





Lecture 16

CSE 331

Quiz 1 this FRIDAY

 note @342   

stop following

105 views

Actions ▾

Quiz 1 on Friday, March 10

The first **in-class** quiz will be on **Friday, March 10**. We will have a 5 mins break after the quiz and the lecture will start after the break.

We will hand out the quiz papers 5 mins before the start of the class, but you will **NOT** be allowed to open the quiz to see the actual questions. However, you can use those 5 minutes to go over the instructions and get yourself in the zone.

There will be two T/F with justification questions (like those in the sample mid term 1). Also quiz 1 will cover all topics that we discussed in class till Wednesday, March 1.

Also, like the mid-term, you can bring in one letter sized cheat-sheet (you can use both sides). But other than a cheatsheet and writing implements, nothing else is allowed.

Project groups finalized

note @359   

stop following **67 views**

Action

Project Group Compositons Done and Emails Sent

Project group composition is now done for those who submitted the group sign-up form. I've sent emails to all groups. Please contact me if

- you have received two emails
 - you were mistakenly included in two groups.
- your group information is incorrect.
- you filled in the form but didn't receive an email.

Everyone who submitted the group sign-up form should have received an email by now. Please contact me by 5pm tomorrow if you notice any error in your group confirmation.

Interval Scheduling Problem

Input: n intervals $[s(i), f(i))$ for $1 \leq i \leq n$

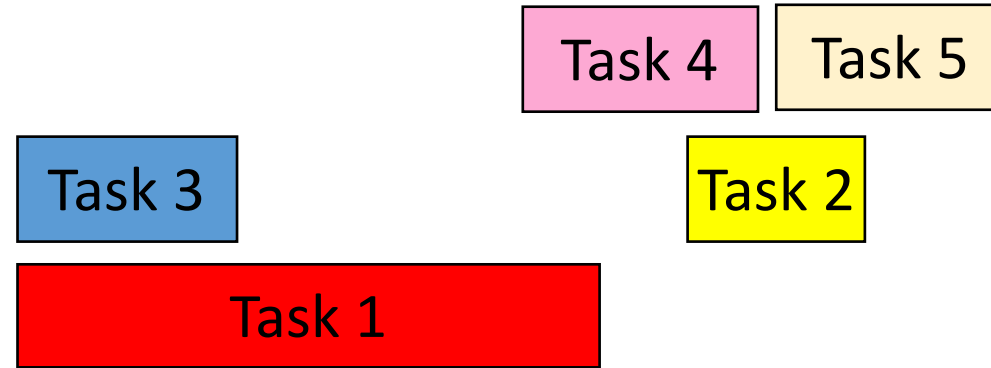
Output: A *schedule* S of the n intervals

