

# Lecture 3

CSE 331

Feb 5, 2021

# Who is Algorithm named after?

Abū ‘Abd Allāh Muhammad ibn Mūsā al-Khwārizmī

9<sup>th</sup> century Persian astronomer/mathematician

825 AD: “On Calculation with Arabic Numerals”

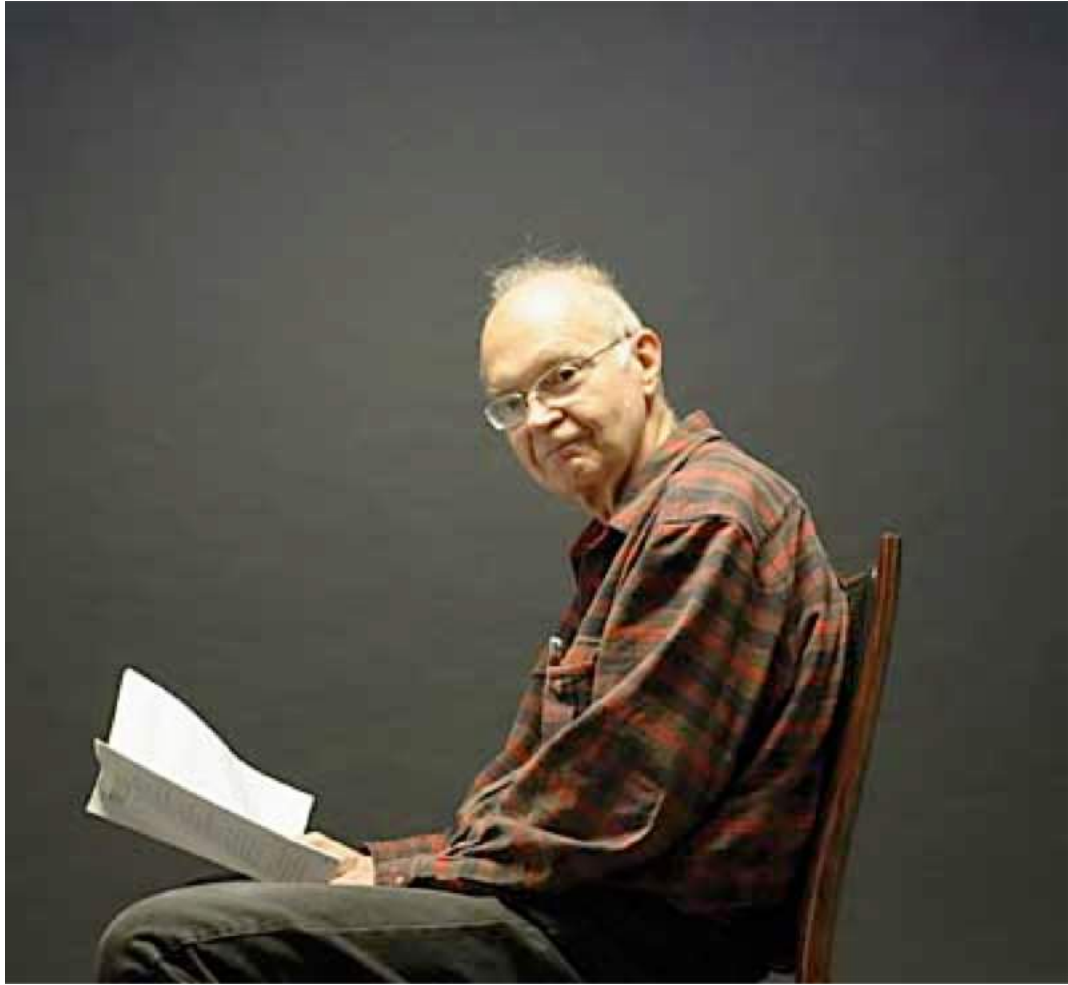


Latin translation 12<sup>th</sup> century

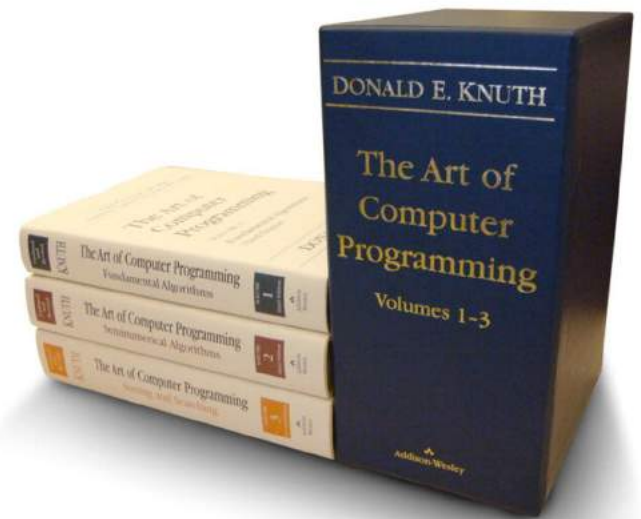
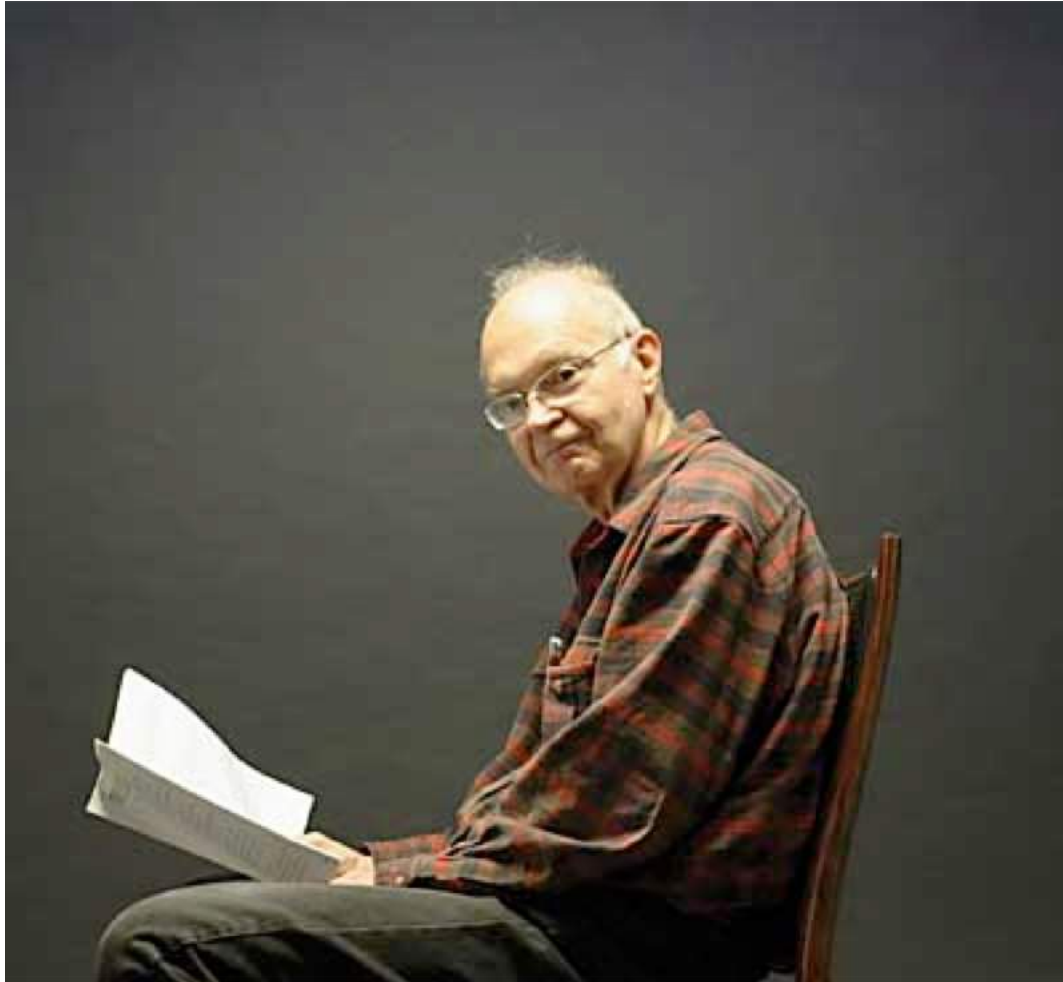
“Algorithmi de numero Indorum”



