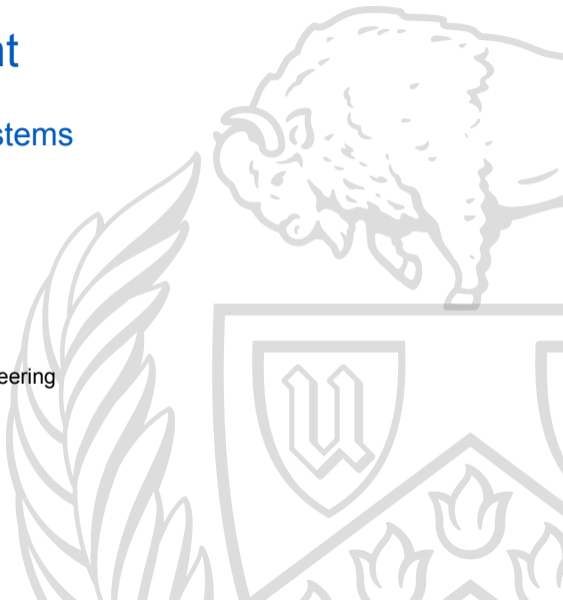


# Byzantine Agreement

CSE 486/586: Distributed Systems

Ethan Blanton

Department of Computer Science and Engineering  
University at Buffalo



# Byzantine Failures

We briefly discussed **Byzantine failures**<sup>1</sup> previously.

This is when a process displays **different behavior** to different observers.

*E.g.*, perhaps process  $p_1$ :

- Says “my value is 0” to process  $p_2$
- Says “my value is 1” to process  $p_3$
- **Fails to respond entirely** to process  $p_4$

This is often **harder to account for** than simpler failures.

---

<sup>1</sup>Sometimes “Byzantine faults”

# Etymology

The term “Byzantine” was coined by Lamport *et al.* [1, 2].

*I have long felt that, because it was posed as a cute problem about philosophers seated around a table, Dijkstra's dining philosopher's problem received much more attention than it deserves. [I believed that ... Reaching Agreement in the Presence of Faults [3]] was very important and deserved the attention of computer scientists. The popularity of the dining philosophers problem taught me that the best way to attract attention to a problem is to present it in terms of a story.*

He has used this tactic [several times since](#).

# Failures

All failures we have previously considered were **consistent**.

A process is either failed, **or it is not**.

A failed process **may give the wrong value**, but it does so **consistently**.

Most of our failures have been **fail-stop**.

# Byzantine Failure

With Byzantine failure, a process may **appear differently**:

- To different processes
- At different times

It cannot (necessarily) be detected by a **failure detector**.

It could be caused by (for example):

- A bad bit in memory that reads inconsistently
- A program bug
- **A malicious process**

# Byzantine Adversaries

A Byzantine failure **may be a malicious adversary**.

In this case, the adversary can **give any answer to any process**.

It could send **the worst possible response** in every case!

A Byzantine attacker can be **very hard to defeat**.

# Byzantine Generals

The **Byzantine Generals** problem is set up as follows:

- Several armies are besieging a city, each led by a general.
- If enough of them attack at once, they will be victorious.
- If too few of them attack, they will fail.
- They can send **reliable and timely** messages to each other.
- **Some of the generals might be traitors.**

How, and under what circumstances, can they agree to attack?

# The Problem

This is a **consensus** problem.

Assume that one general is the **commander**.

The other generals are **lieutenants**.

We want these properties:

- All loyal lieutenants **execute the same order**.
- If the commander is loyal,  
**all loyal lieutenants** follow the commander's orders.



# The Model

The messaging model is **synchronous**.

Messages **cannot be forged**:

- Generals know if a message does not arrive
- Generals know who sent a message
- The message is received as sent

Loyal generals **always behave correctly**.

Traitorous generals can lie, and **can collude**.

# Four Generals

Assume there are **four generals**, with **one traitor**.

