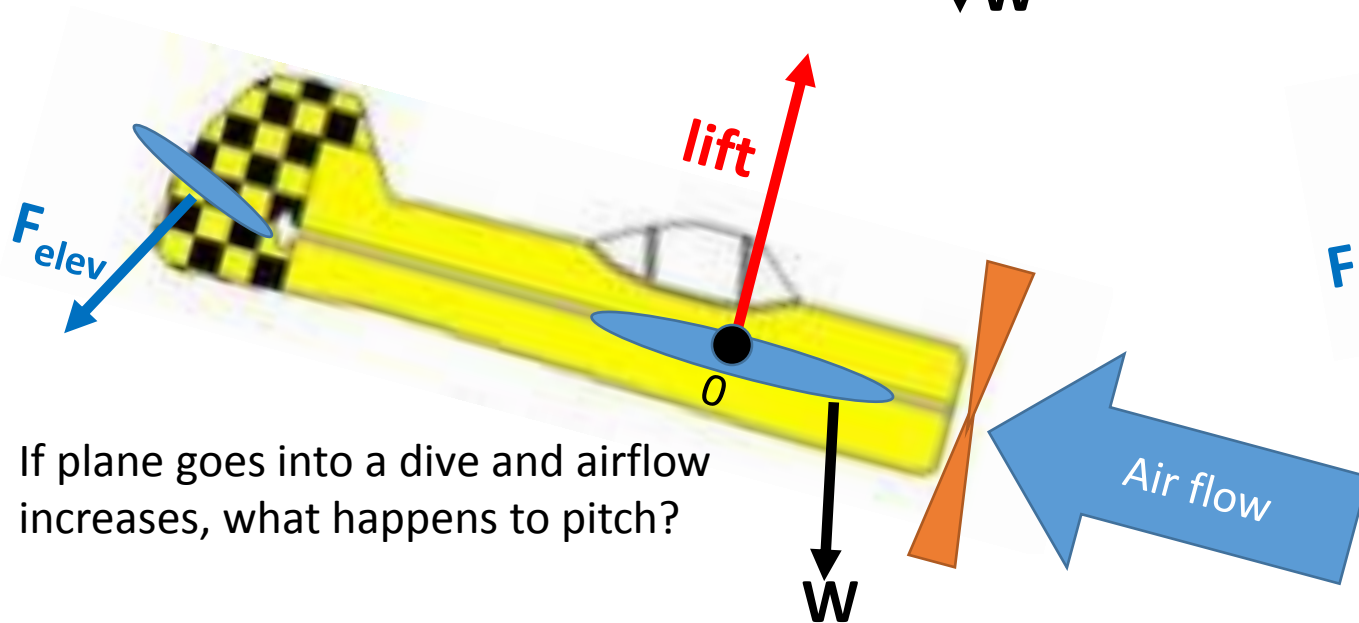
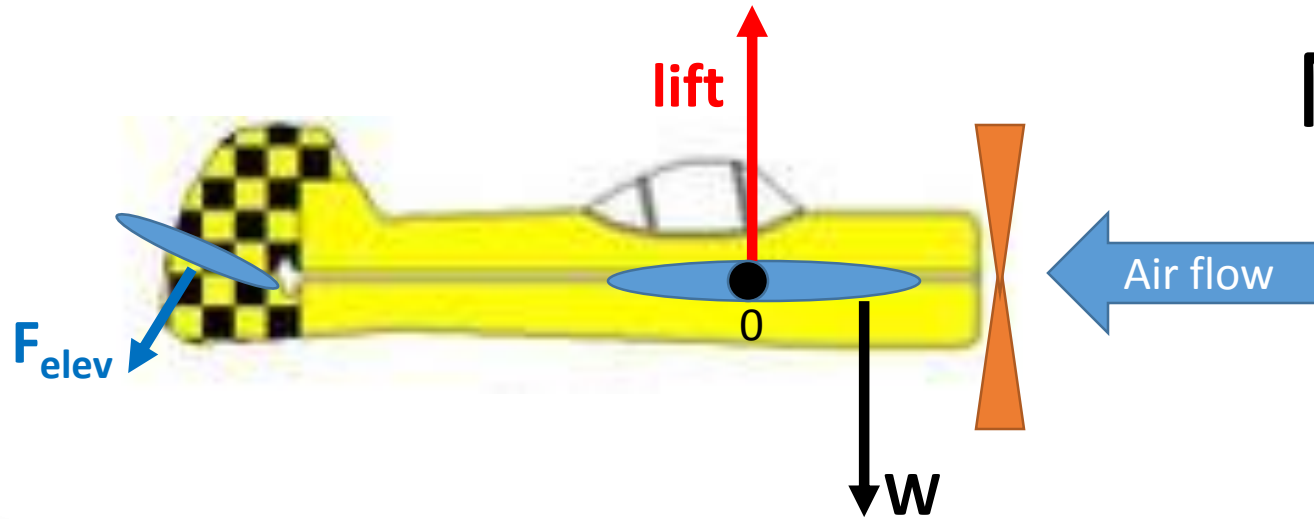
# Advantages/Disadvantages of Dihedral: Yaw-Roll Coupling