# What are Algorithms?



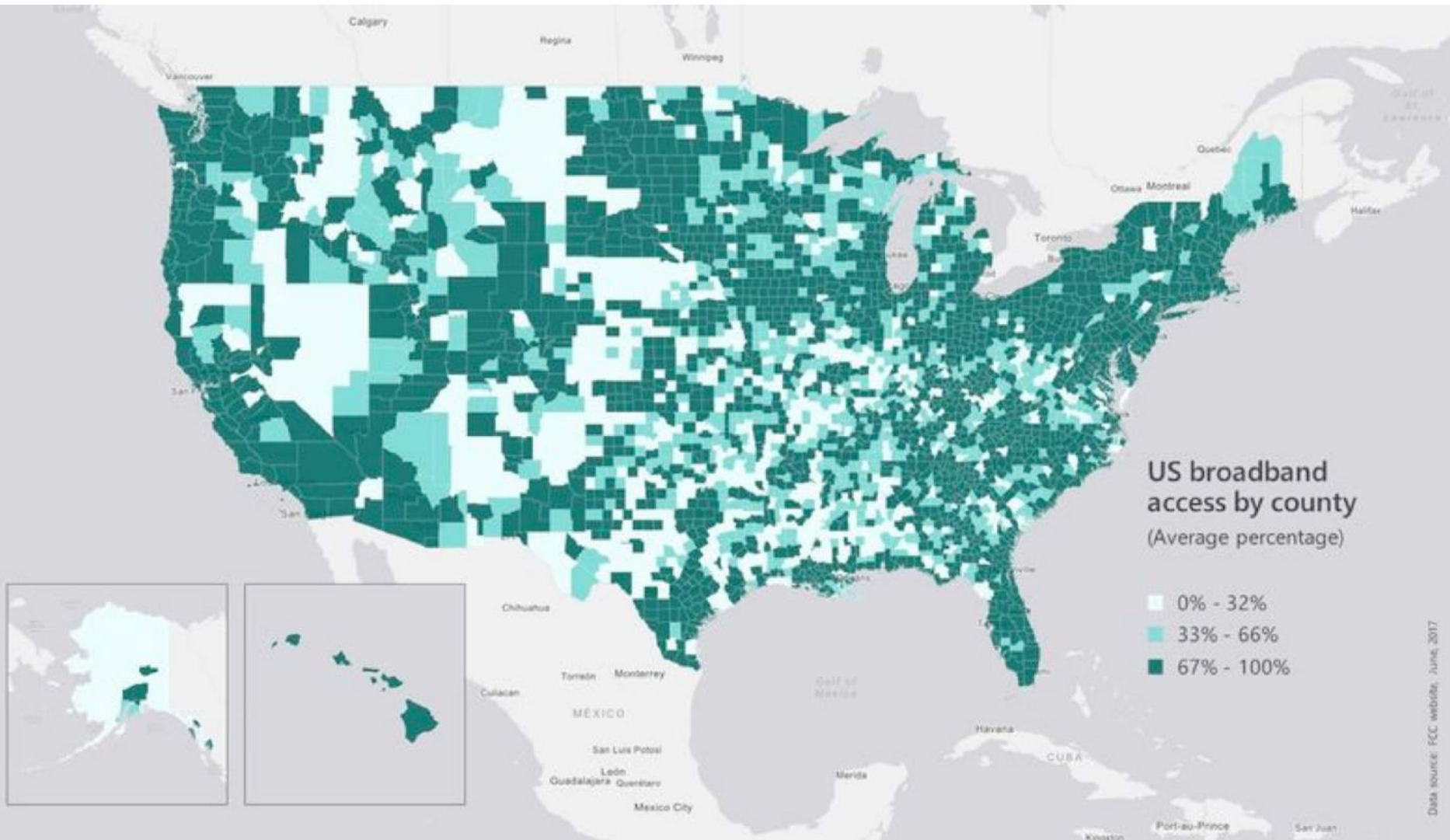
# Don Knuth



# Knuth's Definition

An algorithm is a finite, definitive, effective procedure with some input and some output

