

Lecture 11

CSE 331

Feb 19, 2020

Graphs

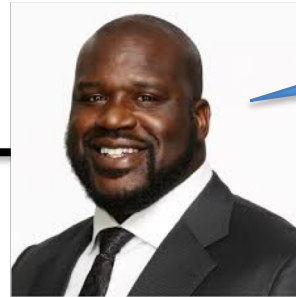
Representation of relationships between pairs of entities/elements

Entities:
NBA players

Relationship: Played together



kobe bryant



shaq o'neal



lebron james



anthony davis



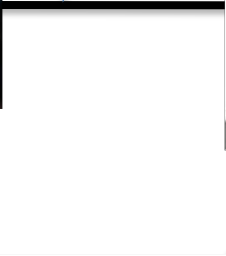
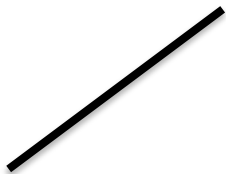
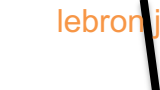
kevin love



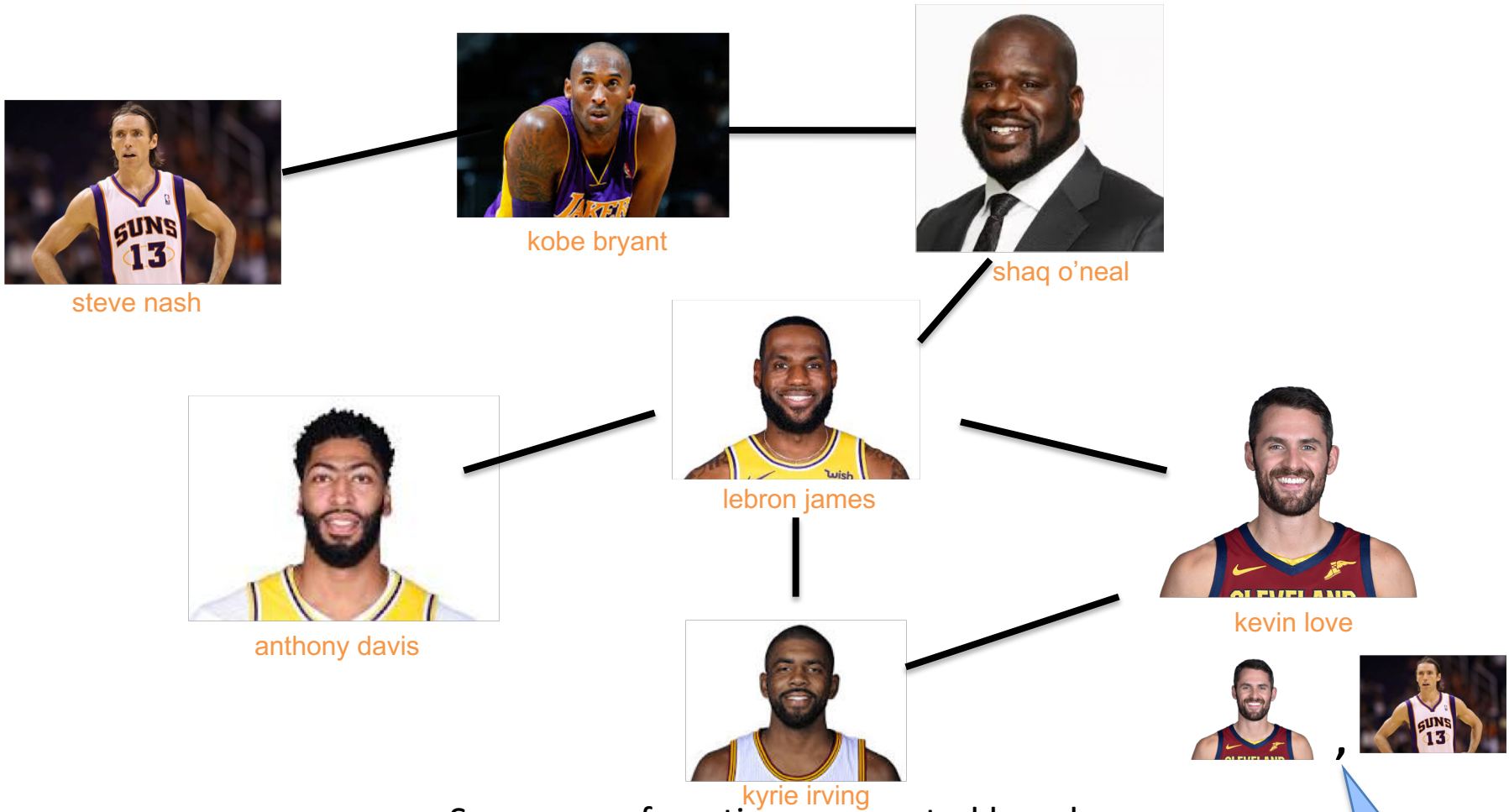
kyrie irving

Edge