No two intervals in S conflict

$|S|$ is maximized

Example 3

More than one conflict



Set S to be the empty set

While R is not empty

 Choose i in R

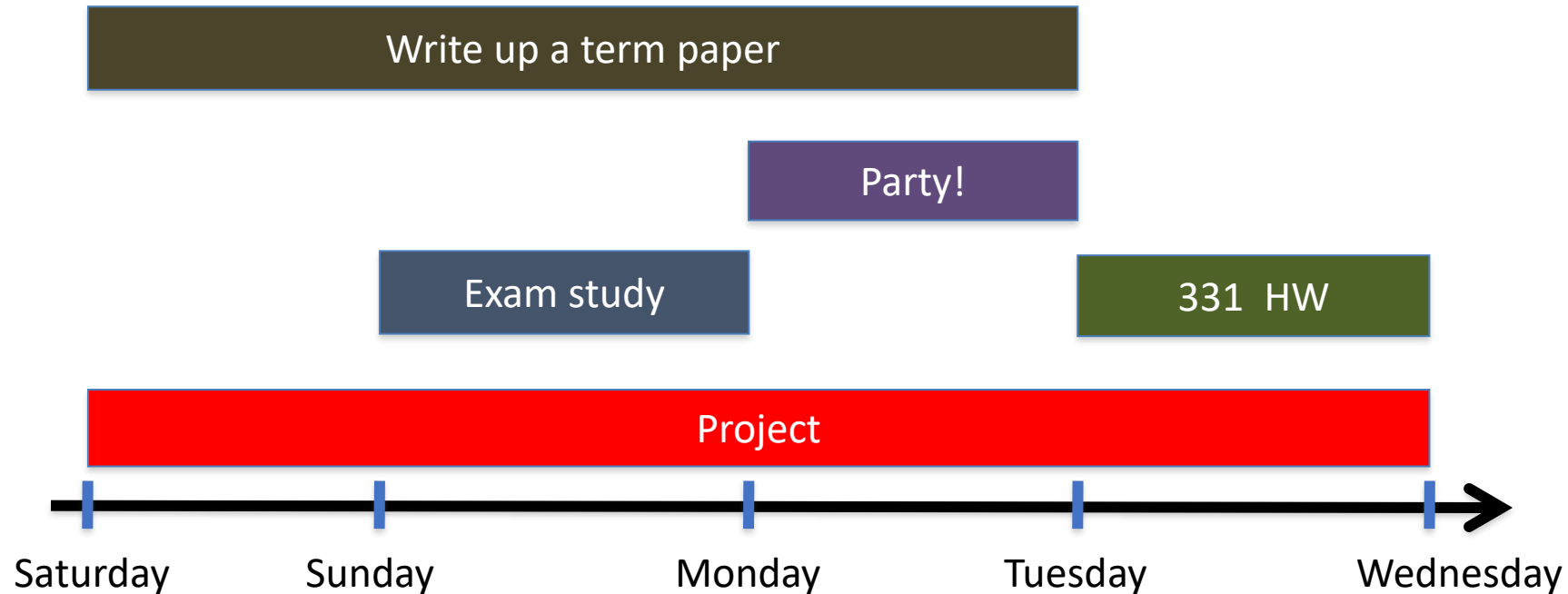
 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$

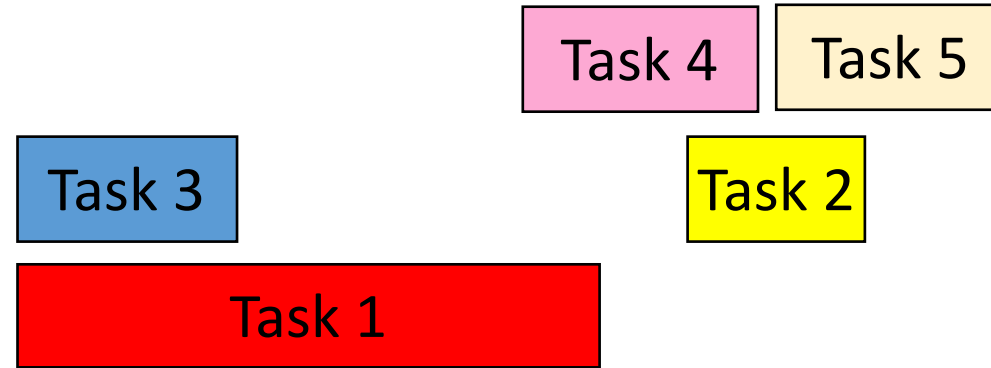
Greedily solve your blues!

