

Lecture 4

CSE 331

Feb 3, 2020

Please do keep on asking Qs!

The only bad question is the one that is not asked!

Not just technical Qs but also on how the class is run

HW 0 solutions are posted

- And go over incorrect proofs

If you need it, ask for help



Read the syllabus CAREFULLY!

No graded material will be handed back till you pass the syllabus quiz!
106 of 153 completed so far


Syllabus Quiz


Options

[View handin history](#)

[View writeup](#)

[Download handout](#)

 Due: May 8th 2020, 12:14 pm

 Last day to handin: May 8th 2020, 2:14 pm

Academic Integrity

Question 1: Sharing my answers to this syllabus quiz with other 331 students

- Is OK if I do it to help out a friend
- It does not matter since there is no grade attached with it
- Is an academic integrity violation and should not be done
- Is an academic integrity violation but I can take the chance

Question 2: Penalty for academic violation in CSE 331 is an automatic

- Warning and a chance to make-up
- A zero in the assignment AND a letter grade reduction (for first violation across all CSE courses) and an F in the course (for 2nd violation across all CSE courses)
- A zero in the corresponding assignment and nothing else
- Expulsion from UB

Separate Proof idea/proof details

</> Note

Notice how the solution below is divided into proof idea and proof details part. **THIS IS IMPORTANT: IF YOU DO NOT PRESENT A PROOF IDEA, YOU WILL NOT GET ANY CREDIT EVEN IF YOUR PROOF DETAILS ARE CORRECT.**

Proof Idea

As the hint suggests there are two ways of solving this problem. (I'm presenting both the solutions but of course you only need to present one.)

We begin with the approach of reducing the given problem to a problem you have seen earlier. ➤ Build the following complete binary tree: every internal node in the tree represents a "parent" RapidGrower while its two children are the two RapidGrowers it divides itself into. After s seconds this tree will have height s and the number of RapidGrowers in the container after s seconds is the number of leaf nodes these complete binary tree has, which we know is 2^s . Hence, the claim is correct.

The proof by induction might be somewhat simpler for this problem if you are not comfortable with reduction. In this case let $R(s)$ be the number of RapidGrowers after s seconds. Then we use induction to prove that $R(s) = 2^s$ while using the fact that $2 \cdot 2^s = 2^{s+1}$.

Proof Details

We first present the reduction based proof. Consider the complete binary tree with height s and call it $T(s)$. Further, note that one can construct $T(s + 1)$ from $T(s)$ by attaching two children nodes to all the leaves in $T(s)$. Notice that the newly added children are the leaves of $T(s + 1)$. Now assign the root of $T(0)$ as the original RapidGrower in the container. Further, for any internal node in $T(s)$ ($s \geq 0$), assign its two children to the two RapidGrowers it divides itself into. Then note that there is a one to one correspondence between the RapidGrowers after s seconds and the leaves of $T(s)$. ➤ Then we use the well-known fact (cite your 191/250 book here with the exact place where one can find this fact): $T(s)$ has 2^s leaves, which means that the number of RapidGrowers in the container after s seconds is 2^s , which means that the claim is correct.

TA office hours finalized

CSE 331 Syllabus Piazza Schedule Homeworks Autolab Mini Project Support Pages Sample Exams

CSE 331


Spring 2020


331

Today Feb 2 - 8, 2020 Print Week Month Agenda

	Sun 2/2	Mon 2/3	Tue 2/4	Wed 2/5	Thu 2/6	Fri 2/7	Sat 2/8
8am		8 - HW 0 due					
9am			9 - 9:50 Winnie OH		9 - 10:50 Liam OH		
10am			10 - 10:50 Rishi OH	10 - 10:50 Winnie OH		10 - 11:50 Nick OH	
11am				11 - 11:50 Rishi OH			
12pm		12p - 12:50p Veronica OH	12p - 12:50p Hans OH	12p - 12:50p Veronica OH	12p - 12:50p Hans OH	12p - 12:50p Xuanhua OH	
1pm			1p - 1:50p Elijah OH		1p - 2:30p Jessica OH		
2pm		2p - 2:50p 331 Lecture	2p - 3:50p Jacob OH	2p - 2:50p 331 Lecture	2:30p - Johnny OH	2p - 2:50p 331 Lecture	
3pm				3p - 3:50p Erdem OH	3p - 3:50p Rishi OH	3p - 3:50p Elijah OH	
4pm		4p - 4:50p Erdem OH 4p - 4:50p Nick OH	4p - 4:50p Jessica OH		4p - 5:30p Johnny OH		
5pm			5p - 5:50p Xuanhua OH				

Events shown in time zone: Eastern Time - New York

 GoogleCalendar



Questions/Comments?

