CSE 4/587
Data Intensive Computing

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Word Co-Occurrence
Announcements

- HW 1 released due Monday 4/3
  - No late submissions will be accepted
Additional References for Today


An online version of this text is also available through UB Libraries since UB subscribes to Morgan and Claypool Publishers.

Online version available at:
http://lintool.github.com/MapReduceAlgorithms/index.html
Dealing with Intermediate Data

- In distributed applications (i.e., MapReduce), one of the most important parts of synchronization is **exchange of intermediate results**
  - This usually involves communication of data over the network
  - In Hadoop/MR intermediate results are also written to disk
- Network and disk latencies are much more expensive compared to most other operations

*Reducing the amount of intermediate data translates to better performance and efficiency*
Local Aggregation

● One way to address the intermediate data problem is to perform local aggregation **before** the data gets written to disk/sent over the network.

● Two basic approaches:
  ○ Combiners
  ○ In-Mapper Combining
class Mapper
    method Map(docid id, doc d)
        for all term t in d do
            emit(t, 1)
    
class Reducer
    method Reduce(term t, int \[c_1, c_2, \ldots\])
        sum ← 0
        for all int c in \[c_1, c_2, \ldots\] do
            sum ← sum + c
        emit(t, sum)
Combiners

- Process to aggregate the output of Mappers
- Can be thought of as "mini-reducers"
- Must preserve the types of <key, value> pairs
  - Must take the output from Mapper as its input, and output something in the same form for the reducers
- It is a completely **optional** optimization in the eyes of MapReduce
  - It may not be run, it may be run once, it may be run many times
  - **Correctness cannot rely on the Combiner**
Combiners

- Process to aggregate the output of Mappers
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*For WordCount, we can use the same Reducer class for the Combiner*
In-Mapper Combining

Another option is to do local aggregation in the Mapper itself.

Makes the mapper more complex, but...

```java
class Mapper
    method Map(docid id, doc d)
        for all term t in d do
            emit(t, 1)
```
Another option is to do local aggregation in the Mapper itself. Makes the mapper more complex, but also gives direct control over aggregation.

```java
class Mapper
    method Map(docid id, doc d)
        for all term t in d do
            emit(t, 1)
```

In-Mapper Combining

Another option is to do local aggregation in the Mapper itself.

Makes the mapper more complex, but...

...also gives direct control over aggregation.

class Mapper
  method Map(docid id, doc d)
    map ← new AssociativeArray
    for all term t in d do
      map[t] ← map[t] + 1
    for all term t in map do
      emit(t, map[t])
Another option is to do local aggregation in the Mapper itself.

Makes the mapper more complex, but...

...also gives direct control over aggregation.

class Mapper
method Map(docid id, doc d)
    map ← new AssociativeArray
for all term t in d do
    map[t] ← map[t] + 1
for all term t in map do
    emit(t, map[t])

Store intermediate result.
Another option is to do local aggregation in the Mapper itself.

Makes the mapper more complex, but...

...also gives direct control over aggregation.

```java
class Mapper {
  method Map(docid id, doc d) {
    map ← new AssociativeArray
    for all term t in d do {
      map[t] ← map[t] + 1
    }
    for all term t in map do {
      emit(t, map[t])
    }
  }
}
```

Only emit after we've processed the whole input.
In-Mapper Combining

What if our mapper is run on multiple <key, value> pair inputs?
In-Mapper Combining

What if our mapper is run on multiple <key, value> pair inputs?

We can utilize the `initialize` and `close` methods of our mapper!
class Mapper
  method Initialize()
    map ← new AssociativeArray

  method Map(docid id, doc d)
    for all term t in d do
      map[t] ← map[t] + 1

  method Close()
    for all term t in map do
      emit(t, map[t])
class Mapper

method Initialize()
    map ← new AssociativeArray

method Map(docid id, doc d)
    for all term t in d do
        map[t] ← map[t] + 1

method Close()
    for all term t in map do
        emit(t, map[t])
In-Mapper Combining

```java
class Mapper {
    method Initialize()
        map ← new AssociativeArray
    method Map(docid id, doc d)
        for all term t in d do
            map[t] ← map[t] + 1
    method Close()
        for all term t in map do
            emit(t, map[t])
}
```

Create the AssociativeArray for intermediate aggregation before processing any data.