Arrange tasks in some order and iteratively pick non-overlapping tasks



Making it more formal

More than one conflict



Set S to be the empty set

While R is not empty

Choose i in R that minimizes $v(i)$

 Add i to S

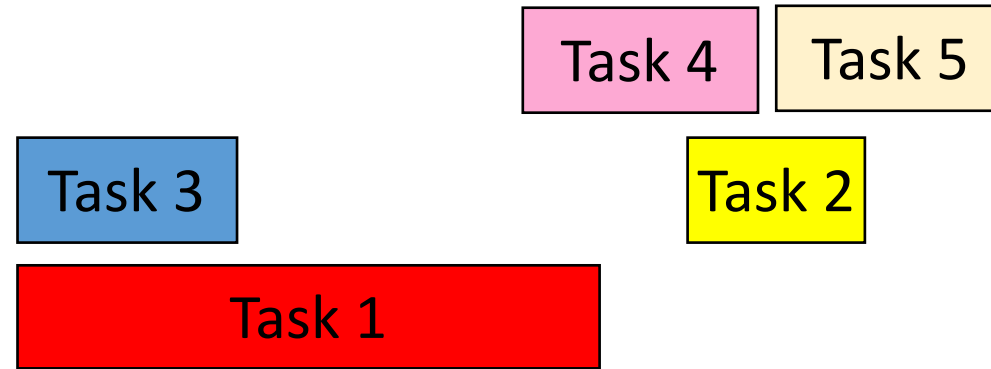
 Remove all tasks that conflict with i from R

Return $S^* = S$

Associate a
value $v(i)$
with task i

What is a good choice for $v(i)$?

More than one conflict



Set S to be the empty set

While R is not empty

 Choose i in R that minimizes $v(i)$

 Add i to S

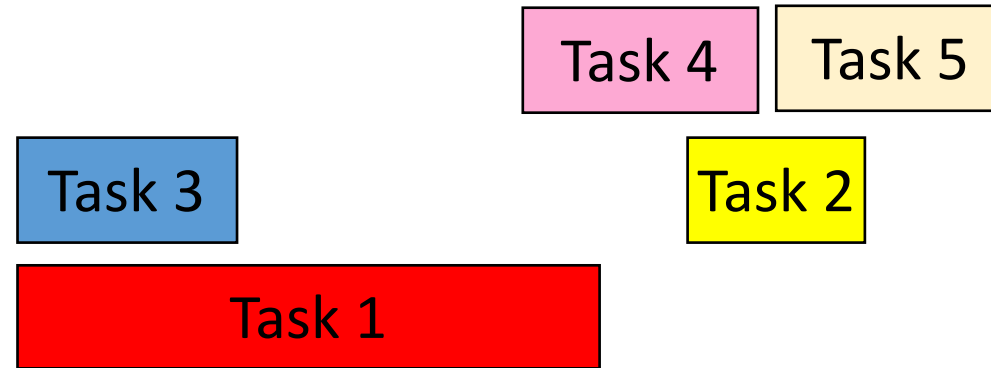
 Remove all tasks that conflict with i from R

Return $S^* = S$

Associate a
value $v(i)$
with task i

$$v(i) = f(i) - s(i)$$

Smallest duration first



Set S to be the empty set

While R is not empty

 Choose i in R that minimizes $f(i) - s(i)$

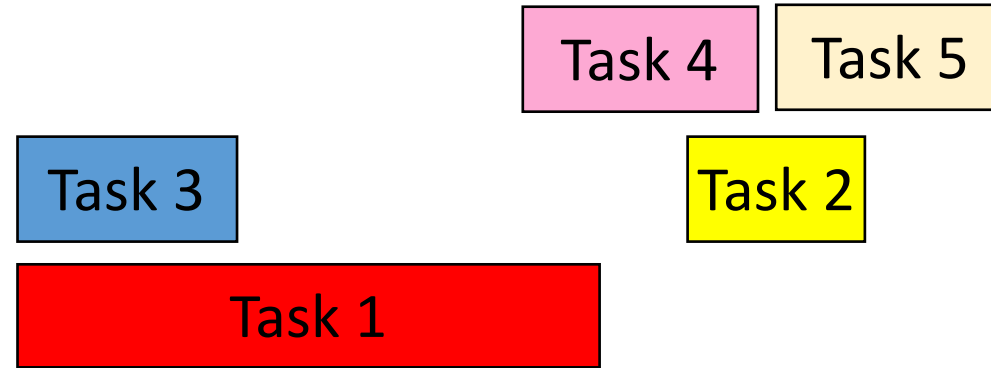
 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$

$$v(i) = s(i)$$

Earliest time first?