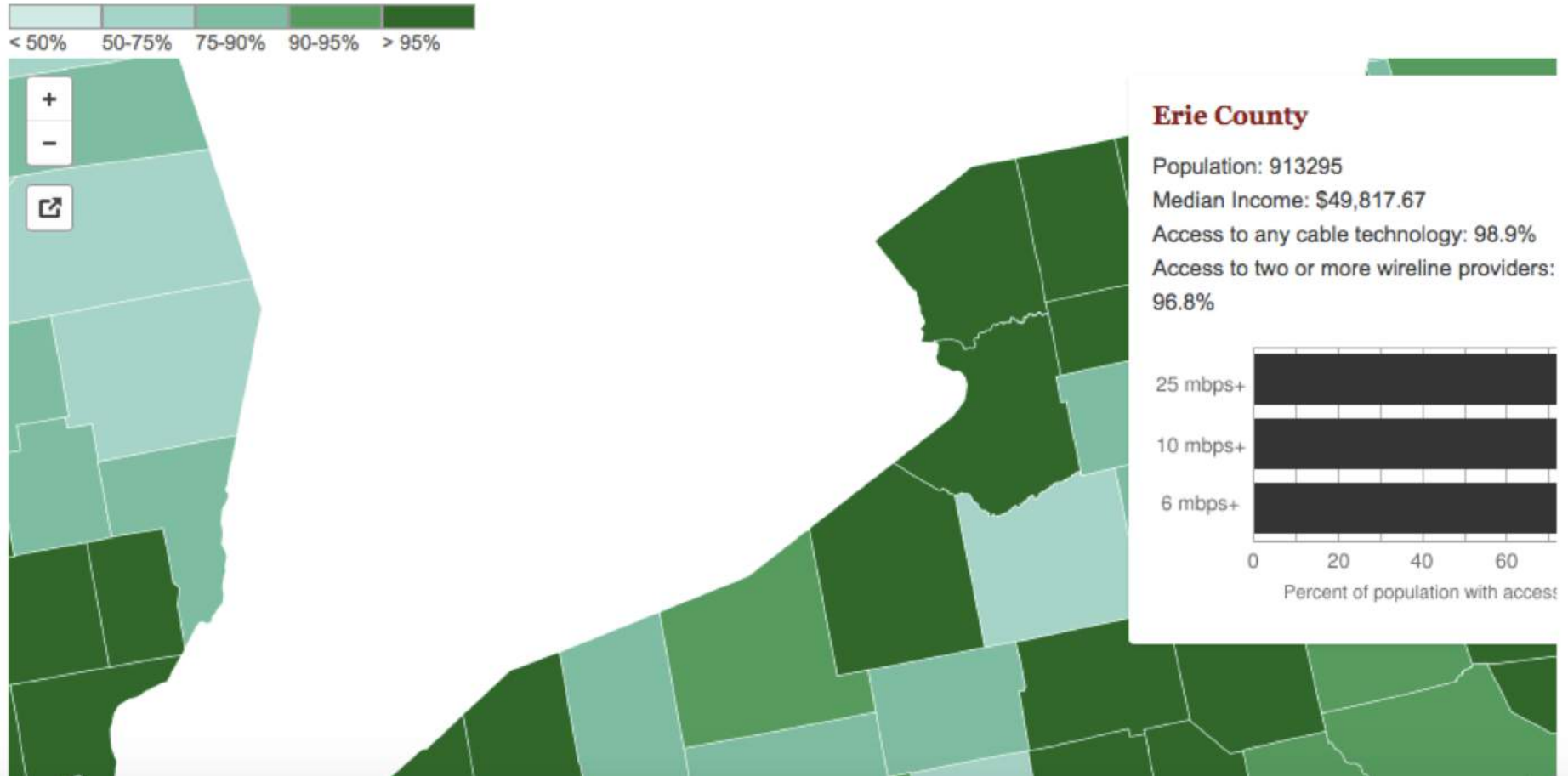
# Broadband access



<https://assets.bwbx.io/images/users/iqjWHBFdfxIU/iZSjibxE1KJs/v1/800x-1.jpg>