Demo 7: Yawing a folded card

# Inherent Airframe Stability: Pitch stability

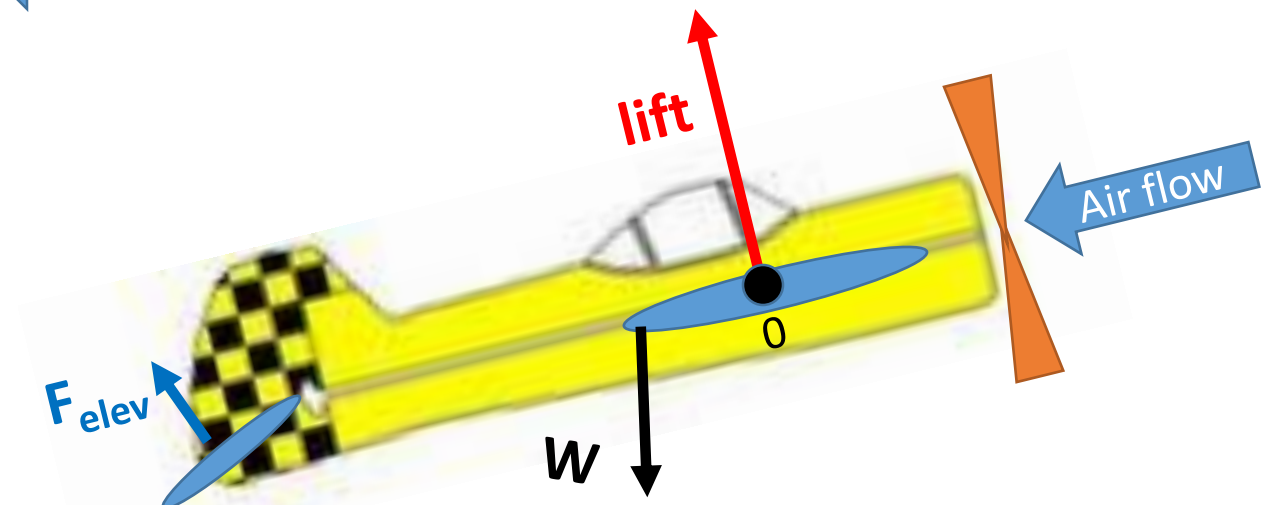
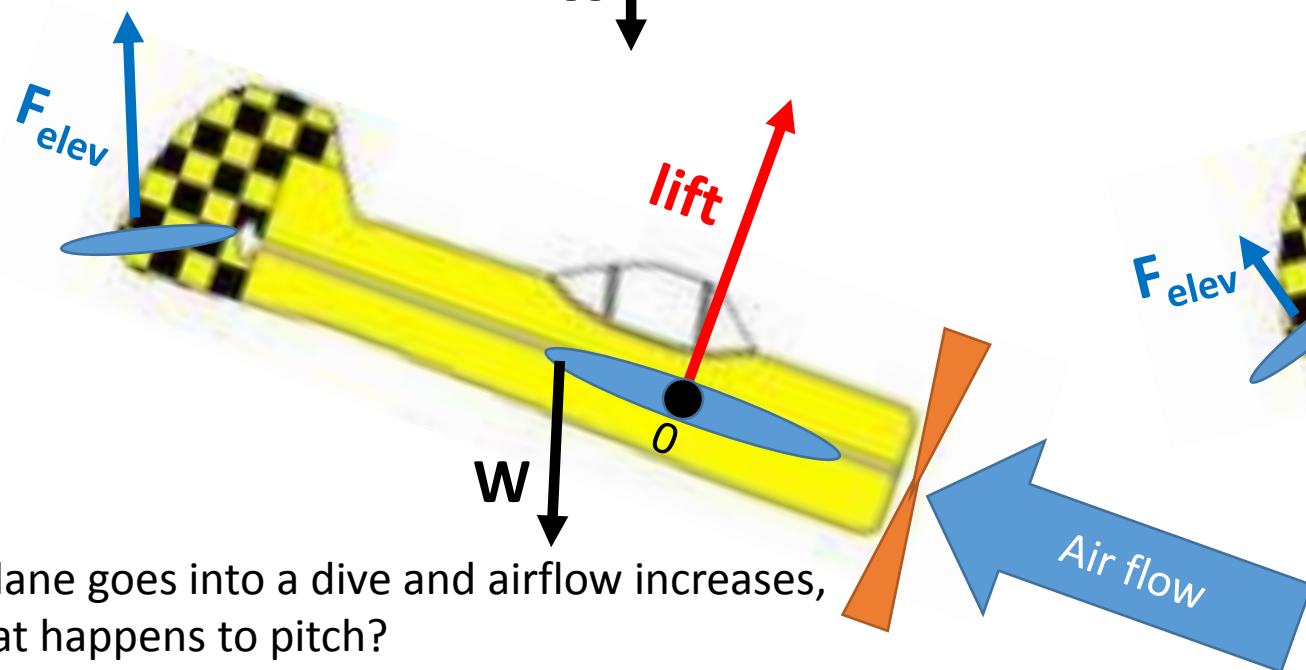
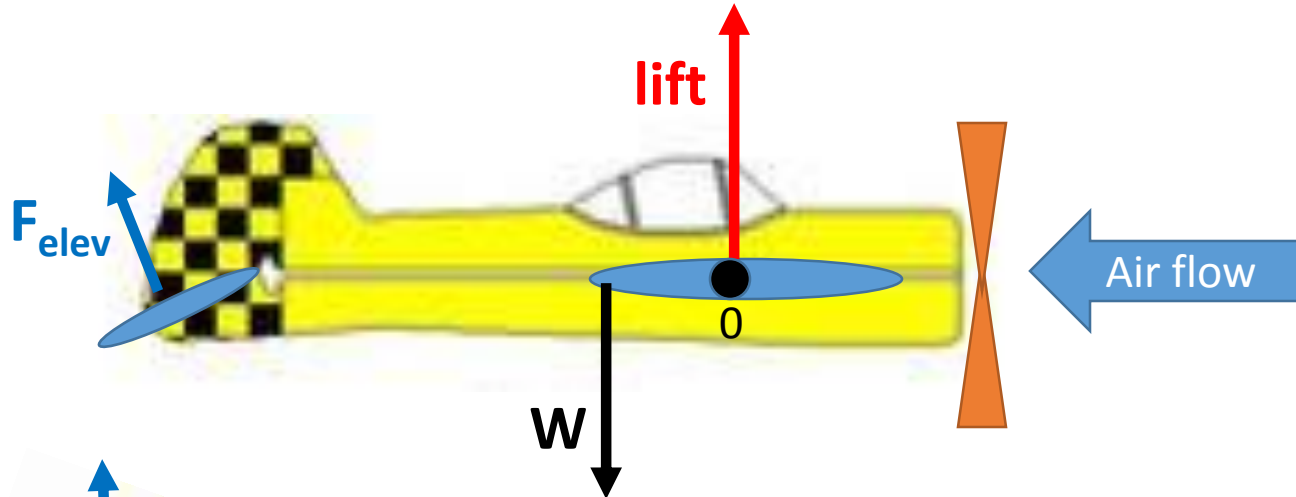
## Nose heavy airplane



If plane pitches up and airflow decrease, what is the response?

# Inherent Airframe Stability: Pitch stability

## Tail heavy airplane



If plane pitches up and airflow decrease, what is the response?

If plane goes into a dive and airflow increases, what happens to pitch?

How do we check if our plane is tail/nose heavy?