Set S to be the empty set

While R is not empty

 Choose i in R that minimizes $s(i)$

 Add i to S

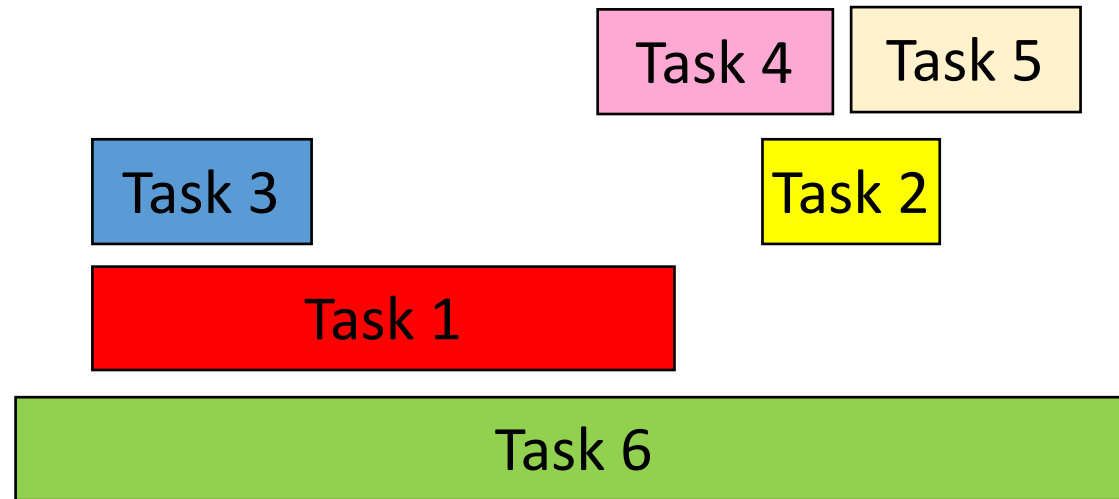
 Remove all tasks that conflict with i from R

Return $S^* = S$

So are we
done?

Not so fast....

Earliest time first?



Set S to be the empty set

While R is not empty

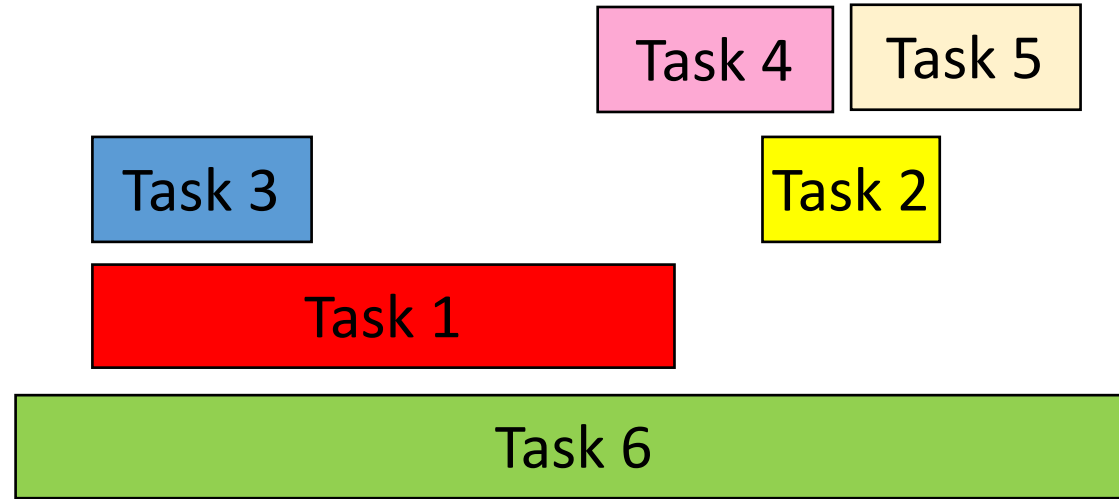
 Choose i in R that minimizes $s(i)$

 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$

Pick job with minimum conflicts



Set S to be the empty set

While R is not empty

 Choose i in R that has smallest number of conflicts

 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$

So are we
done?