# Erie county is reasonably good

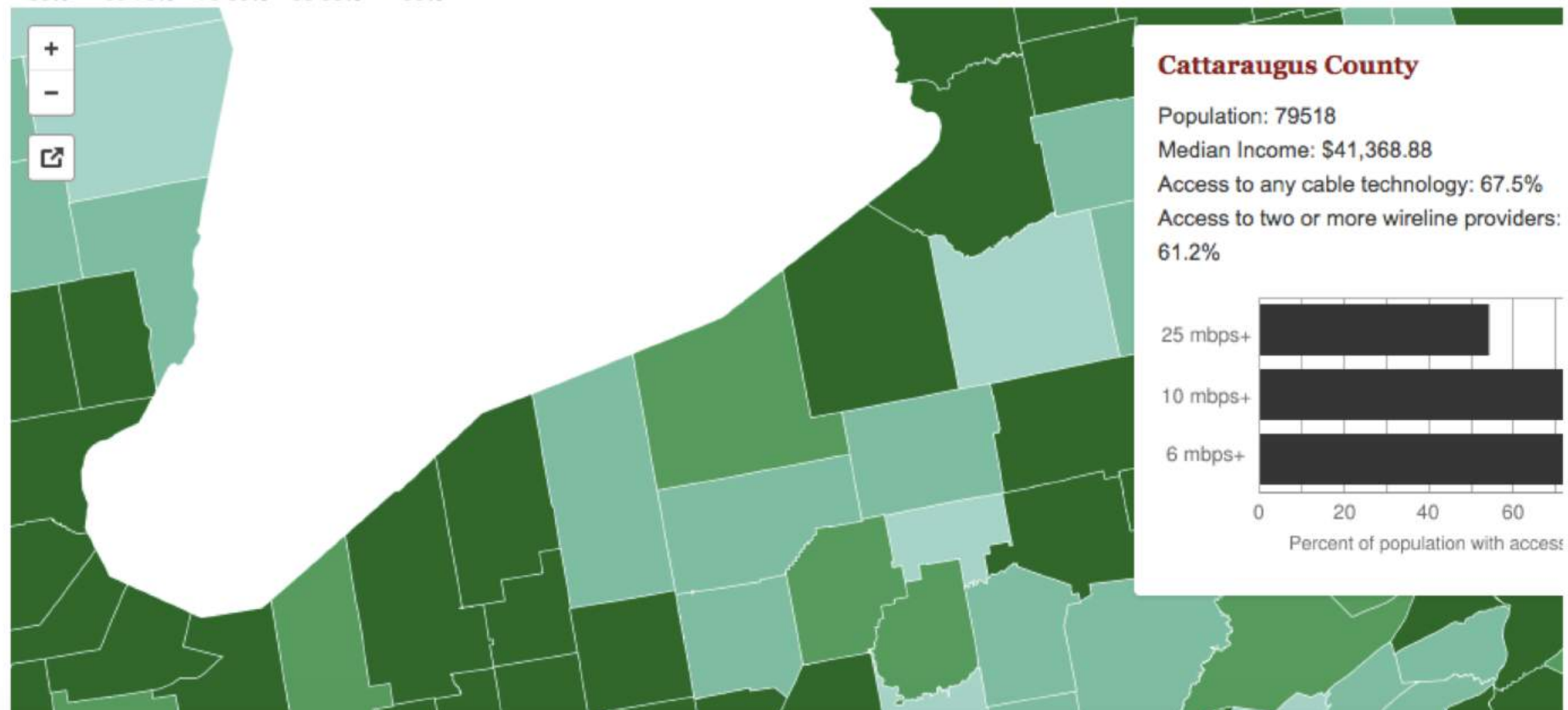
Population with access to advertised download speeds at least 6mbps