Don't emit and `<key, value>` pairs until after we've seen all of our input.
## Trade-Offs

<table>
<thead>
<tr>
<th>Combining</th>
<th>In-Mapper Aggregation</th>
</tr>
</thead>
<tbody>
<tr>
<td>+ Simple mapper code</td>
<td>+ More efficient aggregation</td>
</tr>
<tr>
<td>+ Let MapReduce manage the optimization</td>
<td>+ Direct control</td>
</tr>
<tr>
<td>- No direct control</td>
<td>- Scalability bottleneck requires memory management</td>
</tr>
<tr>
<td>- Overhead of generating intermediate ( &lt;k,v&gt; ) pairs</td>
<td>- No &quot;purity&quot; of functional programming</td>
</tr>
<tr>
<td></td>
<td>- May introduce ordering bugs</td>
</tr>
</tbody>
</table>
Correctness with Local Aggregation

**Example:** `<key, value>` pairs associate a string with a number, we want to compute the mean value for each key.

```
class Mapper
    method Map(str s, int i)
        emit(s, i)

class Reducer
    method Reduce(str s, int [i₁,i₂,...])
        sum ← 0; count ← 0
        for all int i in [i₁,i₂,...] do
            sum ← sum + i
            count ← count + 1
        avg = sum / count
        emit(t, avg)
```
Example: `<key, value>` pairs associate a string with a number, we want to compute the mean value for each key.

```java
class Mapper
    method Map(str s, int i)
        emit(s, i)

class Reducer
    method Reduce(str s, int [i₁, i₂, ...])
        sum ← 0; count ← 0
        for all int i in [i₁, i₂, ...] do
            sum ← sum + i
            count ← count + 1
        avg = sum / count
        emit(t, avg)

Can this reducer also be the combiner?
Correctness with Local Aggregation

**Observation:** \( \text{Mean}(1,2,3,4,5) \neq \text{Mean}(\text{Mean}(1,2),\text{Mean}(3,4,5)) \)

Count was associative and commutative, Mean is not!

*How can we write a combiner to do local aggregation?*
class Combiner:

    method Combine(str s, int \[i_1, i_2, ...\])
        sum ← 0; count ← 0;
        for all int i in \[i_1, i_2, ...\] do
            sum ← sum + i
            count ← count + 1
        emit(s, (sum, count)) // Emit a pair
Combiner Attempt #1

class Combiner
    method Combine(str s, int [i₁,i₂,...])
        sum ← 0; count ← 0;
        for all int i in [i₁,i₂,...] do
            sum ← sum + i
            count ← count + 1
        emit(s, (sum, count)) // Emit a pair

Will this work for local aggregation?
Combiners

- Process to aggregate the output of Mappers
- Can be thought of as "mini-reducers"
- Must preserve the types of <key, value> pairs
  - Must take the output from Mapper as its input, and output something in the same form for the reducers
- It is a completely **optional** optimization in the eyes of MapReduce
  - It may not be run, it may be run once, it may be run many times
  - *Correctness cannot rely on the Combiner*
Combiner Attempt #2

```python
class Mapper:
    method Map(str s, int i):
        emit(s, (i, 1))

class Combiner:
    method Combine(str s, pair [(s, c), ...]):
        sum ← 0; count ← 0
        for all pair (s, c) in [(s, c), ...] do
            sum ← sum + s
            count ← count + c
        emit(t, (sum, count))

class Reducer:
    method Reduce(str s, pair [(s, c), ...]):
        sum ← 0; count ← 0
        for all pair (s, c) in [(s, c), ...] do
            sum ← sum + s
            count ← count + c
        avg = sum / count
        emit(t, avg)
```
Combiner Attempt #2

class Mapper
    method Map(str s, int i)
        emit(s, (i, 1))

class Combiner
    method Combine(str s, pair [(s_1, c_1), ...])
        sum ← 0; count ← 0
        for all pair (s, c) in [(s_1, c_1), ...] do
            sum ← sum + s
            count ← count + c
        emit(s, (sum, count))

    Outputs pairs

class Reducer
    method Reduce(str s, pair [(s_1, c_1), ...])
        sum ← 0; count ← 0
        for all pair (s, c) in [(s_1, c_1), ...] do
            sum ← sum + s
            count ← count + c
        avg = sum / count
        emit(t, avg)

    Inputs are pairs

Inputs AND outputs are pairs
In-Mapper Aggregation