Nope (but harder to show)

Set S to be the empty set

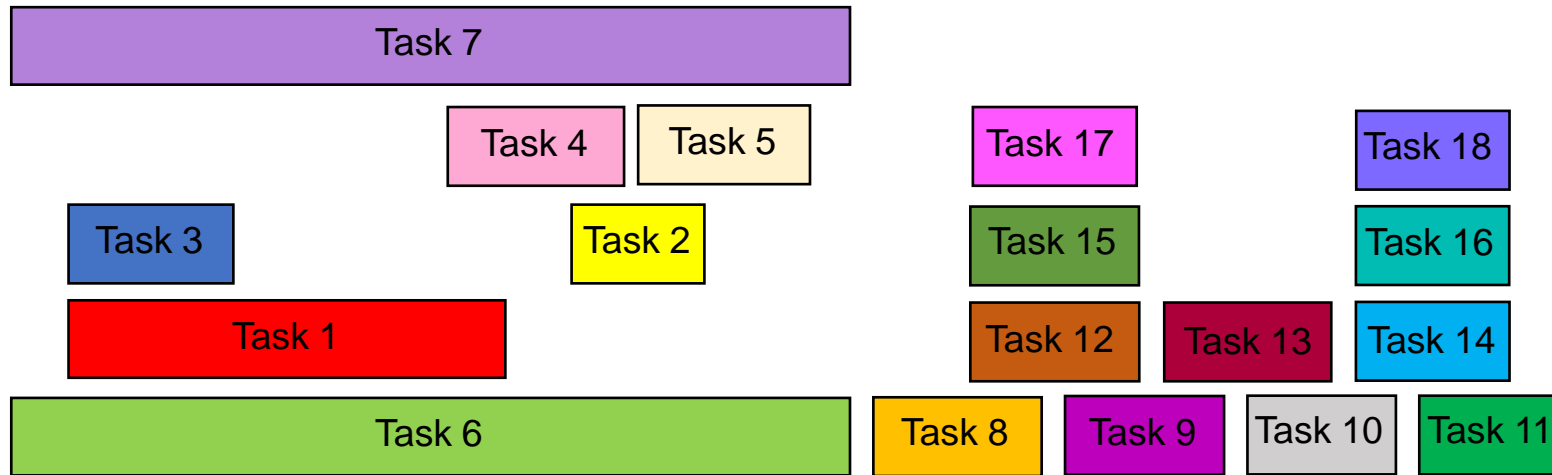
While R is not empty

 Choose i in R that has smallest number of conflicts

 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$



Set S to be the empty set

While R is not empty

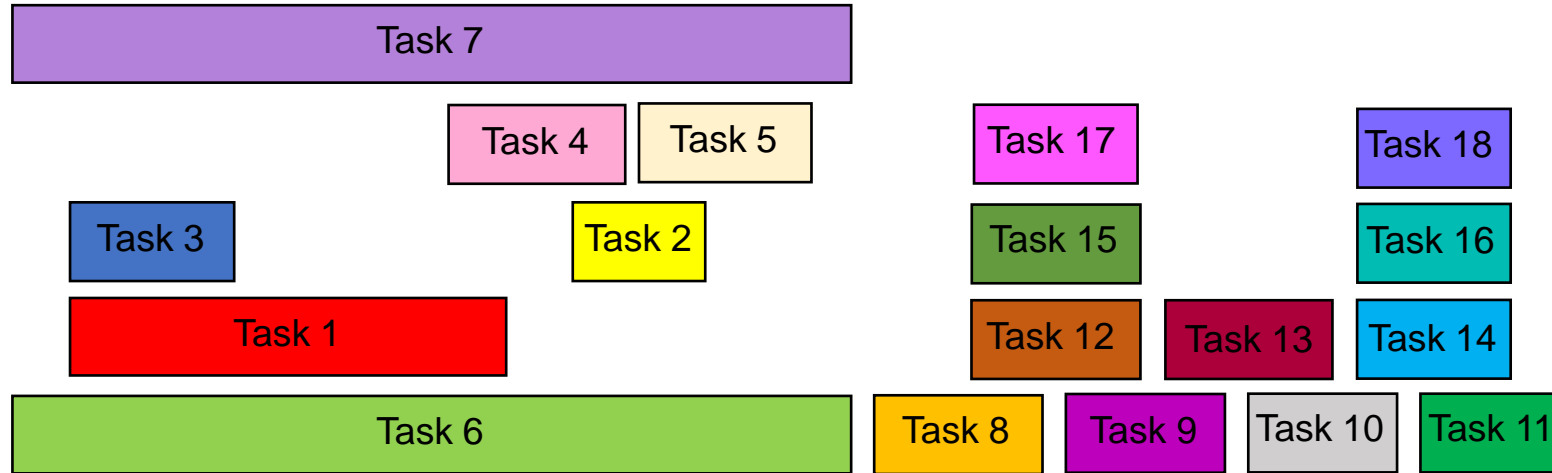
 Choose i in R that has smallest number of conflicts