Vertex/Node



Paths



Sequence of vertices connected by edges



Path length 4

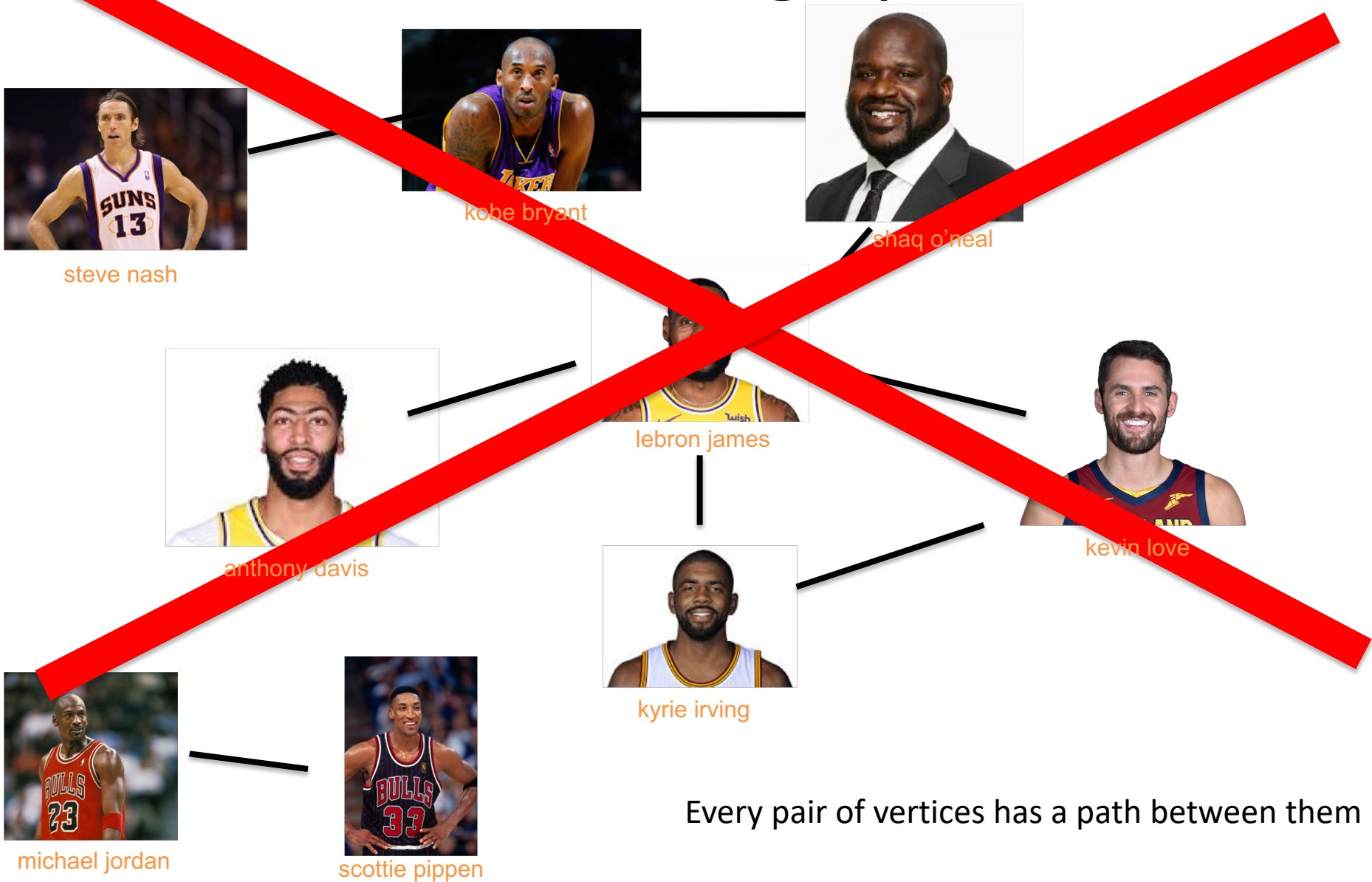
Connected

Connectivity

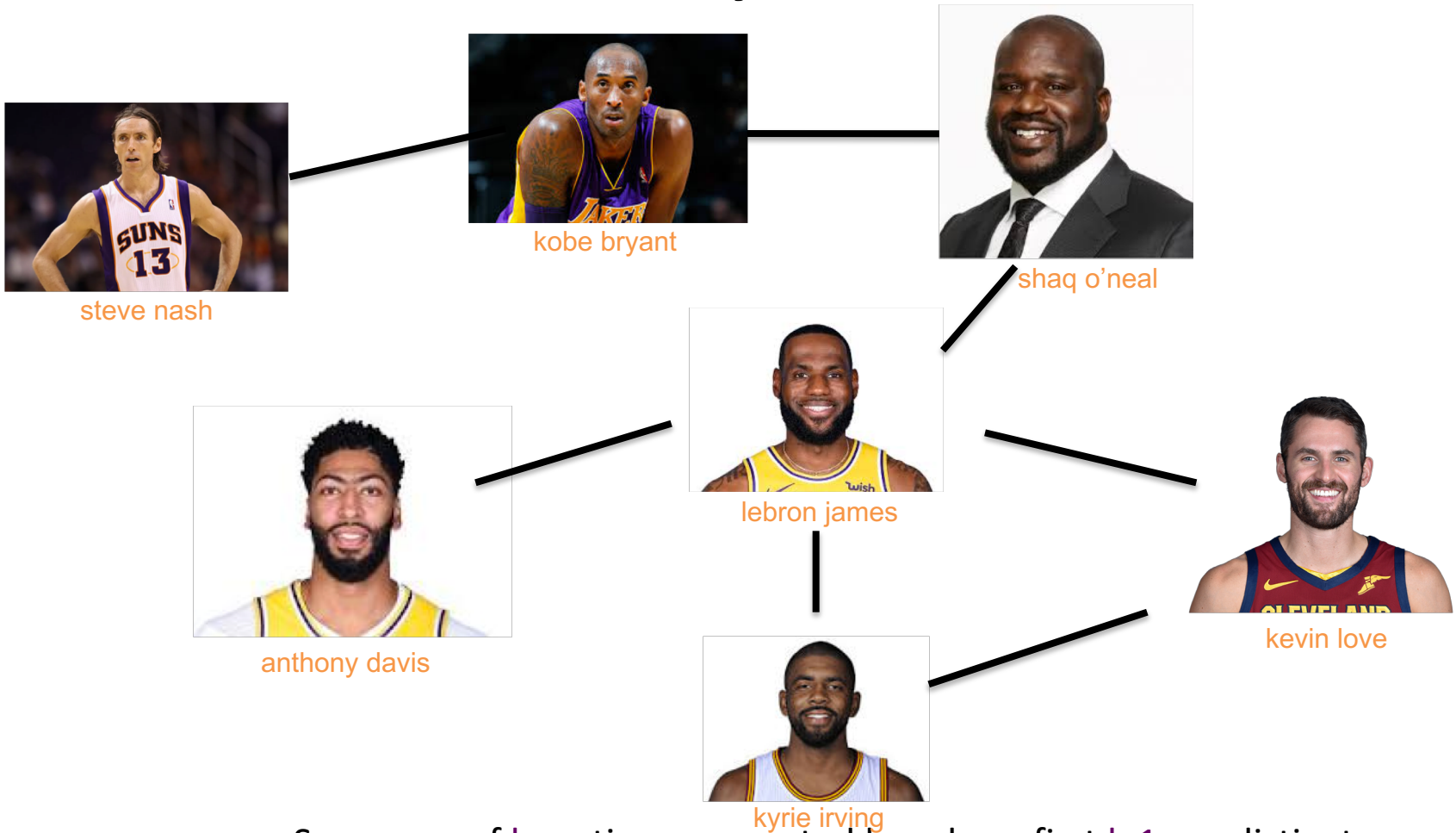
u and w are connected iff there is a path between them

