## Lecture 19

CSE 331
Mar 15, 2021

## Mid-terms this week

## Midterms: Rules that you should follow

The midterms are this week on Wed, Mar 17 and Fri, March 19. Please see @530 about the content and how you should prepare.
 DON'T LOOK AT QUIZ 1 POST FROM LAST WEEK.
 understanding).

First, the rules about start/ finish times, cheat-sheet, and what you need to do before the exam

- The midterms will start at $\mathbf{2 : 4 5} \mathbf{~ p m}$ (NOT 3:00pm!) and end at 4:00pm. This means you must be online at your Zoom link at 2:45pm. You'll be emailed the Zoom links tomorrow.
- Proctors will lock the Zoom rooms at 2:50pm which means you WON'T be able to join the exam after 2:50
- This is important for us because many proctors (including myself!) had trouble with the late joiners; we have to check certain things with each participant so you have to join on time!
- Once you join the Zoom room, the proctor will verify certain things for each participant.
- You must show your UB id to the proctor. If you don't have it (!), you must show your driver's license or passport (your photo must be there!)
- You must ensure that the BOTH cameras are located correctly, see below for this.
- The midterm will be posted on Piazza at 2:58pm (NO EMAIL WILL BE SENT), It'll be a link to a pdf in UB Box.
- This will ensure that everyone will have access at the same time.
- After you click the link, you MUST close the Piazza tab in your browser.
- The exam duration is 62 minutes: starting at $2: 58$, ending at $4: 00$. THIS INCLUDES THE UPLOADING TIME!
- If this was an in-person exam, you would be given just 45 minutes. Thus, you are given EXTRA 17 minutes for uploading.
- The deadline at Autolab will be set as $4: 00 \mathrm{pm}$ sharp. I guarantee that NO LATE SUBMISSION IS POSSIBLE.

- This is a closed-book, closed-notes, closed-internet exam. You can use one letter-sized cheat-sheet during the midterm (you can use both sides).
- You can use the same or different cheat sheets on Wed and Fri.


## Dijkstra's shortest path algorithm



## Towards Dijkstra’s algo: part 1

Determine $\mathrm{d}(\mathrm{t})$ one by one

$$
d(s)=0
$$



## Towards Dijkstra’s algo: part 2

## Determine $\mathrm{d}(\mathrm{t})$ one by one

Let $u$ be a neighbor of $s$ with smallest $\left.\right|_{(s, u)}$

$$
\mathrm{d}(\mathrm{u})=\mathrm{I}_{(\mathrm{s}, \mathrm{u})}
$$



Length of $\sim 0$
Not making any claim on other vertices

## Towards Dijkstra’s algo: part 3

## Determine $\mathrm{d}(\mathrm{t})$ one by one

Assume we know $d(v)$ for every $v$ in $R$

Compute an upper bound d'(w) for every w not in R

$$
\begin{aligned}
& d(w) \leq d(u)+I_{(u, w)} \\
& d(w) \leq d(x)+I_{(x, w)} \\
& d(w) \leq d(y)+I_{(y, w)}
\end{aligned}
$$

$$
d^{\prime}(w)=\min _{e=(u, w) \text { in } E, u \text { in } R} d(u)+l_{e}
$$

## Dijkstra's shortest path algorithm



Input: Directed $G=(V, E), I_{e} \geq 0$, s in $V$
$R=\{s\}, d(s)=0$
While there is a $(u, x)$ in $E$ s.t. $u$ in $R$ and $x$ not in $R$
Pick $w$ among all $x$ with smallest $d^{\prime}(w)$ value Add w to R $d(w)=d^{\prime}(w)$

$$
d^{\prime}(w)=\min _{e=(u, w) \text { in } E, u \text { in } R} d(u)+l_{e}
$$

$$
\begin{array}{ll}
d(s)=0 & d(u)=1 \\
d(w)=2 & d(x)=2 \\
d(y)=3 & d(z)=4
\end{array}
$$



## Couple of remarks

The Dijkstra's algo does not explicitly compute the shortest paths

Can maintain "shortest path tree" separately

Dijkstra's algorithm does not work with negative weights

Left as an exercise

## Rest of Today's agenda

Prove the correctness of Dijkstra's Algorithm

Runtime analysis of Dijkstra's Algorithm