# Electronic Stabilization

## Inertial stabilization and the Foucault pendulum?!?!



Maneuverability  
Unusual shape

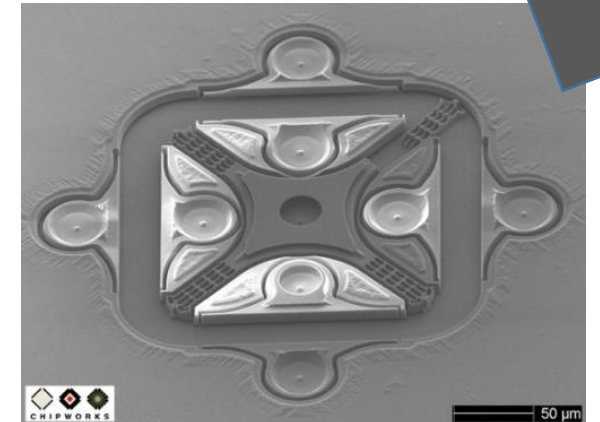


Demo 8: Foucault model



Demo 9: Drone stability

iphone MEMS gyro



Human hair



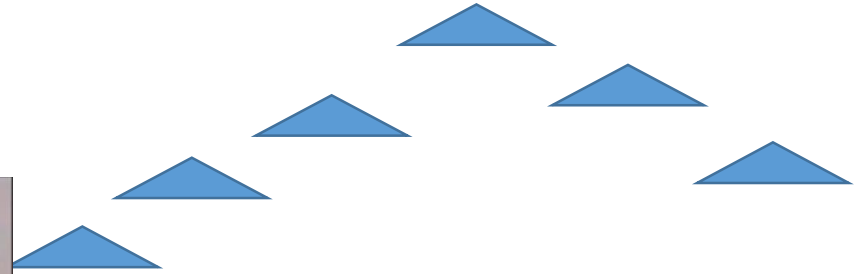
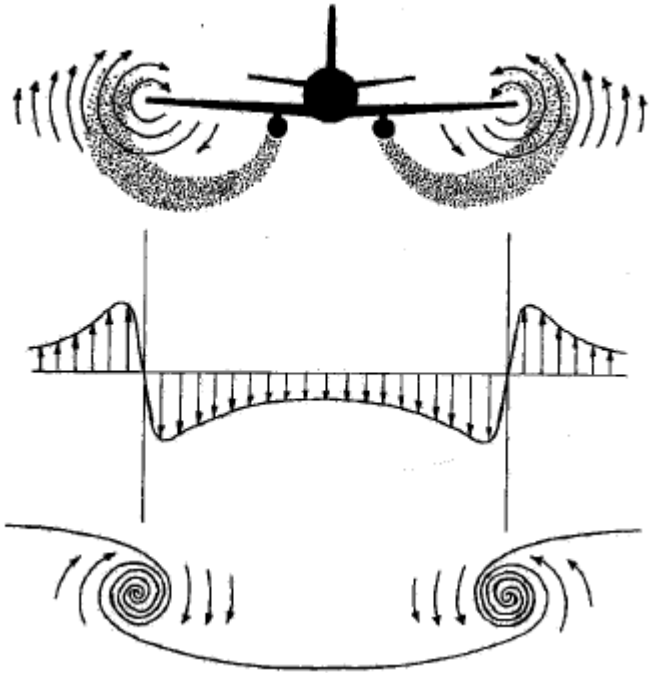
# Putting electronic stabilization to work- helicopters/multi-copters



Demo 10: Quadcopter flight and first person view (FPV)

# Drag and vortices

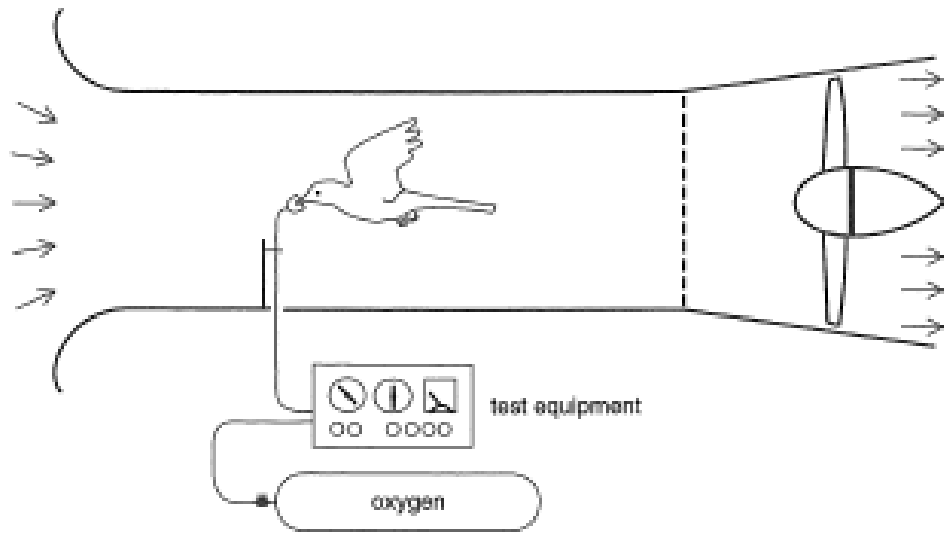
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$D \propto V^2$  but induced drag (power lost to vortices)  $D_i \propto \frac{W^2}{V^2 b^2}$

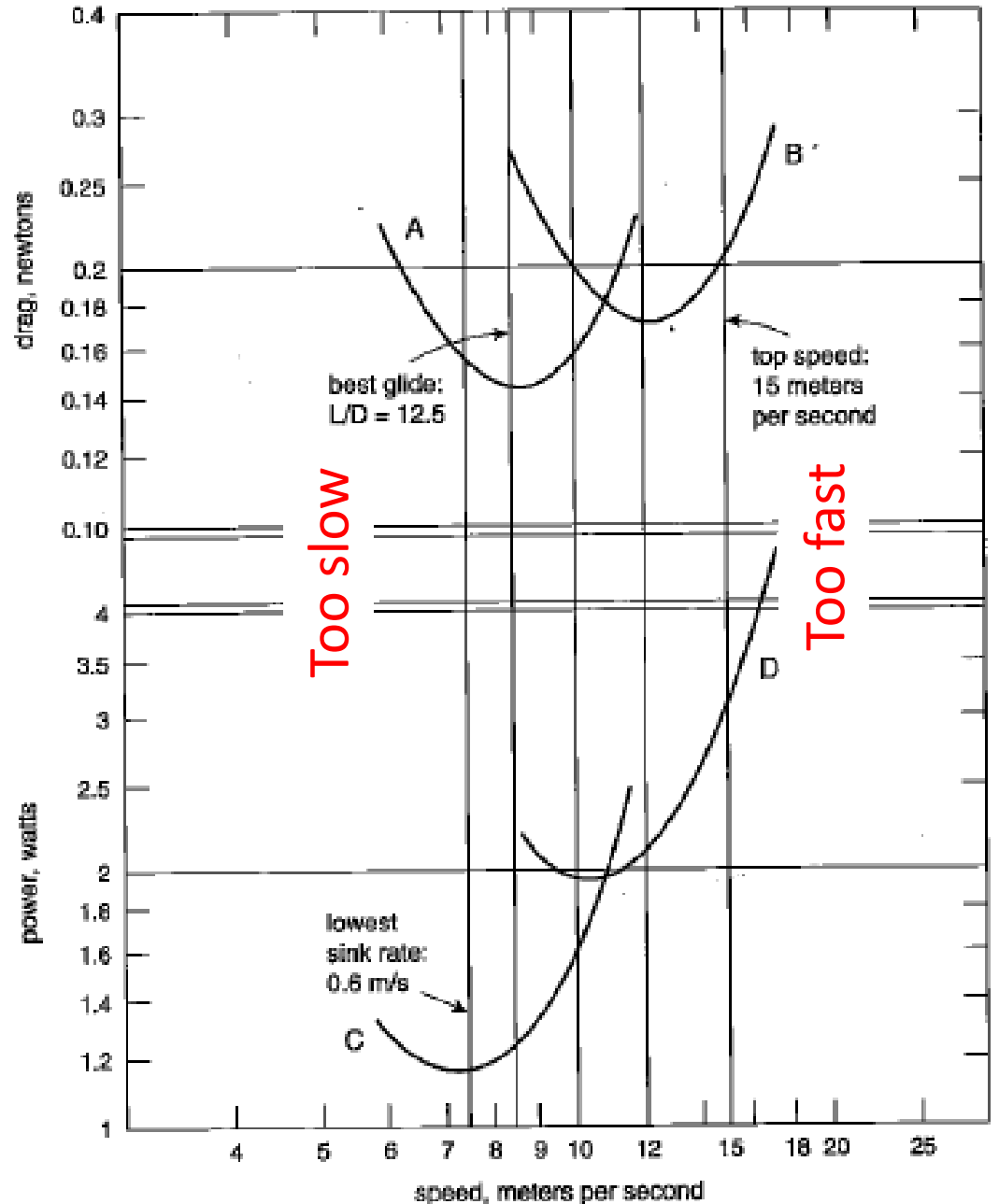
where  $b = \frac{\text{wing length}}{\text{wing chord}}$  (skinniness of wings)