A graph is connected iff all pairs of vertices are connected

Connected graphs



Cycles

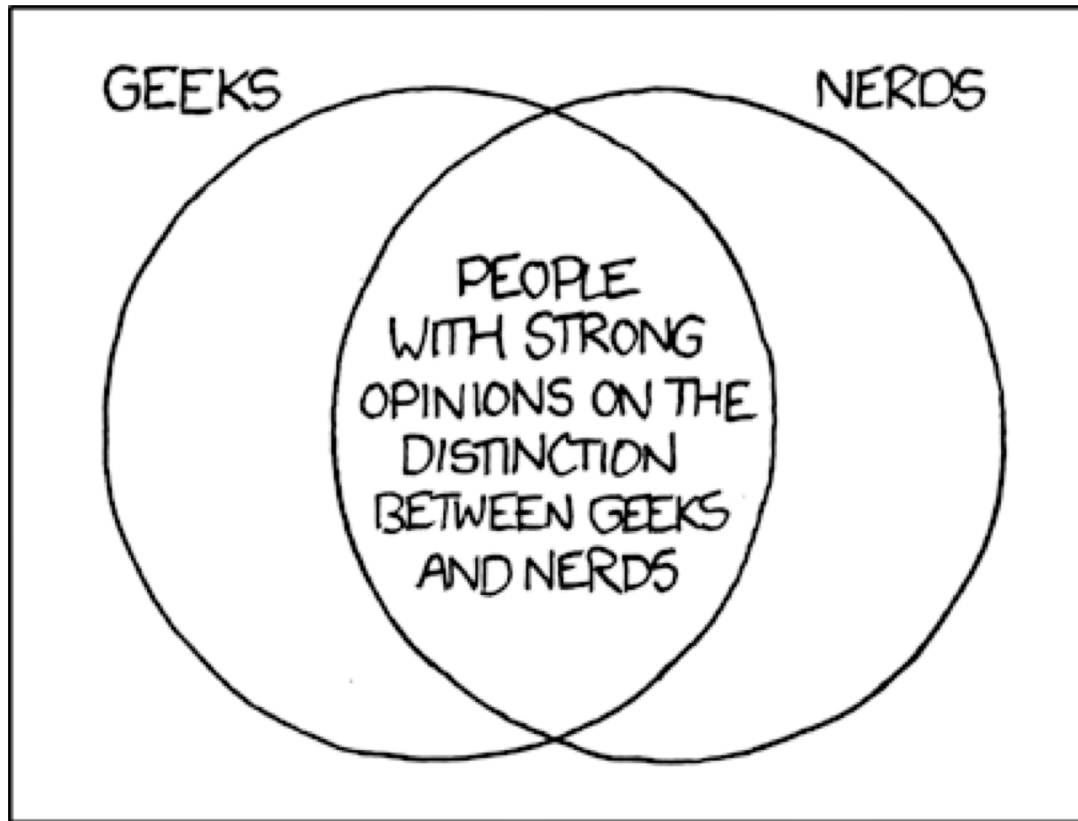


Sequence of k vertices connected by edges, first $k-1$ are distinct



Questions?

