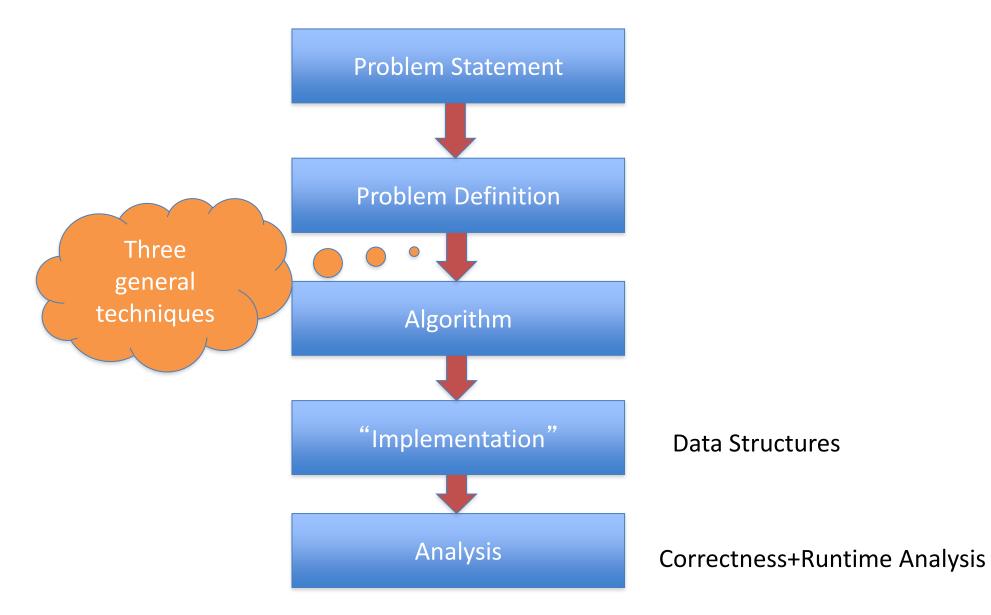
# Lecture 29 CSE 331

## High level view of CSE 331



#### Greedy Algorithms

Natural algorithms

Reduced exponential running time to polynomial

### Divide and Conquer

Recursive algorithmic paradigm



#### Reduced large polynomial time to smaller polynomial time

#### A new algorithmic technique

**Dynamic Programming** 

Dynamic programming vs. Divide & Conquer

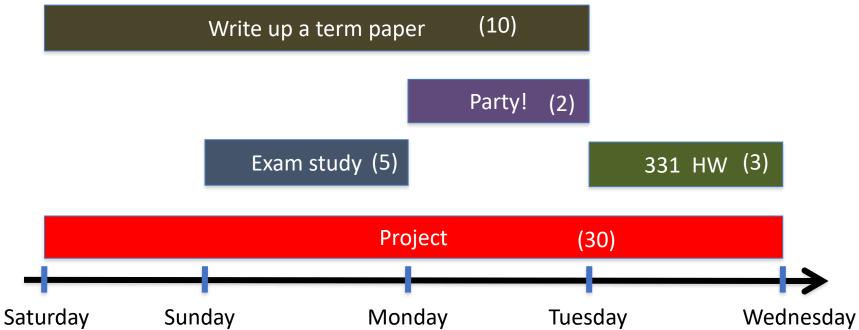
Both design recursive algorithms

Dynamic programming is smarter about solving recursive sub-problems

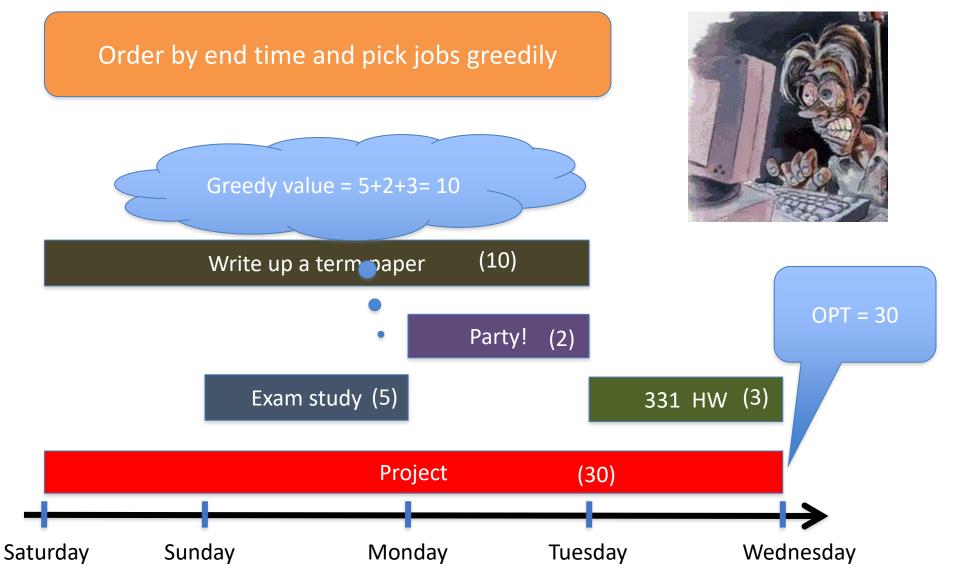
### End of Semester blues

Can only do one thing at any day: what is the optimal schedule to obtain maximum value?