```java
class Mapper {
    method Initialize()
        sumMap ← new AssociativeArray
        countMap ← new AssociativeArray
    method Map(str s, int i)
        sumMap[s] ← sumMap[s] + i
        countMap[s] ← countMap[s] + 1
    method Close()
        for all key in sumMap do
            emit(key, (sumMap[key], countMap[key]))
}
```
Word Co-Occurrence

- Word Co-Occurrence counts the number of times pairs of words occur in the same context, i.e., a sentence.
- Involves constructing an $N \times N$ matrix, $M$, where $N$ is the total number of words in the vocabulary.
  - $M_{ij}$ is the number of times words $w_i$ and $w_j$ occurred in the same context.
  - Very simple to compute...if the matrix fits in memory.
Word Co-Occurrence

Can come up in a number of different domains, not just in text processing

Some Examples:
- Information retrieval, NLP, text mining, etc
- Co-Occurrence in consumer purchases (can help with inventory mgmt)
- Finding associations between recurring financial transactions
class Mapper
  method Map(docid id, doc d)
    for all w in d do
      for all u in Neighbors(w) do
        emit((w,u), 1)

class Reducer
  method Reduce(pair p, int[] cnts)
    sum ← 0
    for all c in cnts do
      sum ← s + c
    emit(p, sum)
The key in our <key,value> pair is a pair of words. Represents a single entry in our co-occurrence matrix.
class Mapper
    method Map(docid id, doc d)
        for all w in d do
            for all u in Neighbors(w) do
                emit((w, u), 1)

The key in our <key,value> pair is a pair of words. Represents a single entry in our co-occurrence matrix.

class Reducer
    method Reduce(pair p, int[] cnts)
        sum ← 0
        for all c in cnts do
            sum ← s + c
        emit(p, sum)

How many possible keys are there? Any issues with this method?
What else could we use as a key?
What else could we use as a key?

Could we use a single word as a key?
What else could we use as a key?

Could we use a single word as a key?

If so, what would be the value?
class Mapper
    method Map(docid id, doc d)
        for all w in d do
            map ← new AssociativeArray
            for all u in Neighbors(w) do
                map[u] ← map[u] + 1
            emit(w, map)
    
class Reducer
    method Reduce(str w, stripes)
        map ← new AssociativeArray
        for all s in stripes do
            Sum(map, s)
        emit(w, map)
**Word Co-Occurrence - Stripes Method**

**Class Mapper**

```java
class Mapper {
  method Map(docid id, doc d) {
    for all w in d do {
      map ← new AssociativeArray
      for all u in Neighbors(w) do {
        map[u] ← map[u] + 1
      }
      emit(w, map)
    }
  }
}
```

**Class Reducer**