# Most efficient flying speed

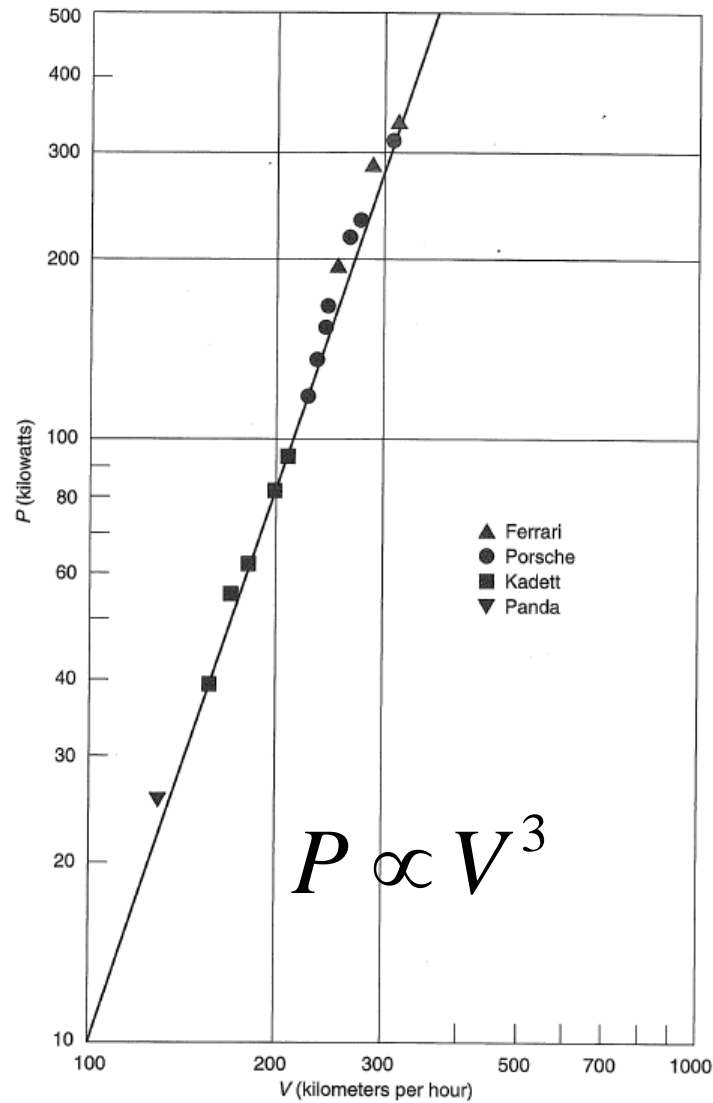


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Demo 11: Yak Harrier (simulator and real model): what happens in slow flight