### Previous Greedy algorithm



### Today's agenda

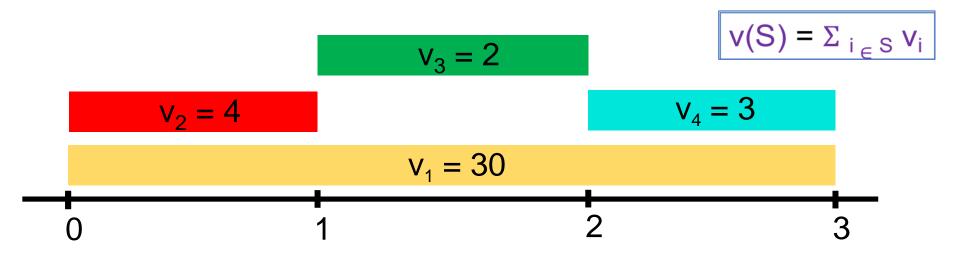
Formal definition of the problem

Start designing a recursive algorithm for the problem

### Weighted Interval Scheduling



#### Output: A valid schedule $S \subseteq [n]$ that maximizes v(S)



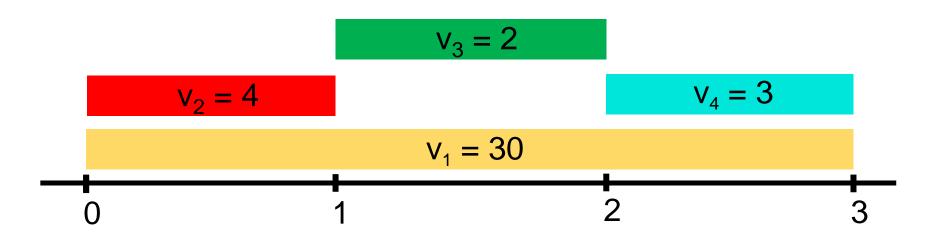
#### Previous Greedy Algorithm

R = original set of jobs

 $S = \phi$ 

While R is not empty Choose i in R where f<sub>i</sub> is the smallest Add i to S Remove all requests that conflict with i from R

Return  $S^* = S$ 

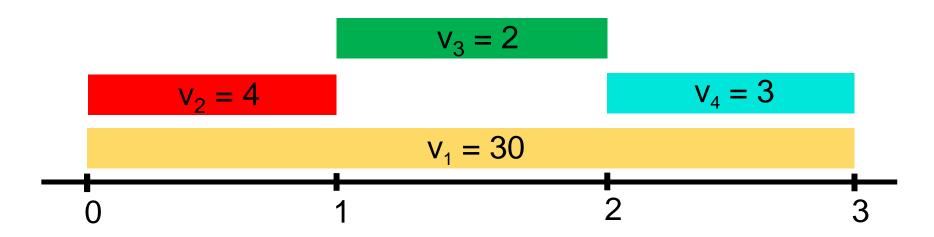


## Perhaps be greedy differently?

- R = original set of jobs
- $S = \phi$

While R is not empty Choose i in R where  $v_i/(f_i - s_i)$  is the largest Add i to S Remove all requests that conflict with i from R