There is a simple solution to this problem.

It is **closely related** to synchronous consensus with  $f = 1$ .

It proceeds in two rounds.

# The Rounds

Round 1:

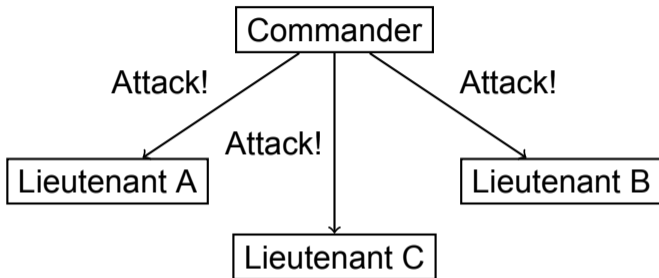
- The general tells every lieutenant their orders.

Round 2:

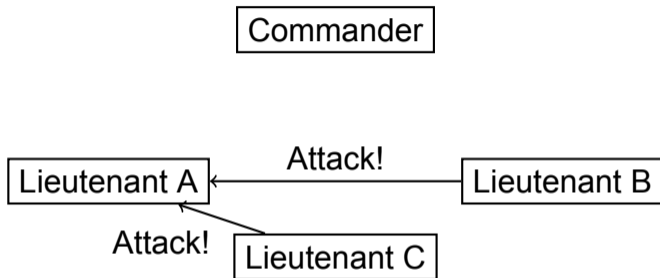
- Every lieutenant tells every other lieutenant their orders.

After round 2, every lieutenant takes the **plurality** of orders.

# Example



# Example



# Introducing ...a Traitor

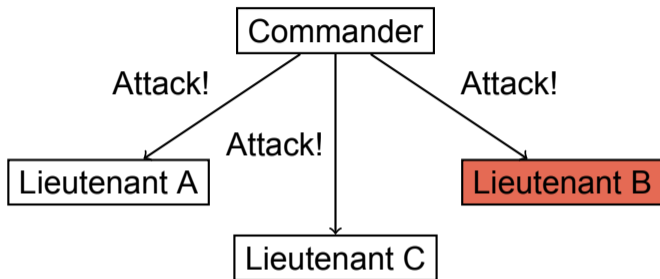
What if one general is a **traitor**?

There are two cases:

- One lieutenant is a traitor
- The commander is a traitor

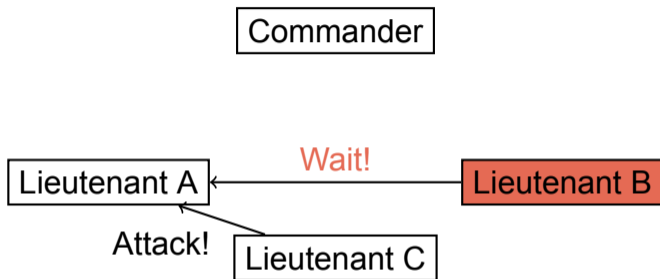
Let's look at each case.

# Traitorous Lieutenant



The general sends messages as in the first example.

# Traitorous Lieutenant



Lieutenant B is a traitor, and **changes the message**.



# Traitorous Lieutenant

Commander

Lieutenant A

Lieutenant B

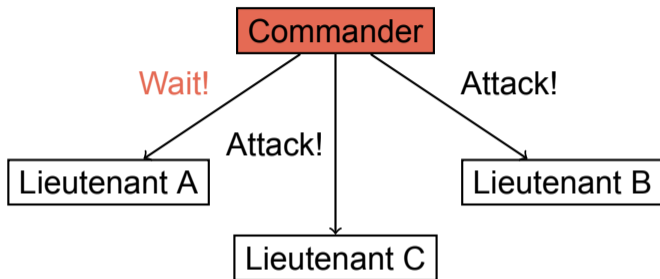
Lieutenant C

Lieutenant A received: { Attack, Attack, Wait }

Lieutenant A attacks!