# One county over

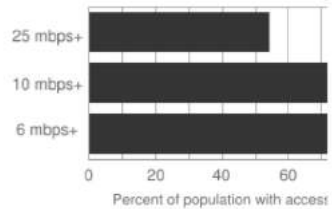
Population with access to advertised download speeds at least 6mbps



# Make broadband more available

## Cattaraugus County

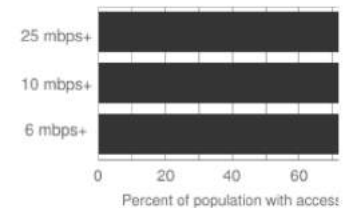
Population: 79518  
Median Income: \$41,368.88  
Access to any cable technology: 67.5%  
Access to two or more wireline providers: 61.2%



Say you are tasked to come up with the infrastructure

## Erie County

Population: 913295  
Median Income: \$49,817.67  
Access to any cable technology: 98.9%  
Access to two or more wireline providers: 96.8%



# Make broadband more available

## Input requirements

Where are the customers located?  
What are the bandwidth requirements?  
How is the input represented?

What objective are we optimizing?  
How should the connections be configured?

## Output requirements

## Problem Definition

Where should we lay down the physical stuff?  
What algorithm should be use to do this?

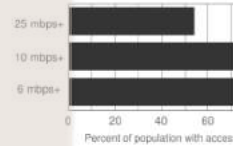
## Algorithm Design

Implement the scheme

How should we do testing and maintenance?

### Cattaraugus County

Population: 79518  
Median Income: \$41,368.88  
Access to any cable technology: 67.5%  
Access to two or more wireline providers: 61.2%



Decide whether this will be for-profit enterprise

What are technology should we use?