Return  $S^* = S$ 



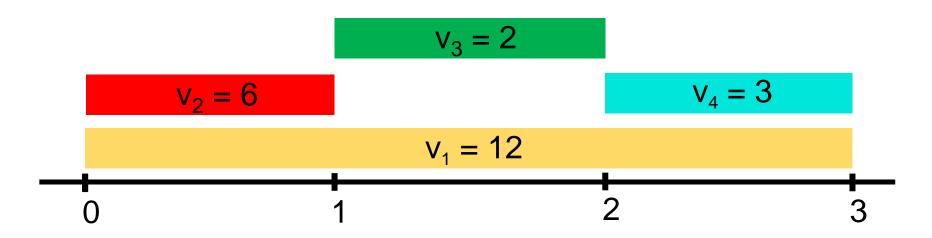
### Can this work?

R = original set of jobs

 $S = \phi$ 

While R is not empty Choose i in R where  $v_i/(f_i - s_i)$  is the largest Add i to S Remove all requests that conflict with i from R

Return  $S^* = S$ 



#### Avoiding the greedy rabbit hole



https://www.writerightwords.com/down-the-rabbit-hole/

There are no known greedy algorithm to solve this problem

#### Perhaps a divide & conquer algo?

#### Divide the problem in 2 or more many EQUAL SIZED INDEPENDENT problems

Recursively solve the sub-problems

Patchup the SOLUTIONS to the sub-problems

### Perhaps a divide & conquer algo?

RecurWeightedInt([n])

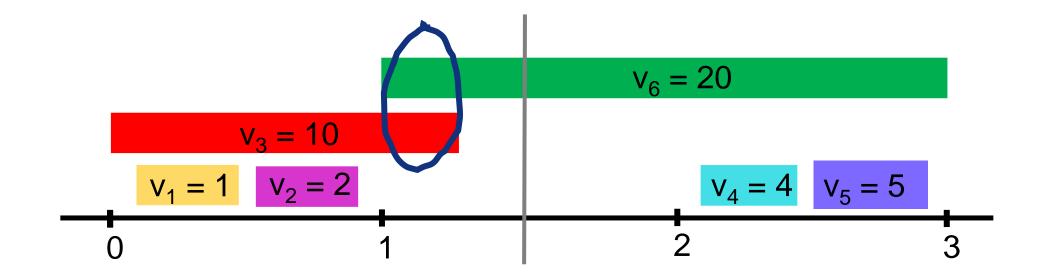
- if n = 1 return the only interval
- L = first n/2 intervals
- R = last n/2 intervals
- S<sub>L</sub> = RecurWeightedInt(L)
- S<sub>R</sub> = RecurWeightedInt(R)

PatchUp(S<sub>L</sub>, S<sub>R</sub>)



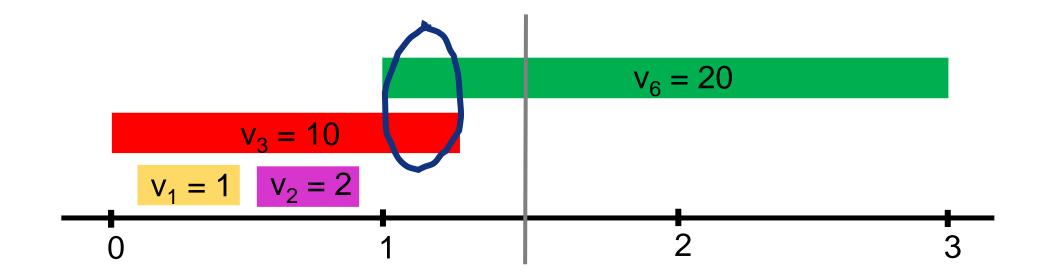
Divide the problem in 2 or more many EQUAL SIZED INDEPENDENT problems