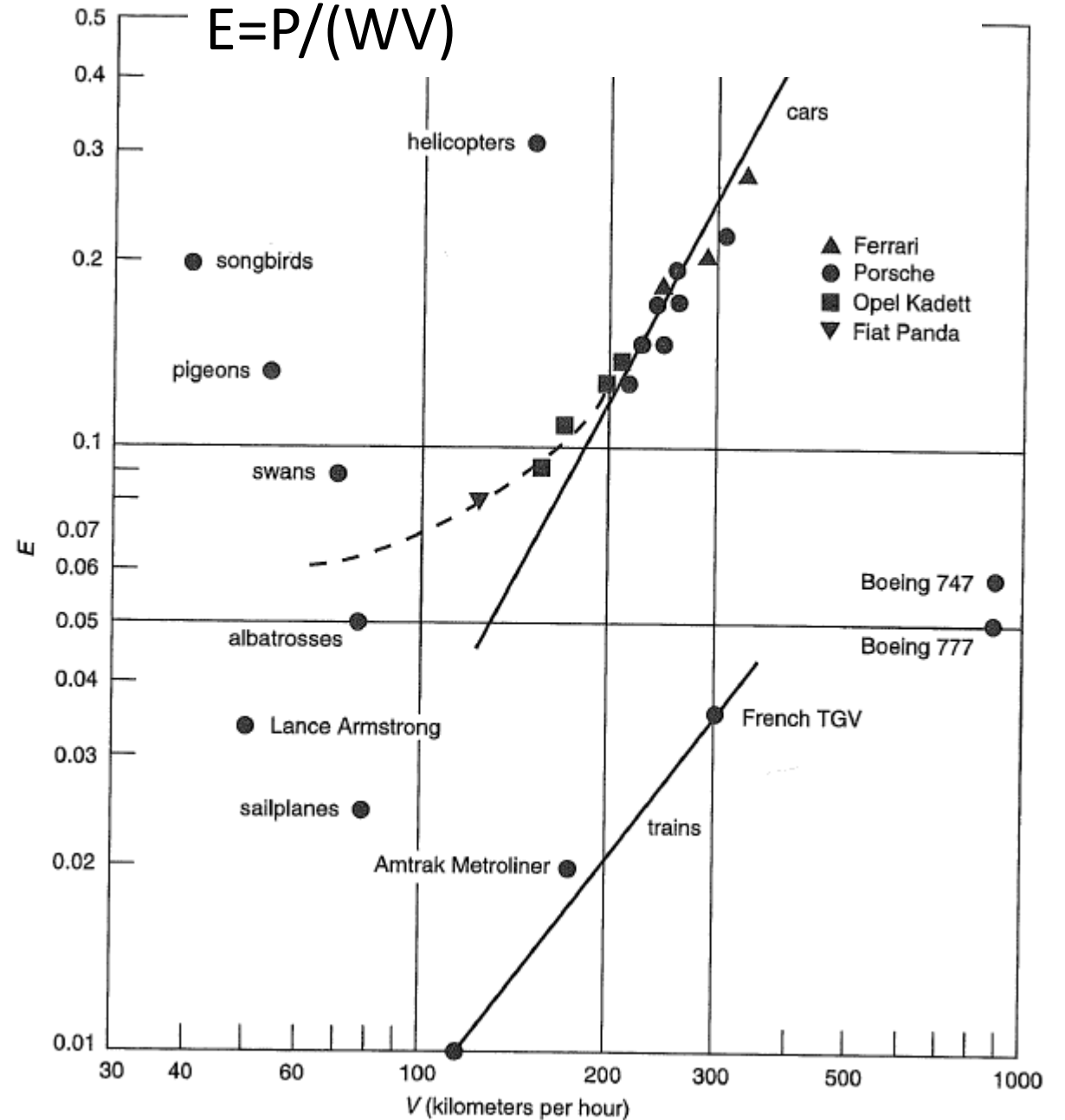
# Transportation Efficiency



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# Specific energy consumption

$$E = P / (WV)$$

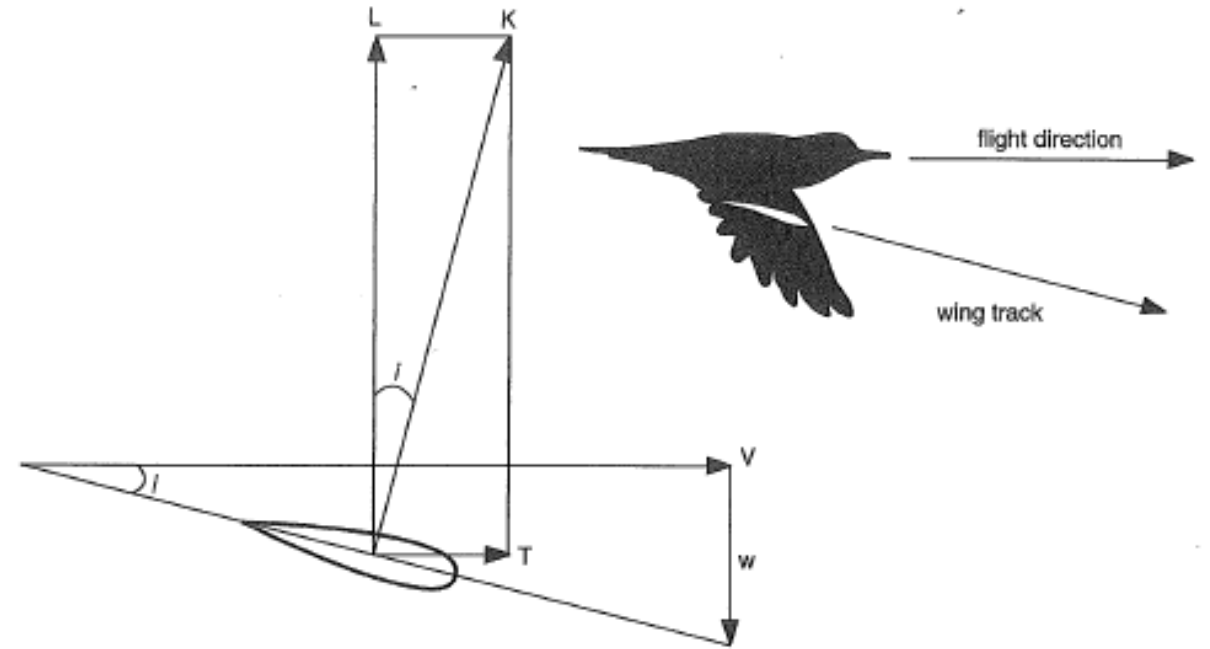
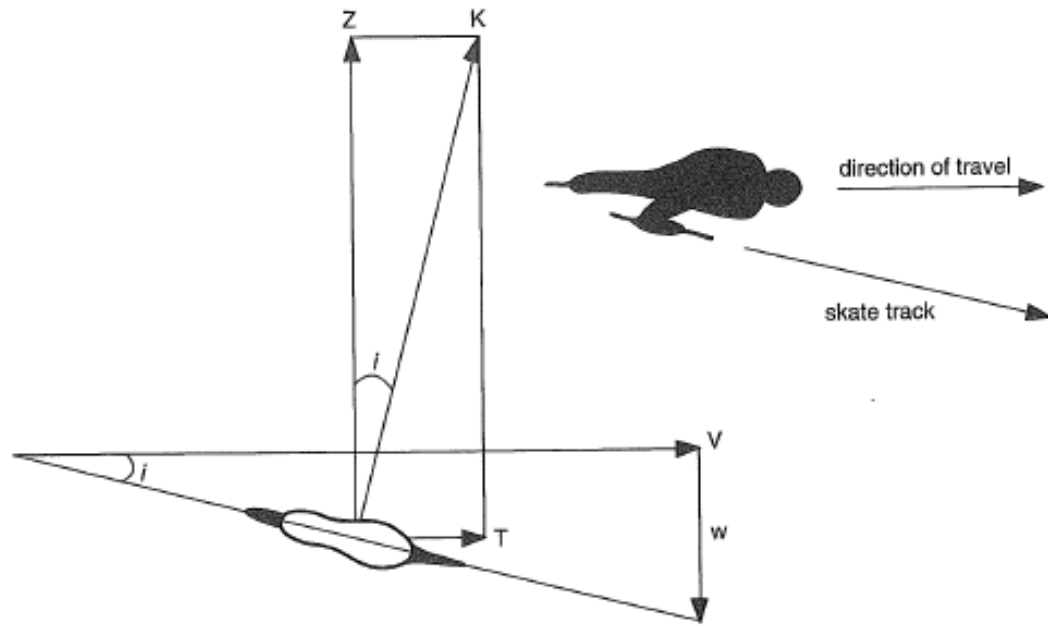