 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$

Algorithm?



Set S to be the empty set

While R is not empty

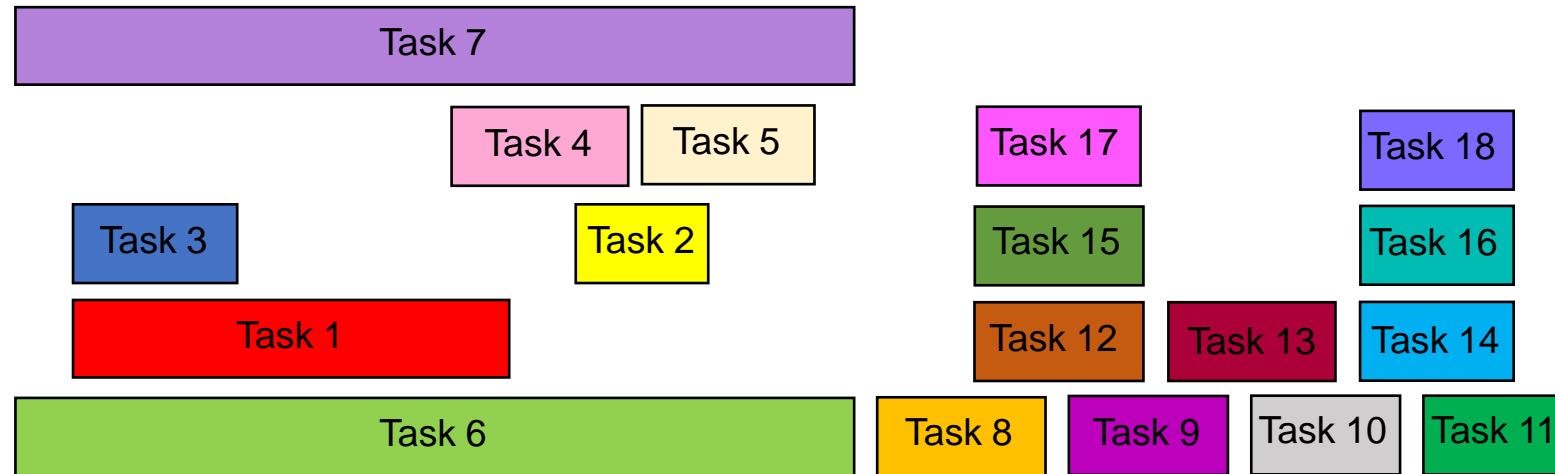
 Choose i in R that minimizes $v(i)$

 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$

Earliest finish time first



Set S to be the empty set

While R is not empty

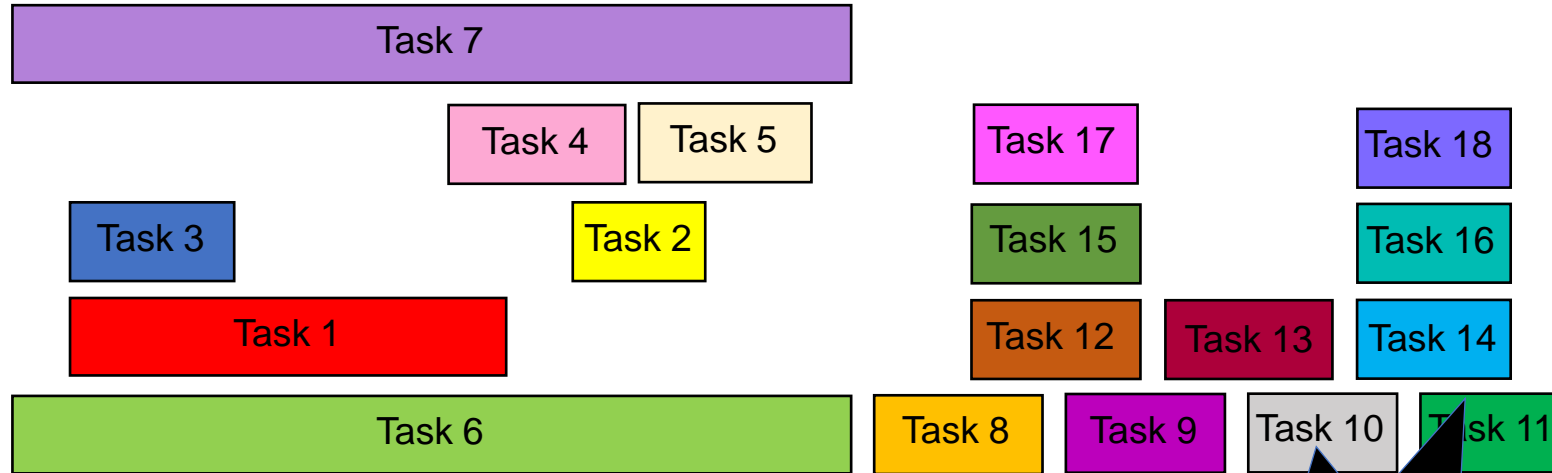
 Choose i in R that minimizes $f(i)$

 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$

Find a counter-example?



Set S to be the empty set

While R is not empty

 Choose i in R that minimizes $f(i)$

 Add i to S

 Remove all tasks that conflict with i from R

Return $S^* = S$

It
works!

Final Algorithm

R : set of requests

Set S to be the empty set

While R is not empty

 Choose i in R with the earliest finish time

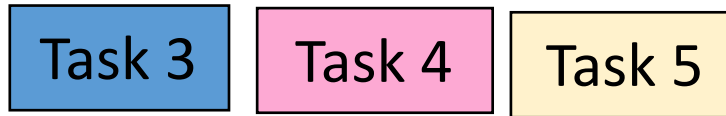
 Add i to S

 Remove all requests that conflict with i from R

Return $S^* = S$

Argue correctness

Observation: A valid schedule sorted by start/finish time gives the same order.



Assume that input intervals are sorted (in increasing order) by finish time