#### Sub-problems NOT independent!

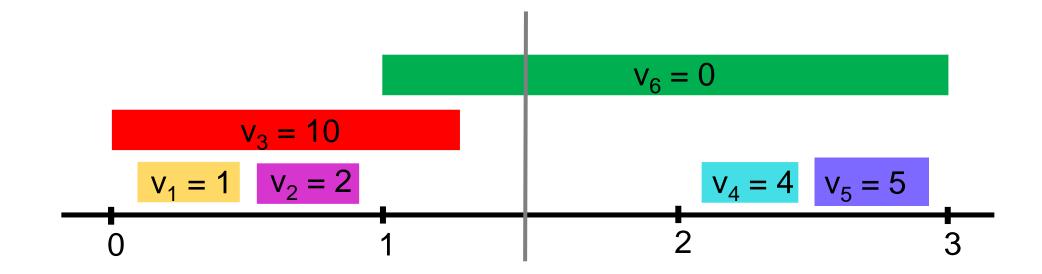


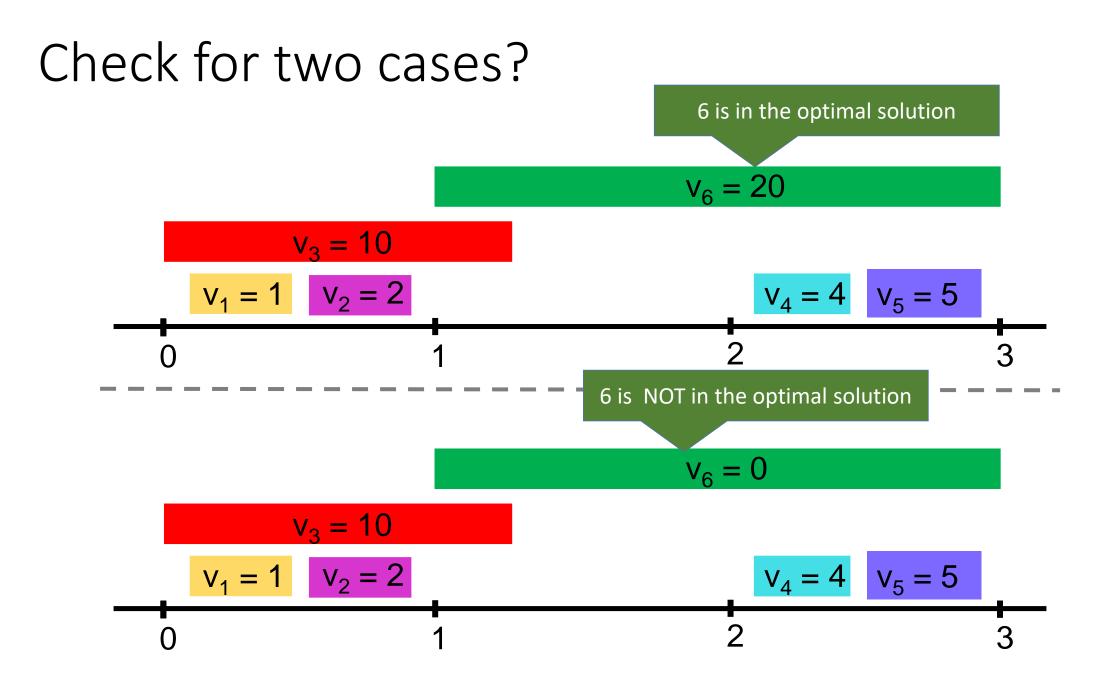
#### Perhaps patchup can help?