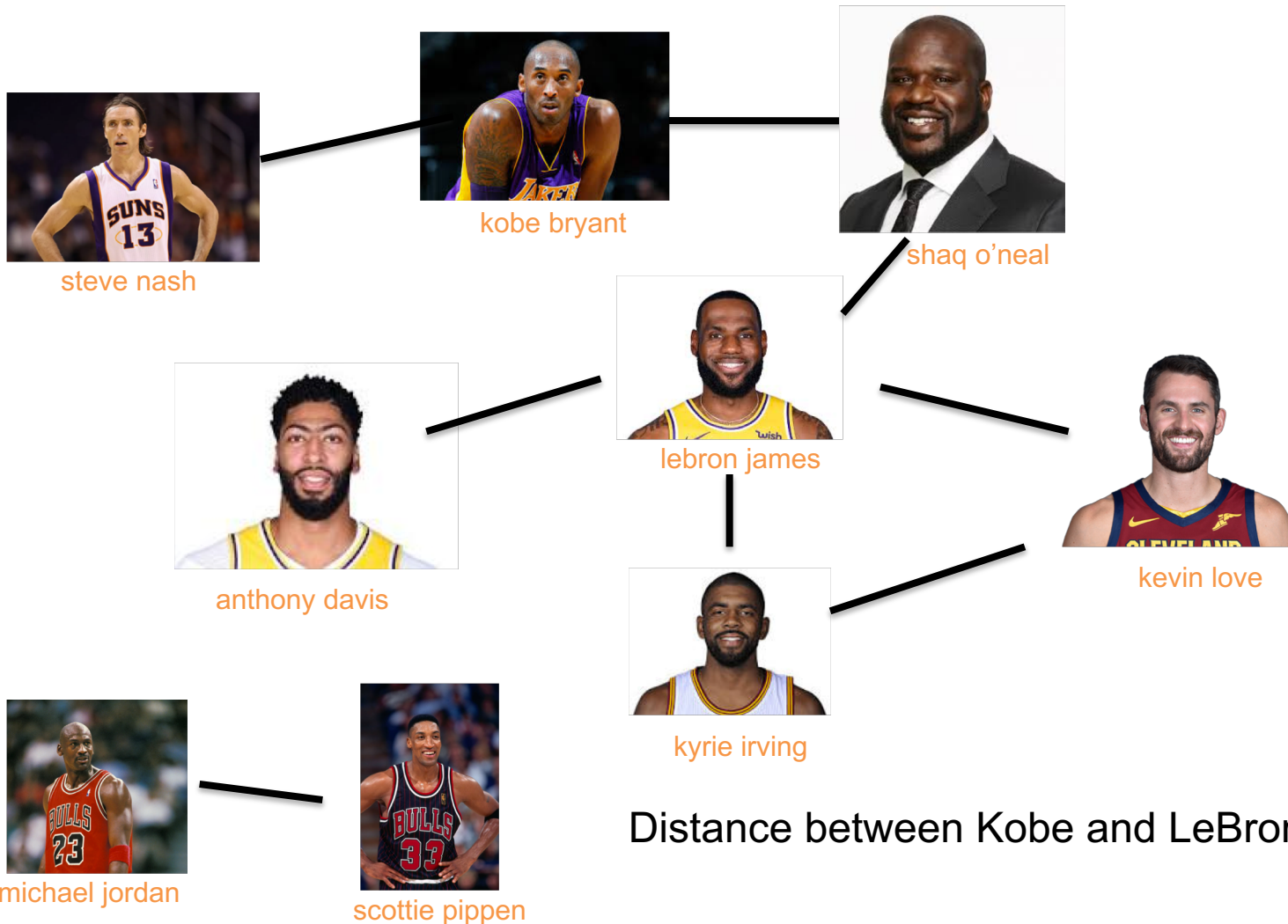
Formally define everything



http://imgs.xkcd.com/comics/geeks_and_nerds.png

Distance between **u** and **v**

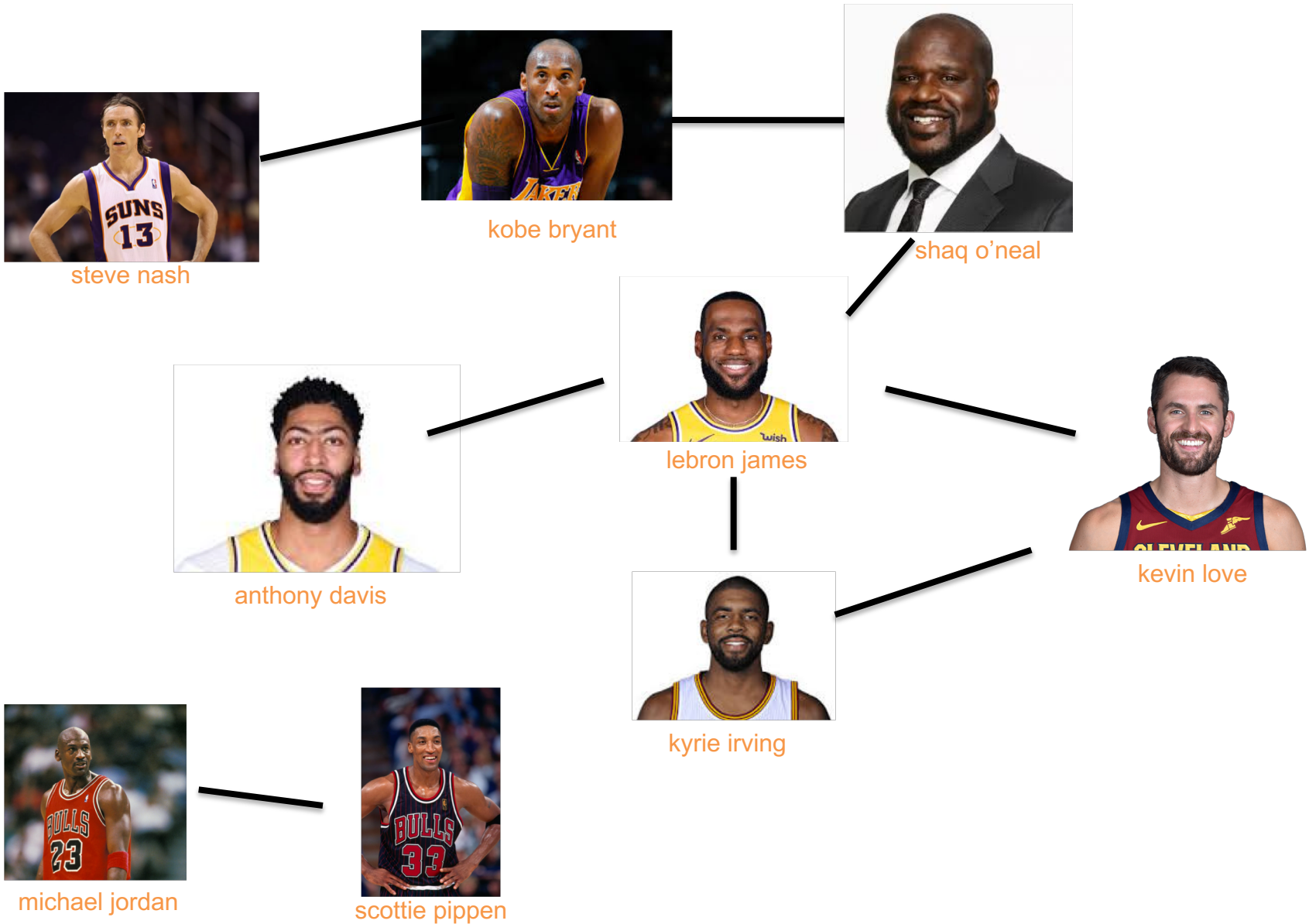
Length of the shortest length path between **u** and **v**