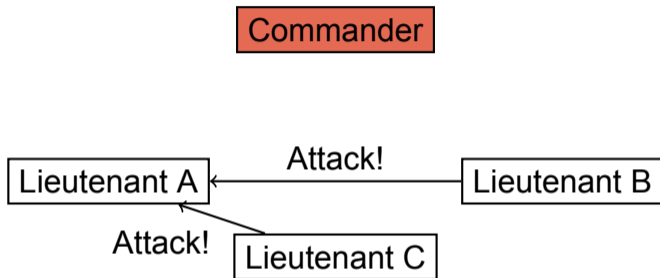
(It is **super effective!**)

# Traitorous Commander



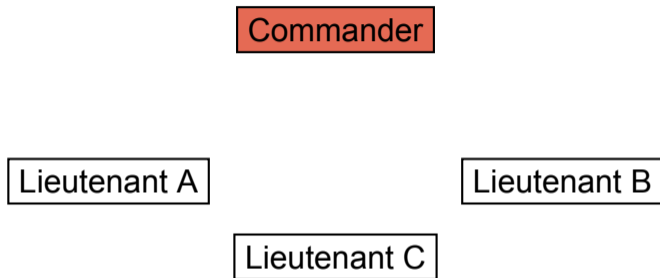
The general sends **mixed messages**.

# Traitorous Commander



Lieutenants B and C repeat what they heard faithfully.

# Traitorous Commander



Lieutenant A received: { Wait, Attack, Attack }

Lieutenant A attacks along with Lieutenants B and C.

# N Generals

To extend this to  $n$  generals with no more than  $m$  traitors:

Round 1 remains the same.

There are  $m + 1$  additional rounds with **particular rules**.

Again, this is like synchronous consensus with  $f$  failures!

# The Magic of $1/3$

Assume that there are  $n$  generals, and  $m$  are traitors.

Under this model,  $2m + 1$  generals **must be loyal**.

If fewer than  $2m + 1$  generals are loyal, loyal generals may not all take the same action.

Thus, **strictly more than  $1/3$**  of the generals must be loyal!

Interestingly, **the loyalty of the commander doesn't matter**.

# Three Generals

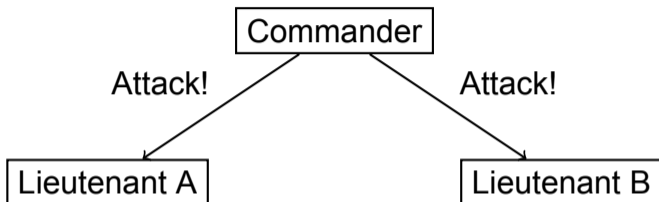
Consider three generals with one traitor.

It is **easy to show** that agreement is impossible.

We have **the same two cases** to consider:

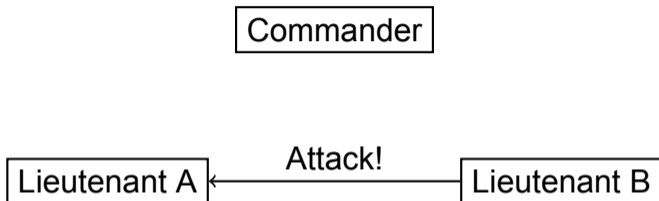
- One of the lieutenants is a traitor
- The commanding general is a traitor

# A Loyal Group

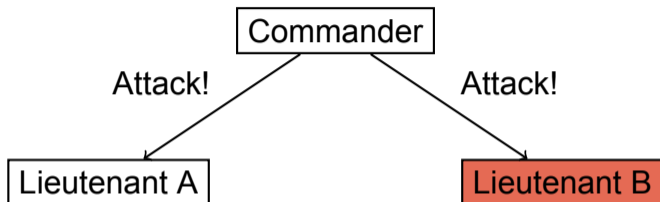




# A Loyal Group

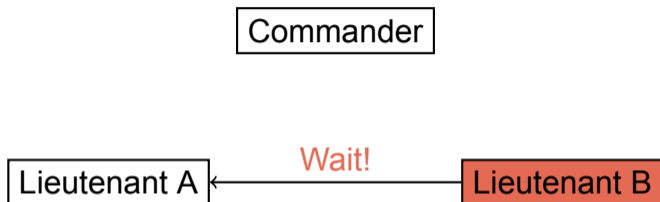


# A Traitorous Lieutenant



Again, the general proceeds as before.