```java
class Reducer {
  method Reduce(str w, stripes) {
    map ← new AssociativeArray
    for all s in stripes do {
      Sum(map, s)
    }
    emit(w, map)
  }
}
```

Build and emit a map containing the counts of all neighbors of w.
class Mapper
method Map(docid id, doc d)
    for all w in d do
        map ← new AssociativeArray
        for all u in Neighbors(w) do
            map[u] ← map[u] + 1
        emit(w, map)

Build and emit a map containing the counts of all neighbors of w

class Reducer
method Reduce(str w, stripes)
    map ← new AssociativeArray
    for all s in stripes do
        Sum(map, s)
    emit(w, map)

Combine all maps for w into one map and output it
Analysis of Stripes

+ Stripes generate far fewer <key, value> pairs
+ Stripes are much more compact (the pairs approach duplicates the left word in the pair for every pair)
+ Fewer and shorter keys means less sorting
+ Better for local aggregation
- Values are larger and more complex with more serialization overhead
- Scalability concerns similar to In-Mapper combining (memory overflow)
Pairs vs Stripes in General

In a pairs approach, each key corresponds to a single entry of our matrix.

In a stripes approach, each key corresponds to a single row of our matrix.

We can also aim to find a middle ground somewhere between the two extremes.
Local Aggregation

- Both combiners and In-Mapper combining can be used with either the pairs or stripes method
  - The pairs method has less opportunity for combining (it is less likely to find many occurrences of a specific pair of words)
  - The stripes method may run into scalability issues as the maps get larger
Performance study from Lin and Dyer Chapter 3

Figure 3.10: Running time of the “pairs” and “stripes” algorithms for computing word co-occurrence matrices on different fractions of the APW corpus. These experiments were performed on a Hadoop cluster with 19 slaves, each with two single-core processors and two disks.
Relative Co-Occurrence Problem

- Individual words occur with different frequency.
  - In English, we expect to come across "the" much more often than "zebra"
- Using absolute counts can be deceiving – more frequent words may have a higher co-occurrence count simply due to being more common
  - "the" and "stripe" may have more co-occurrences than "stripe" and "zebra" simply because "the" is way more common than "zebra"

*How can we determine the "relative" co-occurrence?*
Relative Co-Occurrence Problem

\[ f(w_j | w_i) = \frac{N(w_i, w_j)}{\sum_{w'} N(w_i, w')} \]
Relative Co-Occurrence Problem

\[ f(w_j | w_i) = \frac{N(w_i, w_j)}{\sum_{w'} N(w_i, w')} \]

Number of times \( w_i \) co-occurs with \( w_j \)
Relative Co-Occurrence Problem

\[ f(w_j | w_i) = \frac{N(w_i, w_j)}{\sum_{w'} N(w_i, w')} \]

- Number of times \( w_i \) co-occurs with \( w_j \)
- Number of times \( w_i \) co-occurs with anything else
Relative Co-Occurrence Problem

\[ f(w_j \mid w_i) = \frac{N(w_i, w_j)}{\sum_{w'} N(w_i, w')} \]

Number of times \( w_i \) co-occurs with \( w_j \)

Number of times \( w_i \) co-occurs with anything else

This is called the **marginal**
Relative Co-Occurrence Problem

- Computing relative co-occurrence with stripes is trivial
  - Reducer can sum all counts for a particular key to get the **marginal**
Relative Co-Occurrence Problem

- Computing relative co-occurrence with stripes is trivial
  - Reducer can sum all counts for a particular key to get the marginal

*Can we compute relative co-occurrence with the pairs approach?*
Reducer-Side Aggregation

- The reducer in the pairs method reduces single pairs at a time
  - Just having counts for a single pair is not enough to compute relative co-occurrence, we can't compute the **marginal**
Reducer-Side Aggregation

- The reducer in the pairs method reduces single pairs at a time
  - Just having counts for a single pair is not enough to compute relative co-occurrence, we can't compute the **marginal**
- Just like the Mapper, our Reducers can preserve state across calls to `Reduce(...)`, by using `Initialize()` and `Close()`
  - To do this we need a few modifications...
Reducer-Side Aggregation

Given the following co-occurrence pairs, what assumptions do we need in order to do reducer side aggregation on, for example, the word dog?

(dog, aardvark), (dog, zebra), (dog, apple), (cat, tail), (dog, fur), (fly, banana), (dog, banana), ...
Reducer-Side Aggregation

Given the following co-occurrence pairs, what assumptions do we need in order to do reducer side aggregation on, for example, the word dog?

(dog, aardvark), (dog, zebra), (dog, apple), (cat, tail), (dog, fur), (fly, banana), (dog, banana), ...

1. We need to ensure that all pairs starting with dog go to the same reducer.

Reducer-Side Aggregation

Given the following co-occurrence pairs, what assumptions do we need in order to do reducer side aggregation on, for example, the word dog?

(dog, aardvark), (dog, zebra), (dog, apple), (cat, tail), (dog, fur), (fly, banana), (dog, banana), ...

1. We need to ensure that all pairs starting with dog go to the same reducer.
2. We need to be able to tell when we have reduced all the dog pairs.
Reducer-Side Aggregation

Given the following co-occurrence pairs, what assumptions do we need in order to do reducer side aggregation on, for example, the word dog?

(dog, aardvark), (dog, zebra), (dog, apple), (cat, tail), (dog, fur), (fly, banana), (dog, banana), ...

1. We need to ensure that all pairs starting with dog go to the same reducer.
2. We need to be able to tell when we have reduced all the dog pairs.

This can be accomplished with a custom partitioner/sort order.
Reducer-Side Aggregation

(dog, aardvark),
(dog, apple),
(dog, banana),
(dog, fur),
...
(dog, zebra),
(door, open),
...
Reducer-Side Aggregation

(dog, aardvark),
(dog, apple),
(dog, banana),
(dog, fur),
...
(dog, zebra),
(door, open),
...

If we sort our keys by the first word, we know as soon as we encounter (door, open) we are done with all of the dog keys.
class Reducer

method Initialize()
    currWord ← ""
    map ← new AssociativeArray
method Reduce(pair p, int[] cnts)
    if pair.first != currWord then
        computeAndEmitRelative()
        currWord ← pair.first
        map ← new AssociativeArray
    for all c in cnts do
        map[pair.second] = map[pair.second] + c
Reducer-Side Aggregation

class Reducer
    method Initialize()
        currWord ← ""
        map ← new AssociativeArray
    method Reduce(pair p, int[] cnts)
        if pair.first != currWord then
            computeAndEmitRelative()
            currWord ← pair.first
            map ← new AssociativeArray
        for all c in cnts do
            map[pair.second] = map[pair.second] + c

Since we sorted based on the first word in the pair, we can assume all keys with the same first word will appear in a row...once we encounter a different word, we can output the result for our previous word
Reducer-Side Aggregation

class Reducer

method Initialize()
    currWord ← ""
    map ← new AssociativeArray

method Reduce(pair p, int[] cnts)
    if pair.first != currWord then
        computeAndEmitRelative()
        currWord ← pair.first
        map ← new AssociativeArray
        for all c in cnts do
            map[pair.second] = map[pair.second] + c

The map holds the total number of co-occurrences with our current word
Reducer-Side Aggregation