Distance between Kobe and LeBron? **2**

Tree

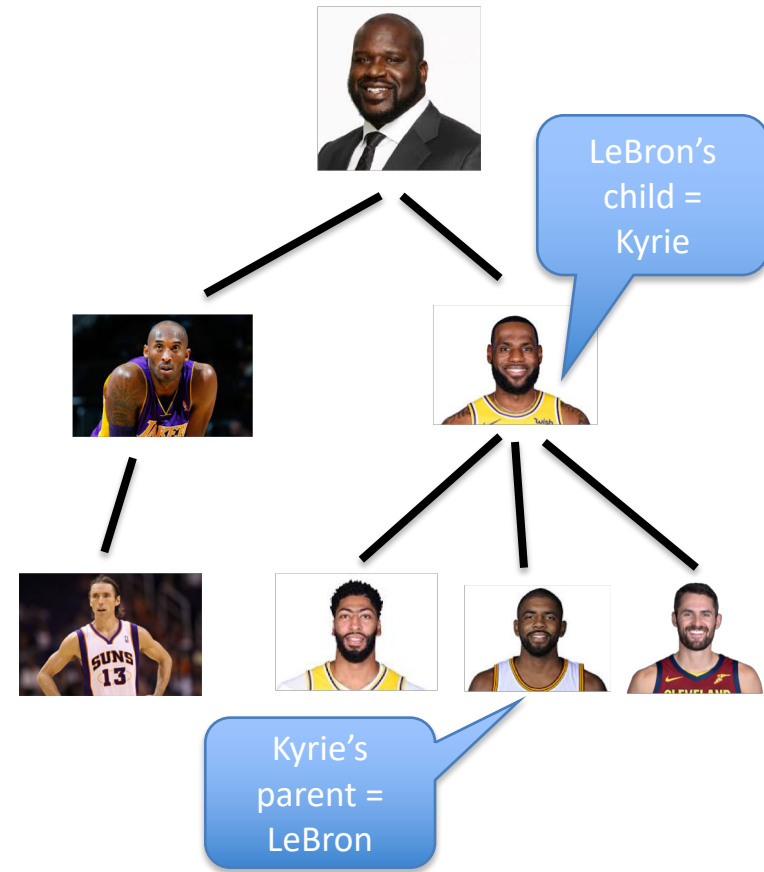
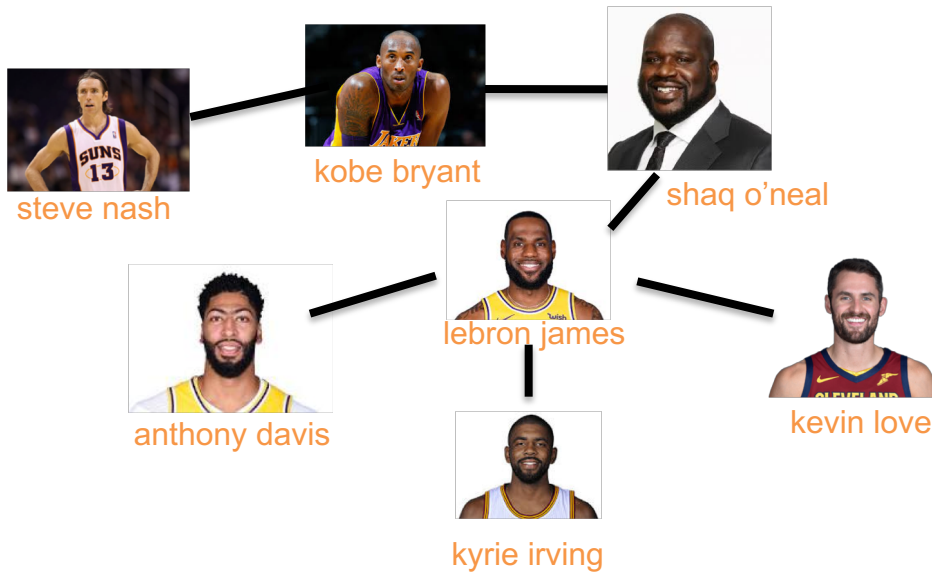
Connected undirected graph with no cycles



Rooted Tree



A rooted tree



Pick any vertex as root

Let the rest of the tree hang under "gravity"

Every n vertex tree has $n-1$ edges

Trees

This page collects material from previous incarnations of CSE 331 on trees, especially the proof that trees with n nodes have exactly $n - 1$ edges.

Where does the textbook talk about this?

Section 3.1 in the textbook has the lowdown on trees.