# Flying and biology → BIRDS

1. Biomechanics-how they fly
2. Biochemistry-how they power their flying
3. Navigation
4. Time-keeping

# Biomechanics-how they fly

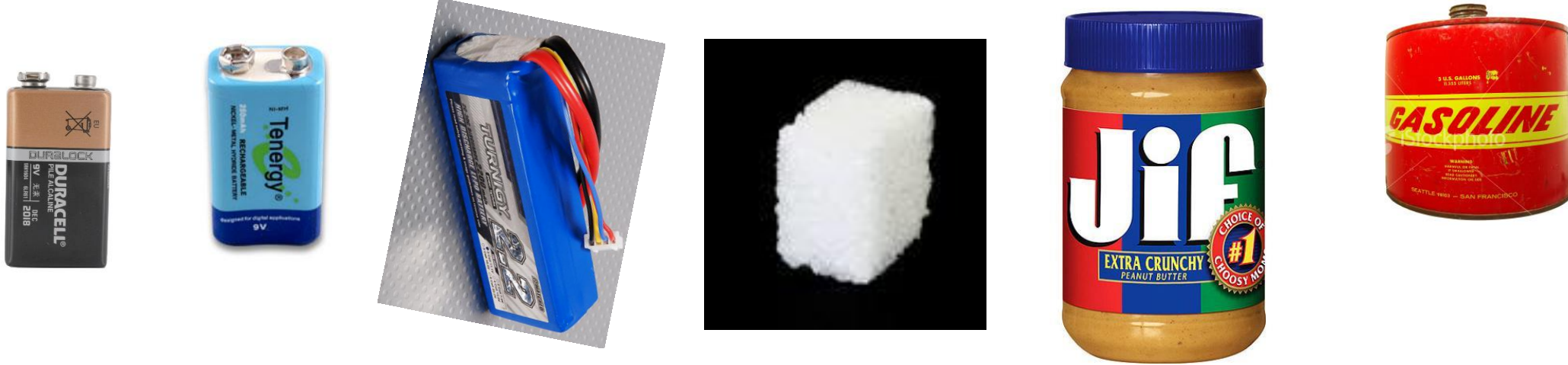
Flapping wings is like paddling a canoe. True or False?



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# Biochemistry-how they power their flying

What is the difference between energy and power?



## Storage type

Alkaline battery

NiCd battery

NiMH battery

**Lithium Polymer battery**

**Sugar**

**Fat**

Gasoline

## Energy Density (MJ/kg)

0.28

0.18

0.27

**0.55**

**15**

**32**

42

## Specific Power (W/kg)

39

150

200

**6000**

**800\***

**RC Models**

**muscles in humans**

**muscles in birds**

\*estimated from Tennekes p. 60, swan consuming 2g of fat per mile traveling at 45mi/h

# Some comparisons

Bird 100W/kg muscle (better pulmonary system)



Human 20W/kg muscle

Sugar energy density 14 MJ/kg (metabolized by humans)



Fat energy density 32 MJ/kg (metabolized by most birds)

Muscle efficiency 25%



Brushless motor efficiency 60% to over 90%

Premier athletes can maintain 5x base heart and 20x base metabolic rates for extended time



Birds can maintain 7x base heart and 14x base metabolic rates for extended time



# Navigation?

Photochemical reaction in retina produces short-lived chemical whose lifetime is sensitive to magnitude and direction of earth's very weak magnetic field, Nature 2008

Grains of iron oxide (magnetite) in beak, but more recent studies found it in inner ear

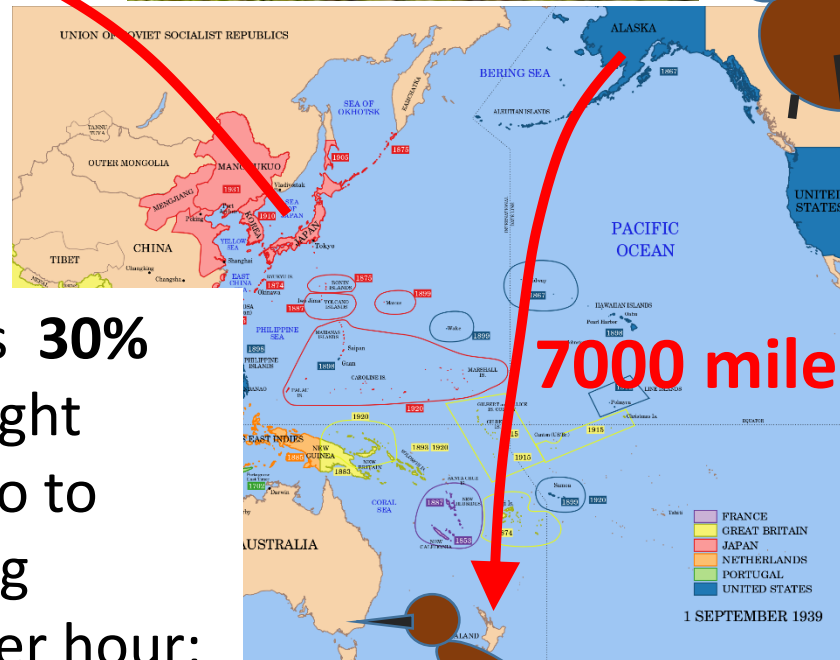
Even if they know direction, how do they know location (high winds ~40 mph can easily carry them off course)?

# Amazing examples of endurance and navigation

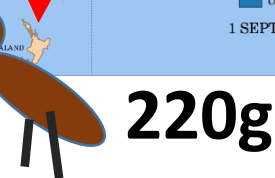
## Bar-tailed godwit



A Boeing 747 loses how much weight in fuel during a 13 hour, 9300 km flight?



Note: A Boeing 747 loses **30%** (130 tons) of takeoff weight during a flight from Tokyo to Amsterdam → lighter wing loading → climbs 800 ft per hour; 30,000ft → 40,000ft



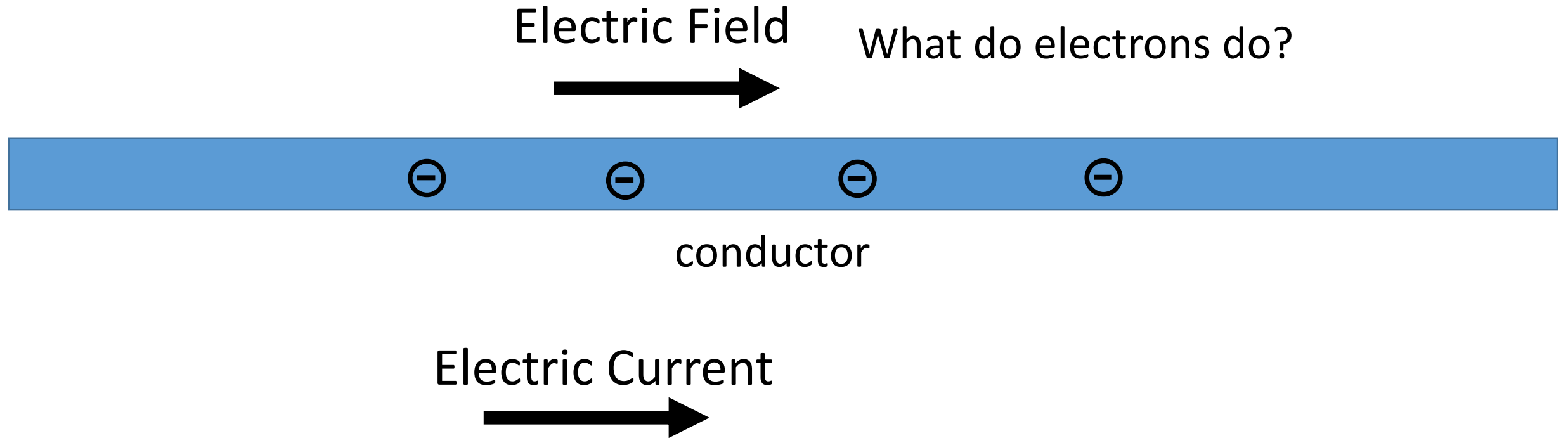
Consumes 220g fat, 40g flight muscle, and 20g of other tissue during 9-day nonstop trip!