Proof Details: Q1(b) on HW0

Argument does not use ANYTHING about the problem statement!

(incomplete) exam

Follows from part (a)

of perfect matchings with n men and n women.

Base case: $P(1) = 1! = 1$

This assumes number of perfect matchings only depends on n

Inductive hypothesis: Assume that $P(n-1) = (n-1)!$

Inductive step: Note that $P(n) = n * P(n-1) = n * (n-1)! = n!$

What are the issues with the above “proof”?

Proof Details: Q1(b) on HW0

Incorrect (incomplete)

Needs justification

Claim 1: Number of perfect matchings is = number of permutations of $1\dots n$

Claim 2: Number of permutations of $1\dots n$ is $n!$

Needs justification

Claims 1 + 2 prove the result

Follow from 191 (?)

What are the issues with the above proof?

Proof by contradiction for Q1(a)

Incorrect example

Assume for contradiction there is an example where number of perfect matchings depends on the identities of the men and women.

Let $n = 1$ and consider two cases

(1) $M = \{BP\}$ and $W = \{JA\}$

(2) $M = \{BBT\}$ and $W = \{AJ\}$

You can only assume things about the example directly implied by it being a counter-example

In both cases the number of perfect matchings is $1 = 1!$

Hence contradiction.

There is NO contradiction

What are the issues with the above proof?

Questions/Comments?

(Perfect) Matching

A matching $S \subseteq M \times W$ such that following conditions hold:

S is a **set** of pairs (m,w) where m in M and w in W

- (1) For every woman w in W , exist *at most* ^{exactly} one m such that (m,w) in S
- (2) For every man m in M , exist *at most* ^{exactly} one w such that (m,w) in S