# A Traitorous Lieutenant



Lieutenant B **changes the orders.**

# A Traitorous Lieutenant

Commander

Lieutenant A

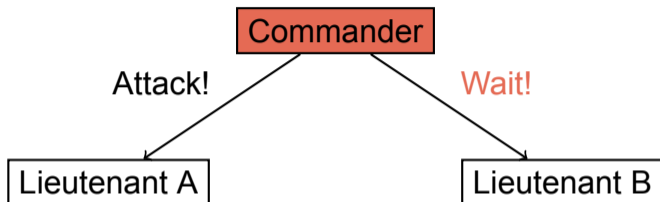
Lieutenant B

Lieutenant A received: { Attack, Wait }

Now what?

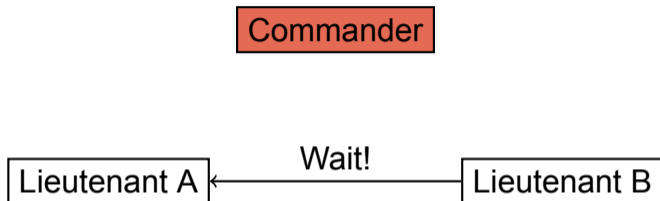
Why can't Lieutenant A simply believe the commander?

# A Traitorous Commander



The general sends a different message to Lieutenant B.

# A Traitorous Commander



Lieutenant B repeats in good faith.

# A Traitorous Commander

Commander

Lieutenant A

Lieutenant B

Lieutenant A received: { Attack, Wait }

This is **exactly the same** as the traitorous Lieutenant B!

# Generalizing to $3m + 1$

This can be generalized<sup>2</sup> to  $3m$  generals.

By contradiction:

1. Assume a solution for  $3m$  or fewer generals
2. Divide the loyal generals into two groups, roughly equally
2. Cause the traitorous generals to work in concert
2. Now you have **three simulated generals**
3. ???
4. **Profit** by solving the three generals problem!

---

<sup>2</sup>See what I did there?



# Summary

- Byzantine failures **present differently** in different circumstances
- Storytelling gets you published
- Consensus can be reached **even with Byzantine failure** (in a synchronous system)
- More than  $2/3$  of processes must be honest to achieve this

# References I

## Optional Readings

- [1] Leslie Lamport. *The Writings of Leslie Lamport: The Byzantine Generals Problem*. URL:  
<http://lamport.azurewebsites.net/pubs/pubs.html#byz>.
- [2] Leslie Lamport, Robert Shostak, and Marshall Pease. “The Byzantine Generals Problem”. In: *ACM Transactions on Programming Languages and Systems* 4.3 (July 1982), pp. 382–401. DOI: 10.1145/357172.357176. URL:  
<http://lamport.azurewebsites.net/pubs/byz.pdf>.

## References II

- [3] Marshall Pease, Robert Shostak, and Leslie Lamport. “Reaching Agreement in the Presence of Faults”. In: 27.2 (Apr. 1980), pp. 228–234. DOI: 10.1145/322186.322188. URL: <http://lamport.azurewebsites.net/pubs/reaching.pdf>.

Copyright 2021 Ethan Blanton, All Rights Reserved.

Reproduction of this material without written consent of the author is prohibited.

To retrieve a copy of this material, or related materials, see <https://www.cse.buffalo.edu/~eblanton/>.