# Keeping flight sensor/computer stable

YouTube



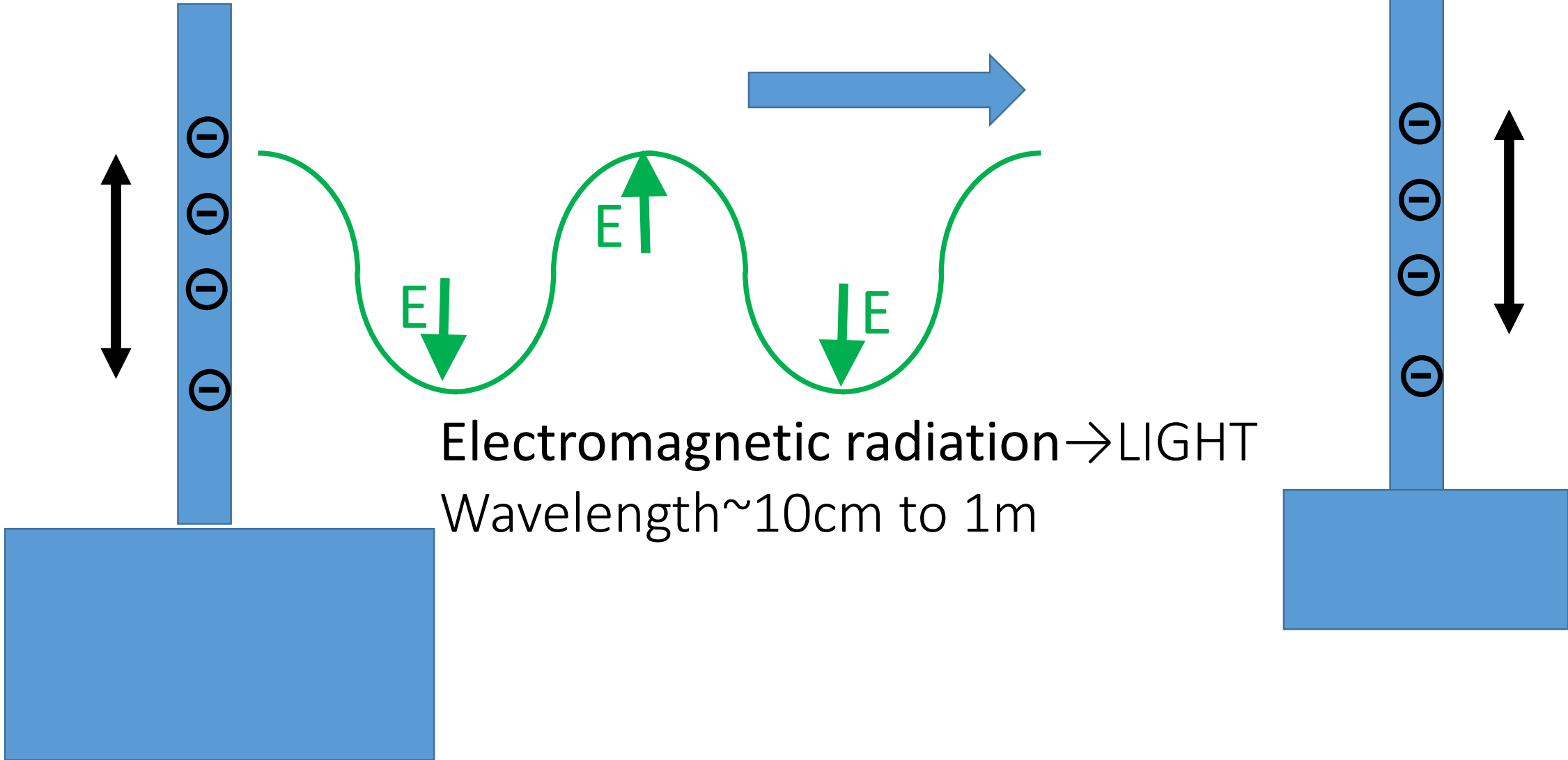
# Radio control: how does it work?