```python
class Reducer:
    method computeAndEmitRelative()
        marginal ← 0
        for all key in map do
            marginal ← marginal + map[key]
        for all key in map do
            N ← map[key]
            relative = N / (marginal - N)
        emit(currWord, relative)
```
Reducer-Side Aggregation

class Reducer
  method computeAndEmitRelative()
    marginal ← 0
    for all key in map do
      marginal ← marginal + map[key]
    for all key in map do
      N ← map[key]
      relative = N / (marginal - N)
      emit(currWord, relative)

Compute marginal across all words co-occurring with our current word
Reducer-Side Aggregation

class Reducer

method computeAndEmitRelative()
    marginal ← 0
    for all key in map do
        marginal ← marginal + map[key]
    for all key in map do
        N ← map[key]
        relative = N / (marginal - N)
        emit(currWord, relative)

Compute relative co-occurrence for all words
Scalability

**Observation:** This method has the same scalability issues as the stripes method In-Mapper aggregation...as our vocabulary gets bigger, the map may not fit in memory

...but we need it to compute the marginal...or do we?
Order Inversion

- Can we compute the marginal \textit{before} we compute the individual co-occurrences?
Order Inversion

- Can we compute the marginal \textbf{before} we compute the individual co-occurrences? \textbf{YES!}
- Emit to a special pair that contains total occurrences of a word
  - ie: (dog, *) would count co-occurrences of dog with \textbf{any} word
  - In our sorting, make sure this pair comes before all other dog pairs

\[
<(\text{dog,*}),[10,2,147]>, \langle \text{dog, aardvark},[2,1]\rangle, \ldots, \langle \text{dog, zebra}, [3,1,1]\rangle, \langle \text{cat,*},[31,491,6]\rangle, \ldots
\]
Order Inversion

- Can we compute the marginal before we compute the individual co-occurrences? **YES!**
- Emit to a special pair that contains total occurrences of a word
  - i.e: (dog, *) would count co-occurrences of dog with any word
  - In our sorting, make sure this pair comes before all other dog pairs

\[<(\text{dog}, \text{*}), [10, 2, 147]>\], \[<(\text{dog}, \text{aardvark}), [2, 1] >\], ..., \[<(\text{dog}, \text{zebra}), [3, 1, 1] >\], \[<(\text{cat}, \text{*}), [31, 491, 6] >\], ...

This is the first "dog" pair our reducer will encounter, and can be used to compute the marginal for dog before we compute the individual co-occurrences for dog. This is called **order inversion**.
class Mapper
    method Map(docid id, doc d)
        for all w in d do
            for all u in Neighbors(w) do
                emit((w,u), 1)
                emit((w,*), 1)

class Reducer
    method Initialize()
        marginal ← 0
    method Reduce(pair p, int[] cnts)
        N ← 0
        for all c in cnts do
            N ← N + c
        if p.second == * then
            marginal ← N
        else
            emit(p, N / (marginal - N))
class Mapper
    method Map(docid id, doc d)
        for all w in d do
            for all u in Neighbors(w) do
                emit((w,u), 1)
                emit((w,*), 1)

Special pair can be used to compute the marginal and indicates we are starting a new word in the reducer

class Reducer
    method Initialize()
        marginal ← 0
    method Reduce(pair p, int[] cnts)
        N ← 0
        for all c in cnts do
            N ← N + c
        if p.second == * then
            marginal ← N
        else
            emit(p, N / (marginal - N))