Perfect matching

On matchings

Michael



Pam



Dwight



Angela



Jim



Holly



A valid matching

Michael



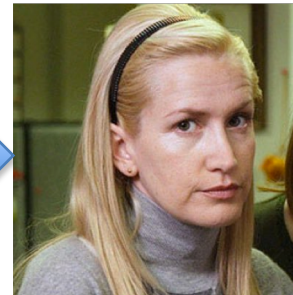
Pam



Dwight



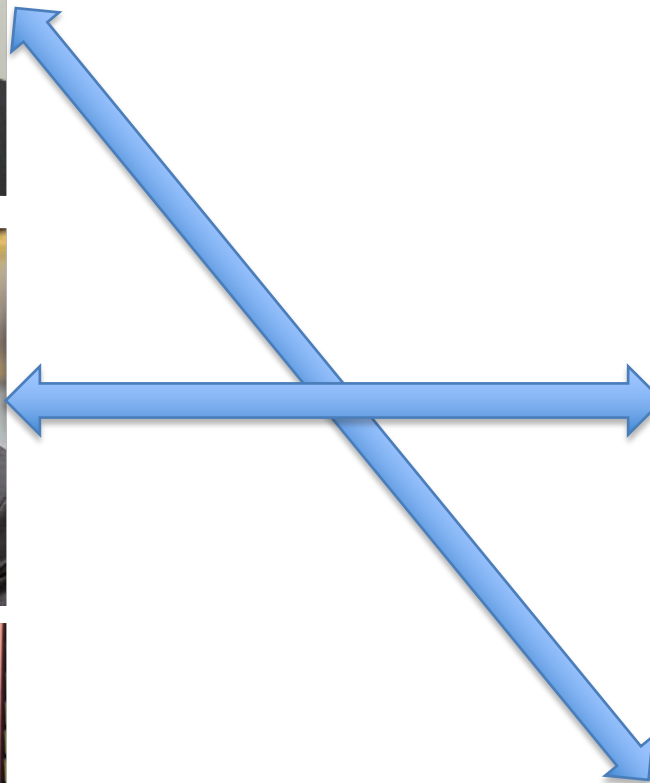
Angela



Jim



Holly



Not a matching

Michael



Pam



Dwight



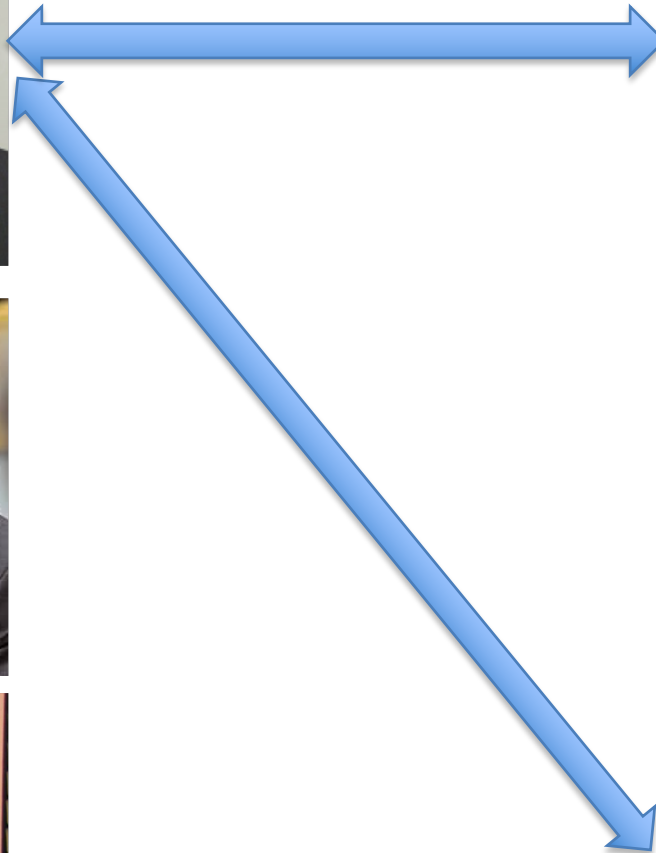
Angela



Jim



Holly



Perfect matching

Michael



Pam



Dwight



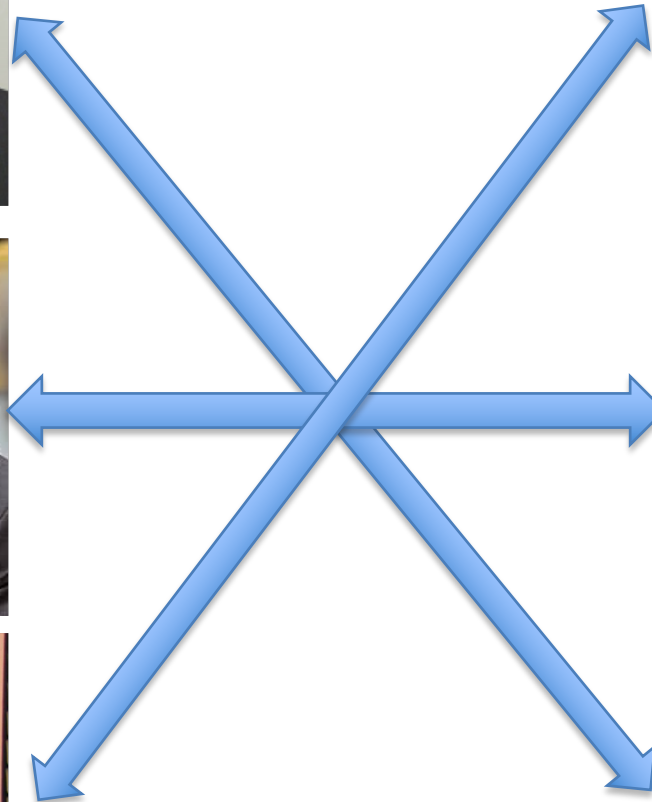
Angela



Jim



Holly



Back to couple more definitions

Preferences



Instability