Get regulatory approval

Get funding

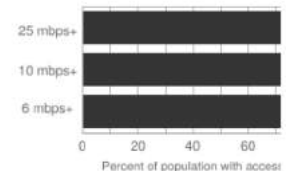
Hire people

Get access to physical space

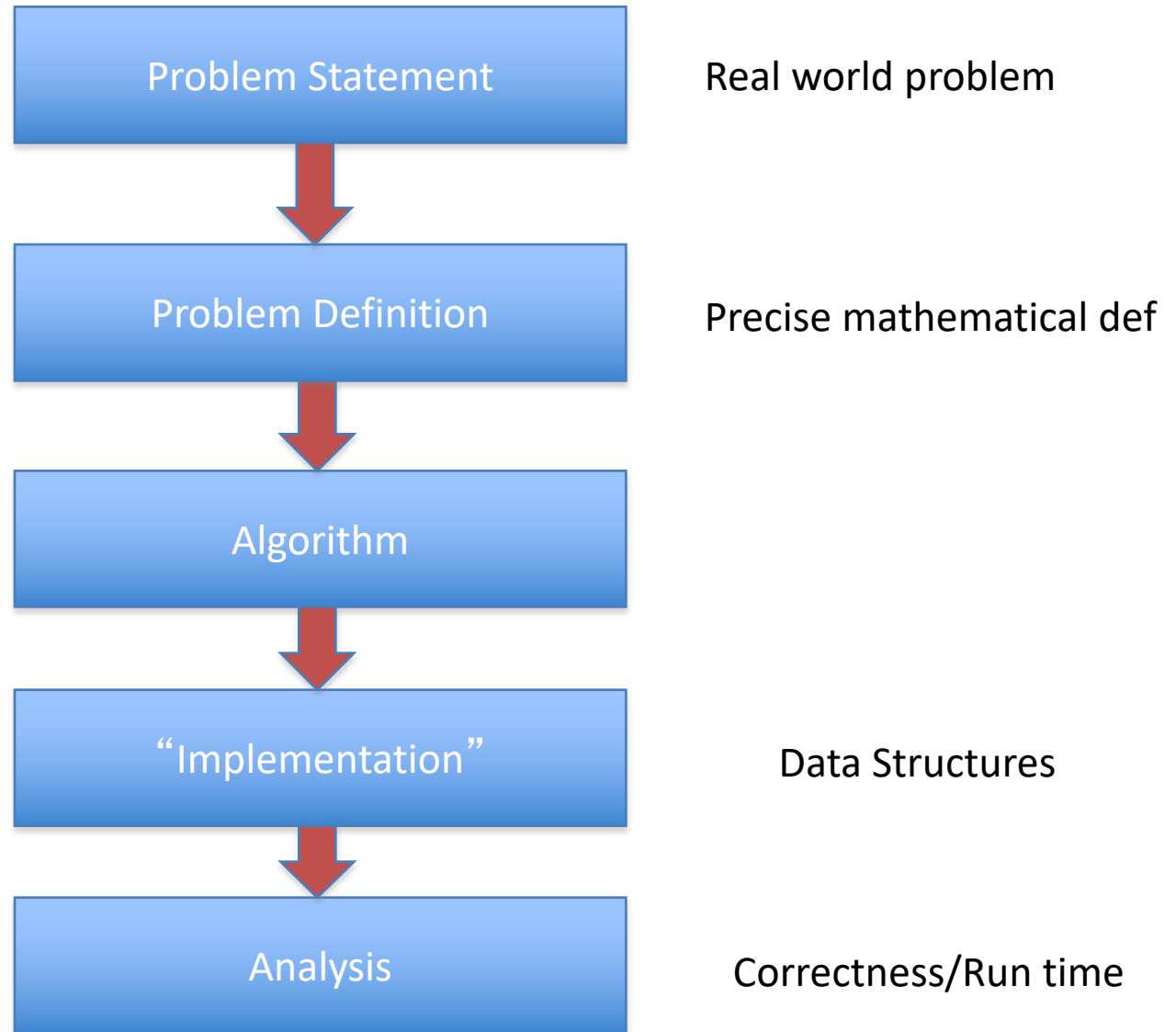
Outreach

### Erie County

Population: 913295  
Median Income: \$49,817.67  
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# Main Steps in Algorithm Design



# National Resident Matching

## Preparing for #Match2018?

**Frequently  
Asked  
Question**

**An NRMP ID is  
NOT Required for  
Submitting Your  
Applications**

[>> Learn more](#)

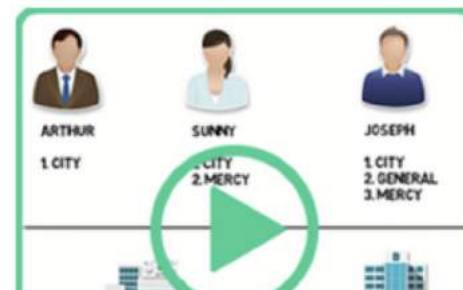
### WHAT'S HAPPENING

- Check the Eligibility of Applicants
- Registration Open for Adolescent Medicine, Medical Toxicology, and Headache Medicine
- Timely Residency Applicant Resources
- Registration Open for Colon & Rectal Surgery, Medical Genetics, Sleep Medicine, and Spinal Cord Injury

[READ MORE](#)



**VIDEO: The Match Process for Applicants**



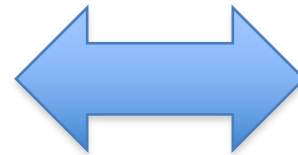
# (Screen) Docs are coming to BUF



Bailey (Grey's Anatomy)



Buffalo General



JD (Scrubs)



Millard Fillmore (Suburban)

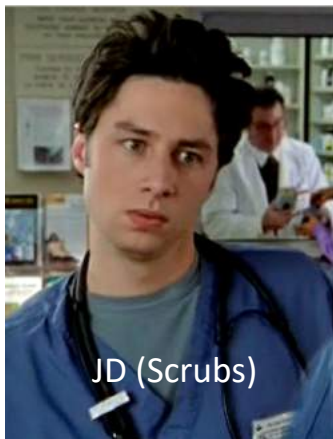
# What can go wrong?