Fall 2018 material

Here is the lecture video:

CSE331 on 9/21/2018 (Fri)



Every n vertex tree has $n-1$ edges

Let G be an undirected graph on n nodes

Then ANY two of the following implies the third:

T is connected

T has no cycles

T has $n-1$ edges

Rest of Today's agenda

Algorithms for checking connectivity

Checking by inspection



steve nash



kobe bryant



shaq o'neal



anthony davis



lebron james



kevin love



kyrie irving

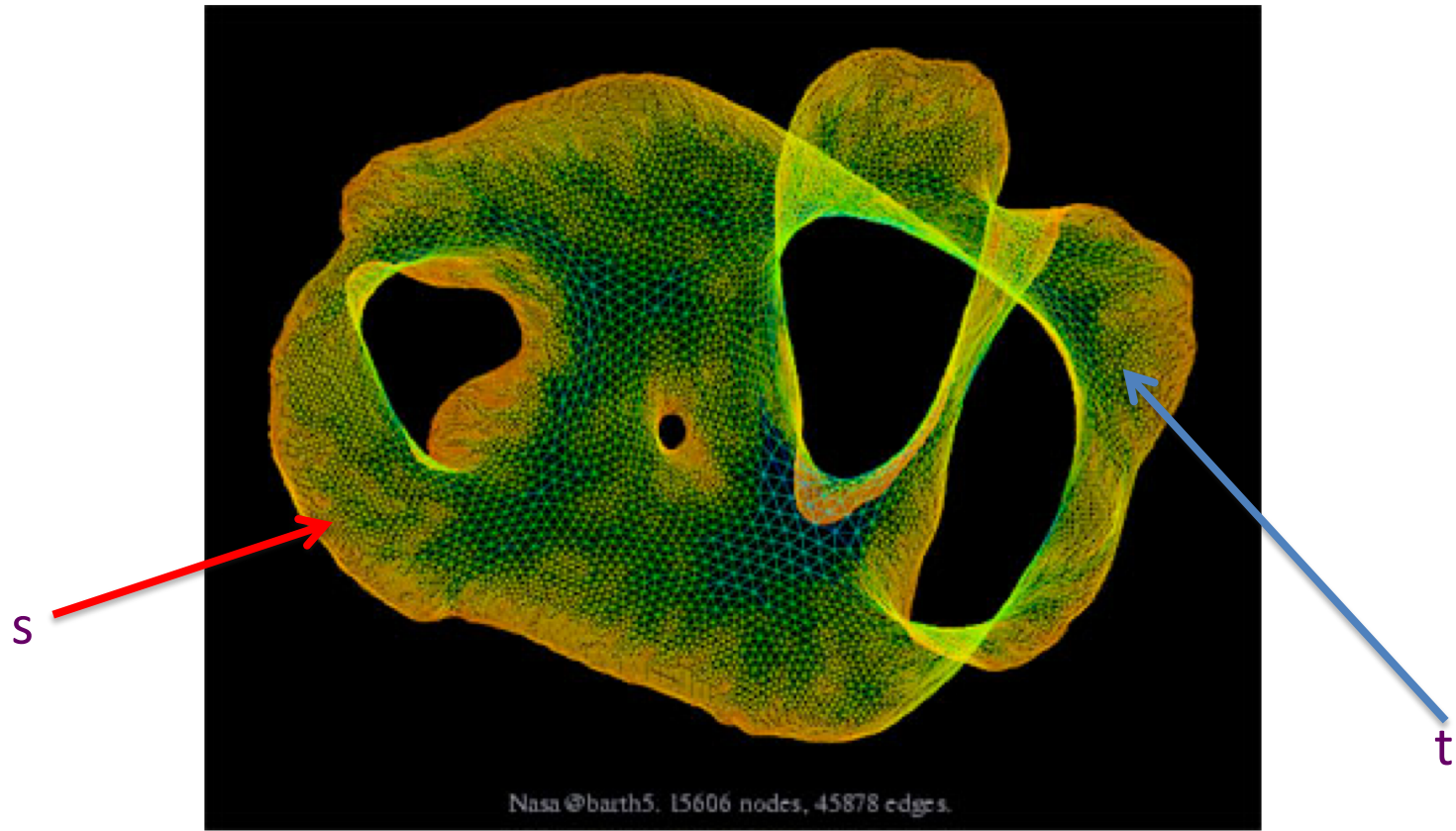


michael jordan



scottie pippen

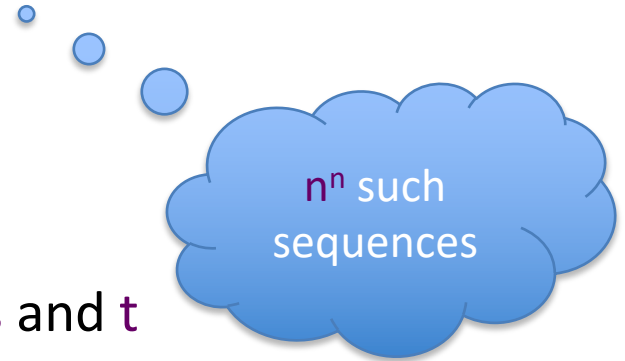
What about large graphs?