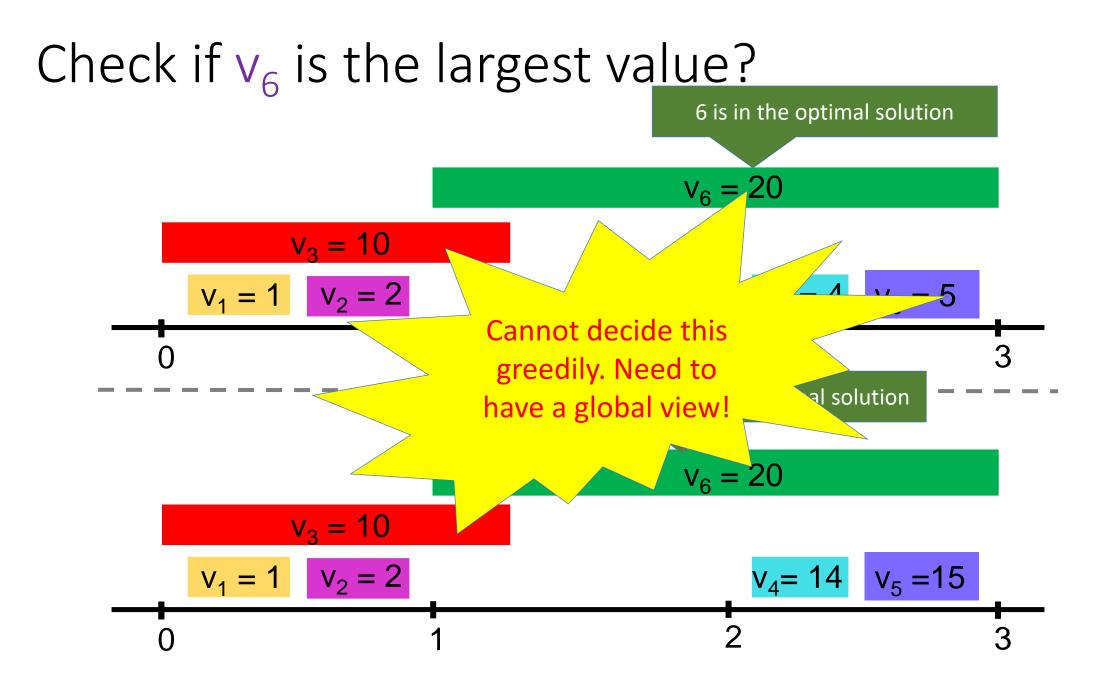
Patchup the SOLUTIONS to the sub-problems



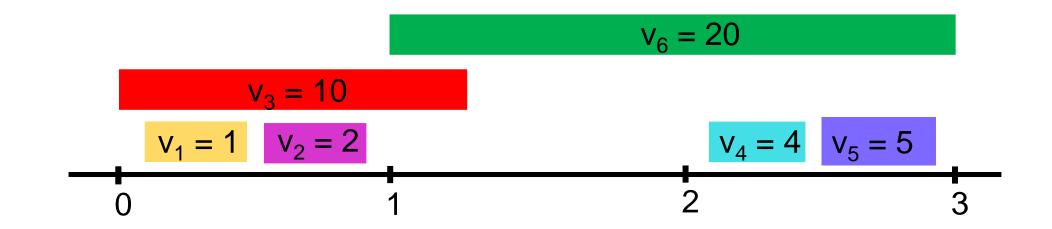
#### Sometimes patchup NOT needed!





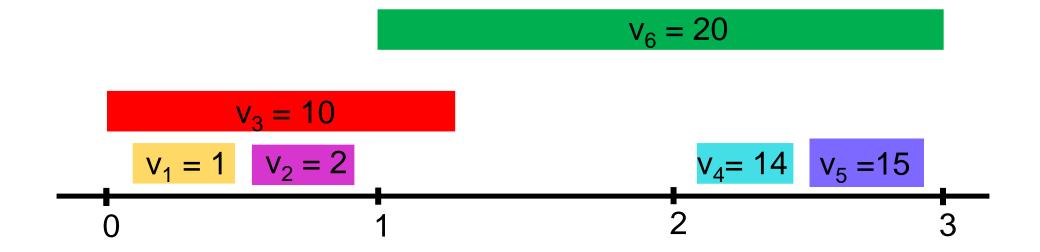


### Check out both options!



Case 1: 6 is in the optimal solution

### 6 is not in optimal solution



#### So what sub-problems?

#### Divide the problem in 2 or more many EQUAL SIZED INDEPENDENT problems