$$\implies f(1) \leq f(2) \leq f(3) \leq \dots \leq f(n).$$

(If the input is not sorted, sort it in $O(n \log n)$ time.)

Greedy Algorithm

0. $R \leftarrow [n]$
1. $S \leftarrow \Phi$
2. while $R \neq \Phi$
 - (2.1) let i be the smallest index in R
 - (2.2) add i to S
 - (2.3) remove i from R
 - (2.4) delete all $j \in R$ that conflict with i
3. Return $S^* \leftarrow S$

Greedy Algorithm

```
0.  $R \leftarrow [n]$ 
1.    $S \leftarrow \Phi$ 
2.   while  $R \neq \Phi$ 
      (2.1) let  $i$  be the smallest index in  $R$ 
      (2.2) add  $i$  to  $S$ 
      (2.3) remove  $i$  from  $R$ 
      (2.4) delete all  $j \in R$  that conflict with  $i$ 
3.   Return  $S^* \leftarrow S$ 
```

Theorem: S^* is an optimal solution.

(that is, \forall inputs, among all possible valid schedules for the input, S^* has the maximum number of intervals.)

Ex 1: Algorithm terminates.

Ex. 2: S^* is a valid schedule.

Proof of correctness of Greedy algorithm:

1. Greedy stays ahead
2. Exchange argument (minimize max. lateness, sec. 4.2 of KT)

Greedy “stays ahead”



Argue correctness on the board...