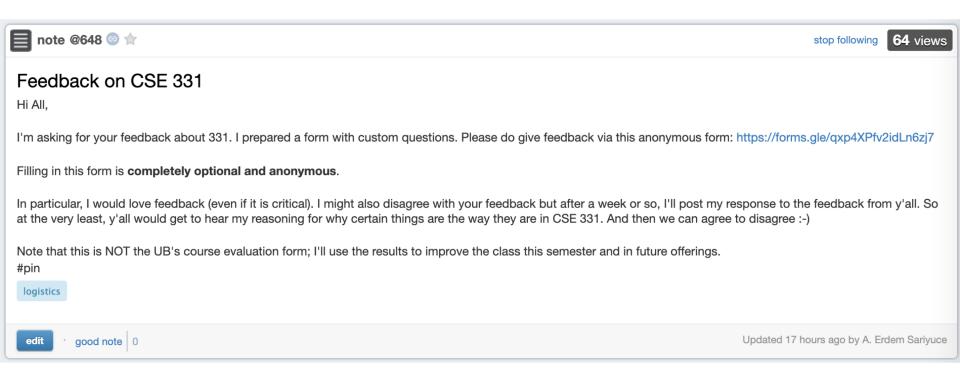
### Lecture 32

CSE 331 Apr 20, 2020

#### Give feedback!



## Subset sum problem

Input: n integers  $w_1, w_2, ..., w_n$ 

bound W

Output: subset S of [n] such that

(1) sum of w<sub>i</sub> for all i in S is at most W

(2) w(S) is maximized

#### Recursive formula

 $OPT(j, B) = max value out of w_1,...,w_j with bound B$ 

If 
$$w_j > B$$

$$OPT(j, B) = OPT(j-1, B)$$

$$OPT(j, B) = max \{ OPT(j-1, B), w_j + OPT(j-1, B-w_j) \}$$

## Knapsack problem

Input: n patege(νε<sub>1</sub>,νν<sub>1</sub>,),ν.<sub>2</sub>, , (ν,γ,γ<sub>1</sub>),

bound W

Output: subset S of [n] such that

(1) sum of w<sub>i</sub> for all i in S is at most W

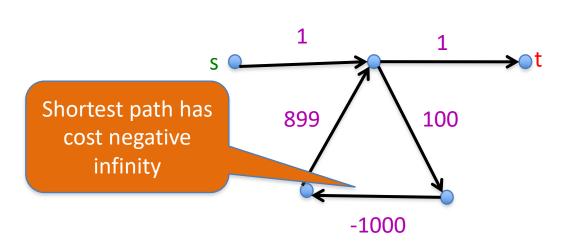
(2) w((S)) is maximized

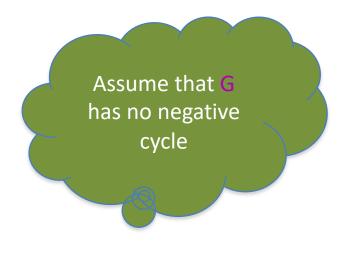
#### **Shortest Path Problem**

Input: (Directed) Graph G=(V,E) and for every edge e has a cost  $c_e$  (can be <0)

t in V

Output: Shortest path from every s to t





### When to use Dynamic Programming

There are polynomially many sub-problems



Richard Bellman

Optimal solution can be computed from solutions to sub-problems

There is an ordering among sub-problem that allows for iterative solution

# Today's agenda

Bellman-Ford algorithm