Are s and t connected?

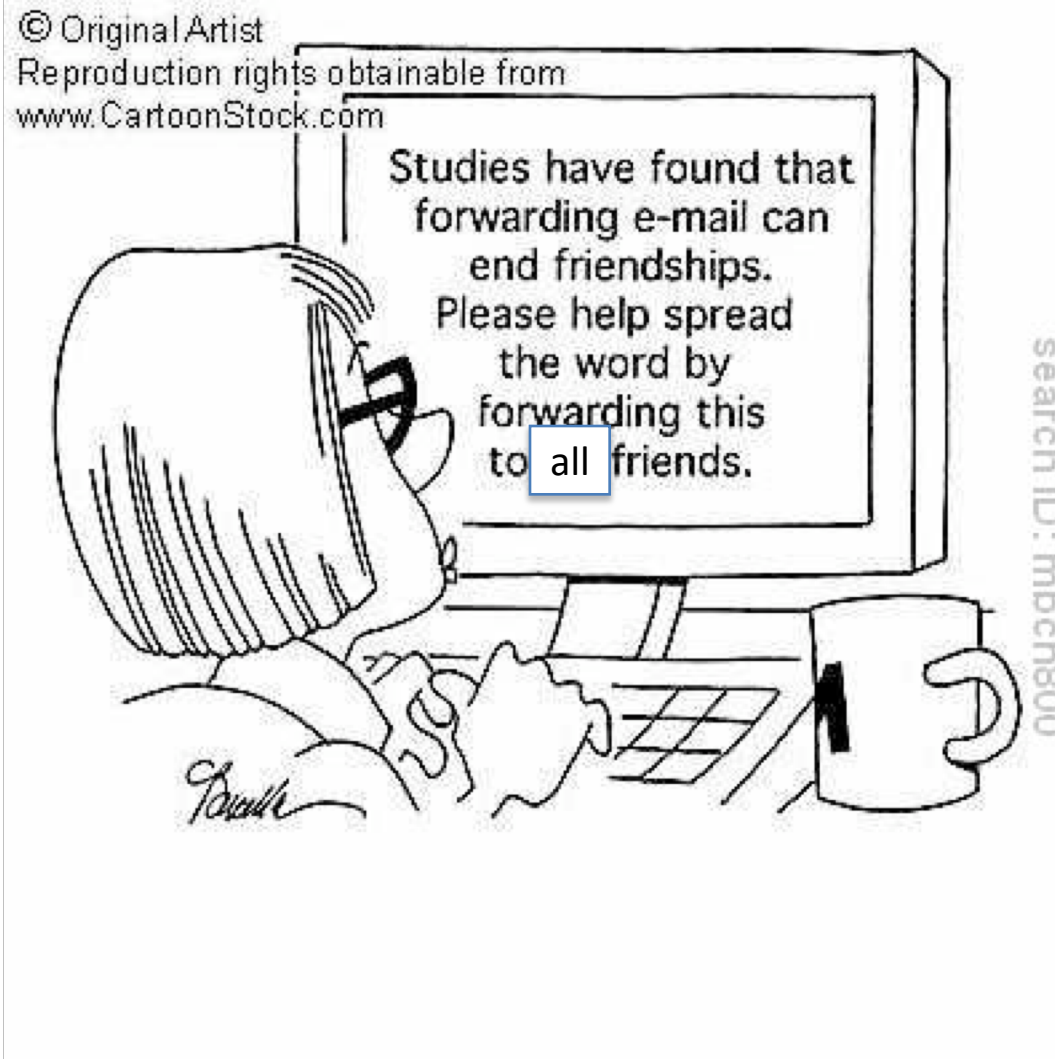
Brute-force algorithm?

List all possible vertex sequences between s and t



Check if any is a path between s and t

Algorithm motivation



Breadth First Search (BFS)

BFS via examples

In which we derive the breadth first search (BFS) algorithm via a sequence of examples.

Expected background

These notes assume that you are familiar with the following:

- Graphs and their representation. In particular,
 - Notion of connectivity of nodes and connected components of graphs
 - Adjacency list representation of graphs
 - Notation:
 - $G = (V, E)$
 - $n = |V|$ and $m = |E|$
 - $CC(s)$ denotes the connected component of s
- Trees and their basic properties

The problem

In these notes we will solve the following problem:

Connectivity Problem

Input: Graph $G = (V, E)$ and s in V

Output: All t connected to s in G

Breadth First Search (BFS)

Build layers of vertices connected to s

$$L_0 = \{s\}$$

Assume L_0, \dots, L_j have been constructed

L_{j+1} is the set of vertices not chosen yet but are connected by an edge to L_j

Stop when new layer is empty