# Radio control: how does it work?

Transmitter antenna

Receiver antenna

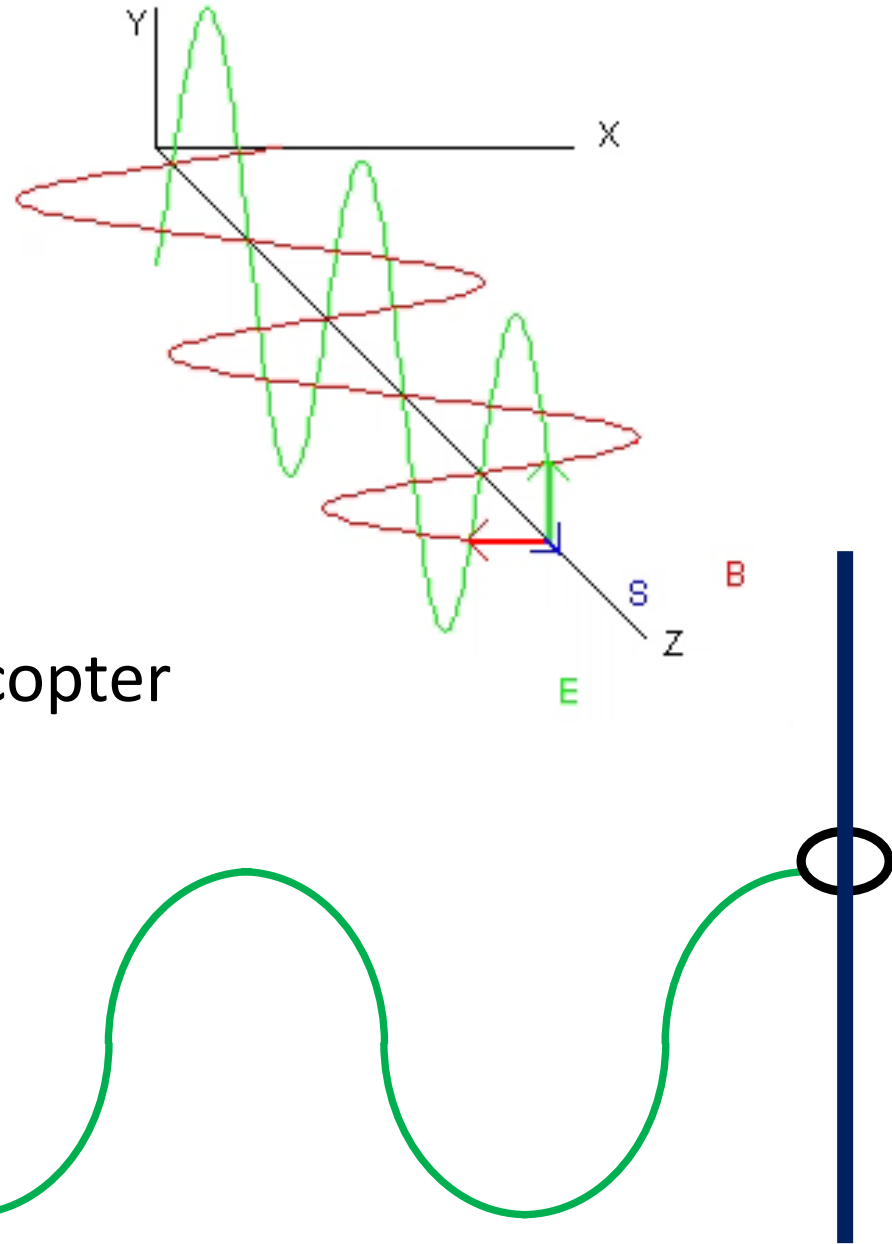


# Polarization of light

claw.physics.buffalo.edu

Demo 12: Polarized wave

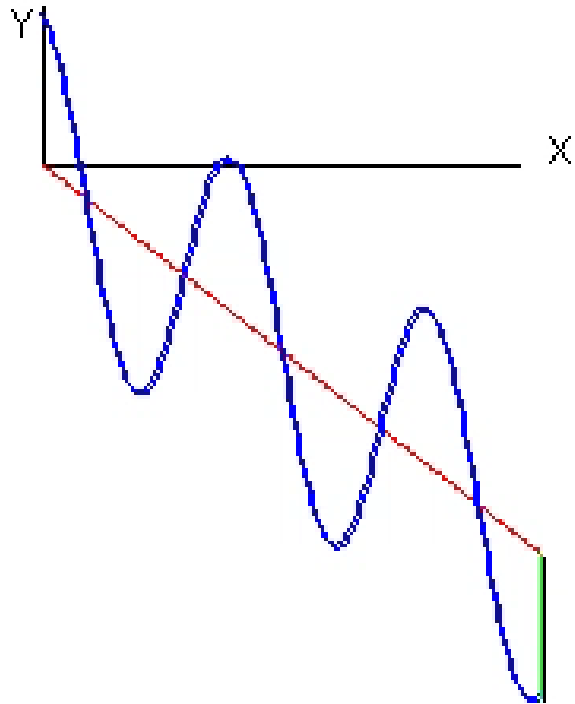
Look at receiver antennas on quadcopter



Why TWO antennas?



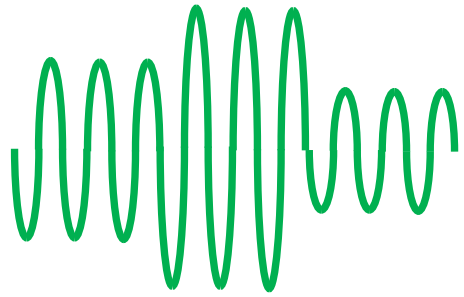
# Polarization Physlet



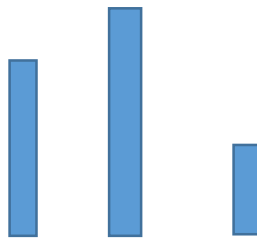
Antenna for left-circularly polarized light



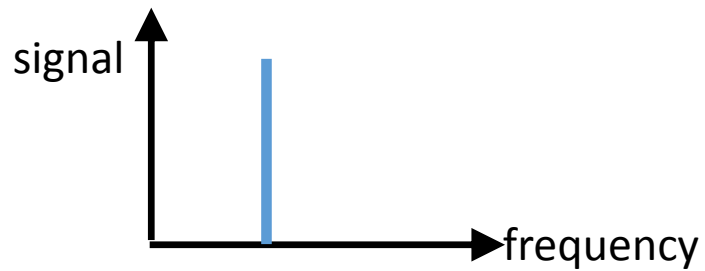
# Some Radio Control Concepts



Amplitude Modulation

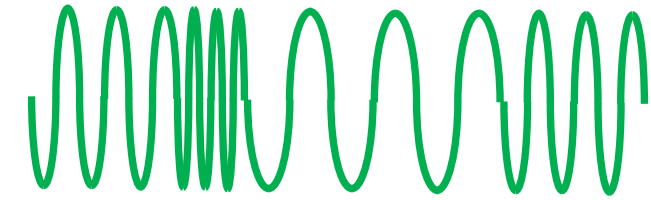


Analog



Single radio frequency

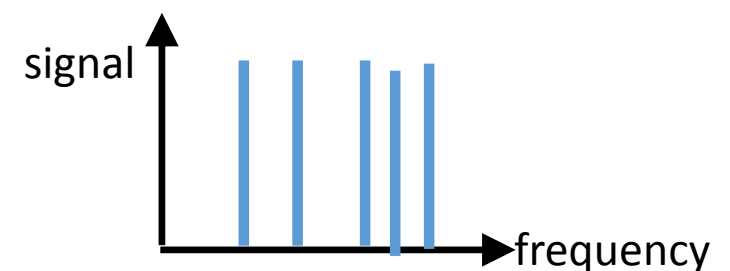
vs



Frequency Modulation

**35 48 18**

digital



Spread Spectrum

vs

vs

# Equations (mathematical MODELS) are your friends!

Building a homemade ultralight...where to start?

What will we need?

What motor power, wing area, etc?

1. Estimate flying weight: 70kg person+ 40kg wings+30kg motor/prop+60kg frame, fuel, misc → 200kg → 2000N
2. Want to cruise at 60 km/h (17 m/s) →  $W/S = 0.38V^2$  →  $S = 19\text{m}^2$
3. Glide ratio of 8 is reasonable for such an airplane, descent  $w = 2\text{m/s}$  →  $P = Ww = 4000\text{W}$  to stay level, if want to climb at 3m/s need another 6000W → 10000W (14 Hp) total
4. Best prop efficiency is around 50% → need a 28 Hp motor

# Numbers matter!

Global warming, energy/economics policy, business → need reliable, quantitative estimates to make good decisions

The economics of flight:

Car with 4 people: 30 miles per gallon, 55 mph speed → 0.008 gallon per passenger mile

Boeing 747 with 400 people and cargo (total=115,000 lbs) ~520 people+luggage: 0.18 miles per gallon (burn 3000 gallons per hour!), 560 mph speed  
→ 0.011 gallon per passenger mile

40% increase in fuel but 10 times the speed!

In transportation industry, time matters: ocean liner produces 200 million passenger miles per year, high speed train produces 250 million passenger miles per year, and Boeing 747 produces 750 million passenger miles per year

Take Home message: Radio control flying is exciting, interesting, fun and can teach us a lot about science and technology

