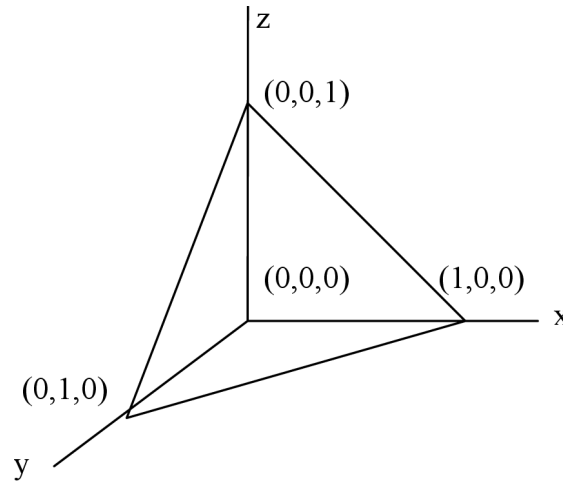


Instructions: 50 min closed book, notes. Answer all questions in the bluebook provided.

Question 1



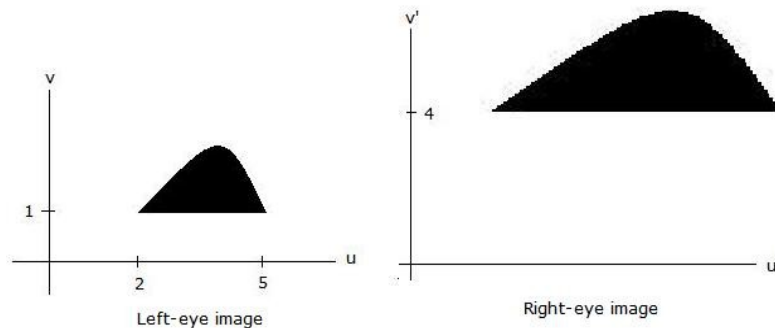
- (a) Construct a polyhedral volumetric model for the given tetrahedron.
- (b) Construct a sweep model for the given tetrahedron.

Question 2

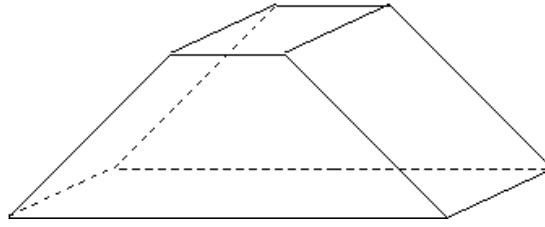
- (a) Explain how computation of an epipolar line facilitates stereopsis.
- (b) The Longuet-Higgins Equation for a given camera model is $u^T F u' = 0$ where the fundamental matrix F is

$$F = \begin{bmatrix} 0 & 0 & 6 \\ 0 & 0 & -1 \\ -1 & 1 & 0 \end{bmatrix}$$

The left-eye image, corresponding to the unprimed vector u in the Longuet-Higgins Equation above, is shown below. The visible black object has a straight edge in the image at $v=1$ which is of length 3. The same straight edge is visible in the right-eye image at $v'=4$. What is its length?



Question 3

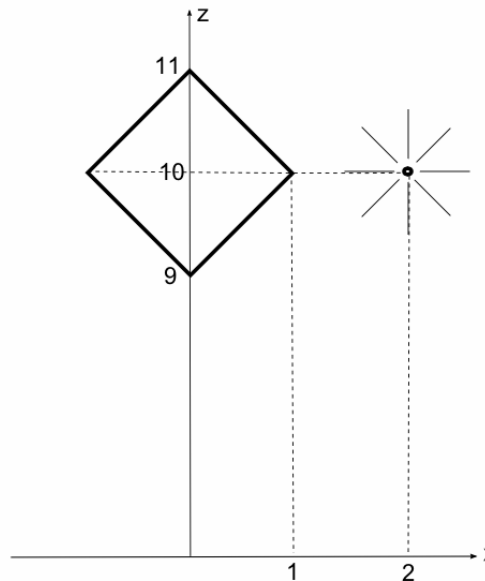


The front and back faces of this 6-sided object are trapezoids, the other 4 are rectangles. The top and bottom faces are parallel, also the front and back faces are parallel.

- Consider the aspect from which you can see only the front face. Sketch all the adjacent aspects, ie. all aspects connected to the front-face aspect in the aspect graph.
- How many topologically distinct characteristic views are there? Justify.
- How many nodes are there in the entire aspect graph for this object? HINT: Count all the nodes corresponding to aspects in which you see 1 face, then 2 faces, then 3 faces, etc.

Question 4

The diagram below shows the cross section in the xz plane of a three dimensional scene. The Lambertian object in the center has a square cross section which is constant for all y . This object is illuminated by a line source of light (like a thin florescent tube) oriented parallel to the y axis, so it appears as a single point at $x=2$, $z=10$ in this cross section.



- What point (x,y) in the image plane will be illuminated the brightest by the light reflected from the object? Use orthographic projection. Explain your reasoning.
- Compute the ratio of irradiance at the point $(x,y)=(1/2,1/2)$ in the image plane to the irradiance at the point $(1/4,1/4)$.