Bailey (Grey's Anatomy)



Buffalo General



JD (Scrubs)



Millard Fillmore (Suburban)



# The situation is unstable!



Bailey (Grey's Anatomy)



Buffalo General



HOUSE  
9/25 FOX 9/8 TUE



JD (Scrubs)



Mercy Hospital of Buffalo



Millard Fillmore (Suburban)





# What happens in real life



Preferences

**NRMP**  
National Resident Matching Program



Information

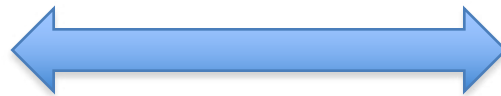
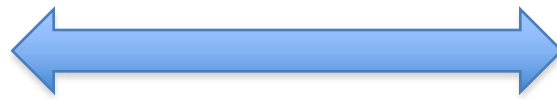
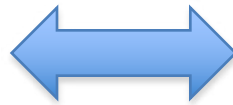
**NRMP**  
National Resident Matching Program



Preferences

**NRMP**  
National Resident Matching Program

# NRMP plays matchmaker



# Stable Matching Problem



David Gale



Lloyd Shapley

Questions/Comments?

# Matching Employers & Applicants

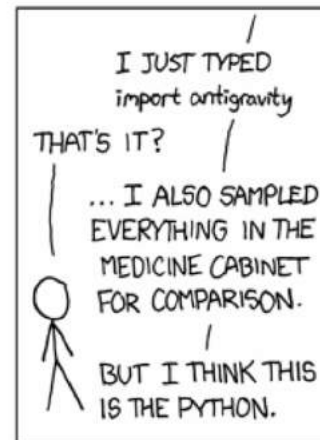
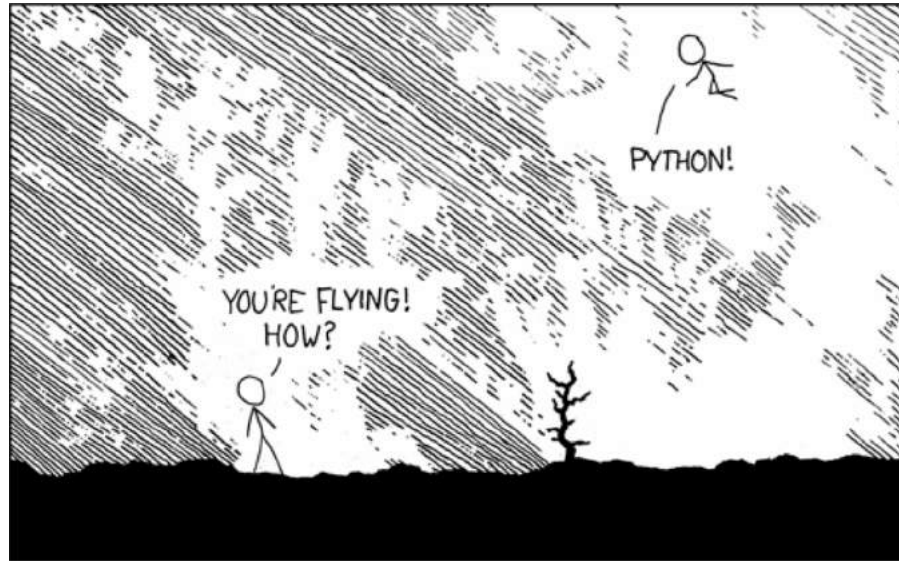
**Input:** Set of employers ( $E$ )  
Set of applicants ( $A$ )  
Preferences

**Output:** An assignment of applicants to employers that is “stable”

For every  $x$  in  $A$  and  $y$  in  $E$  such that  $x$  is **not** assigned to  $y$ , either

- (i)  $y$  prefers every accepted applicant to  $x$ ; or
- (ii)  $x$  prefers her employer to  $y$

# Simplicity is good



# Matching Employers & Applicants

**Input:** Set of employers ( $E$ )  
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**What questions to think about?**

# What questions to think about?

1) How do we specify preferences?

Preference lists

2) Ratio of applicant vs employers

1:1

3) Formally what is an assignment?

(perfect) matching

4) Can an employer get assigned  $> 1$  applicant?

NO

5) Can an applicant have  $> 1$  job?

NO

6) How many employer/applicants in an applicants/employers preferences?

All of them

7) Can an employer have 0 assigned applicants?

NO

8) Can an applicant have 0 jobs?

NO