

Lecture 40

CSE 331

$$Y \leq_P X$$

Question 2 (Big G is in town)



$$\leq_P$$

CSE Major	Slot 1	Slot 2	Slot 3	Slot 4
S ₁	E ₁	free	E ₂	free
S ₂	free	E ₁	free	E ₂

CSE Major	Slot 1	Slot 2	Slot 3	Slot 4
S ₁	E ₁	free	E ₂ (truncate here)	
S ₂	free	E ₁ (truncate here)		

Poly time steps



ANY algo for stable matching problem works!

Arbitrary Y instance

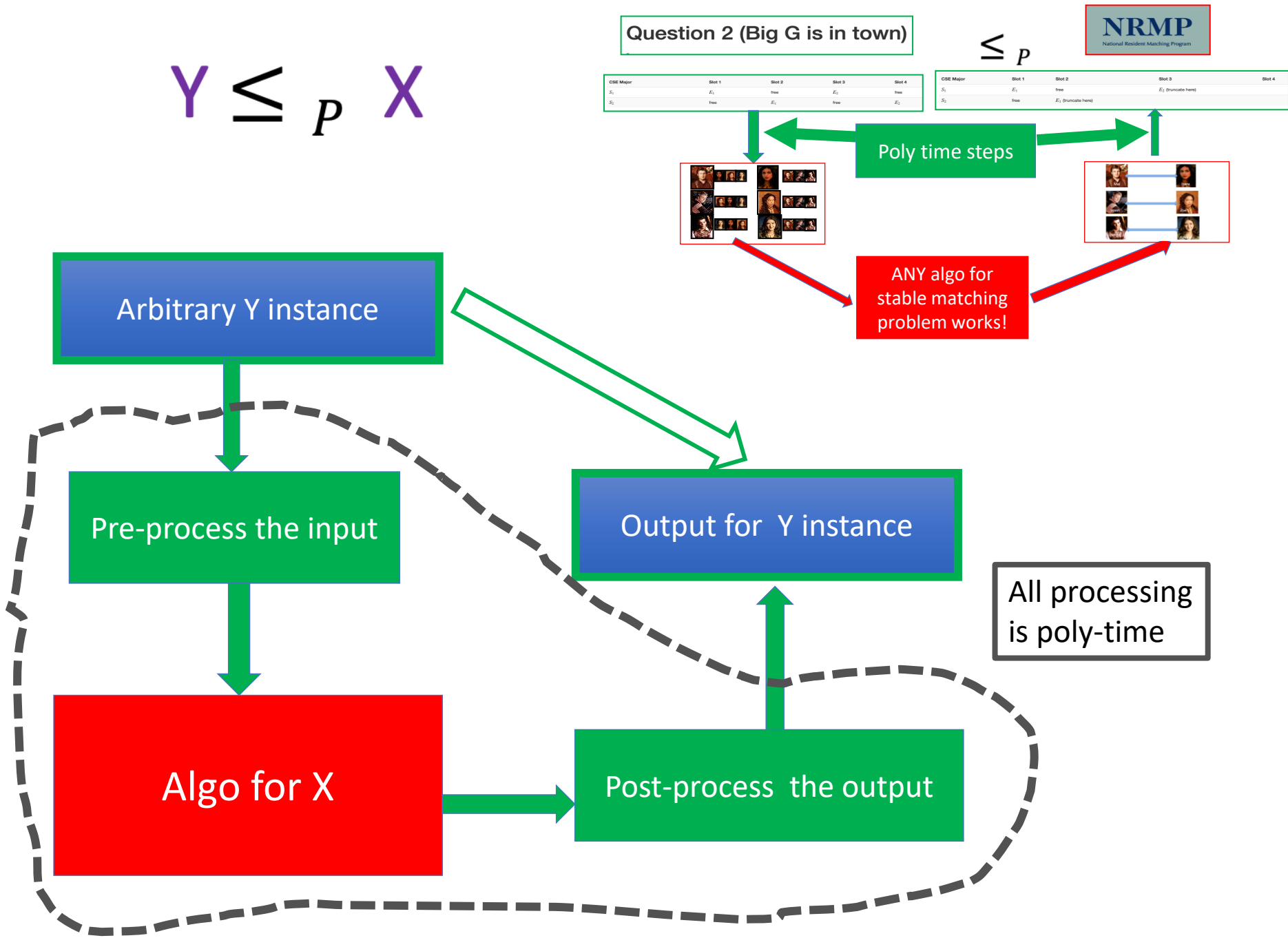
Pre-process the input

Algo for X

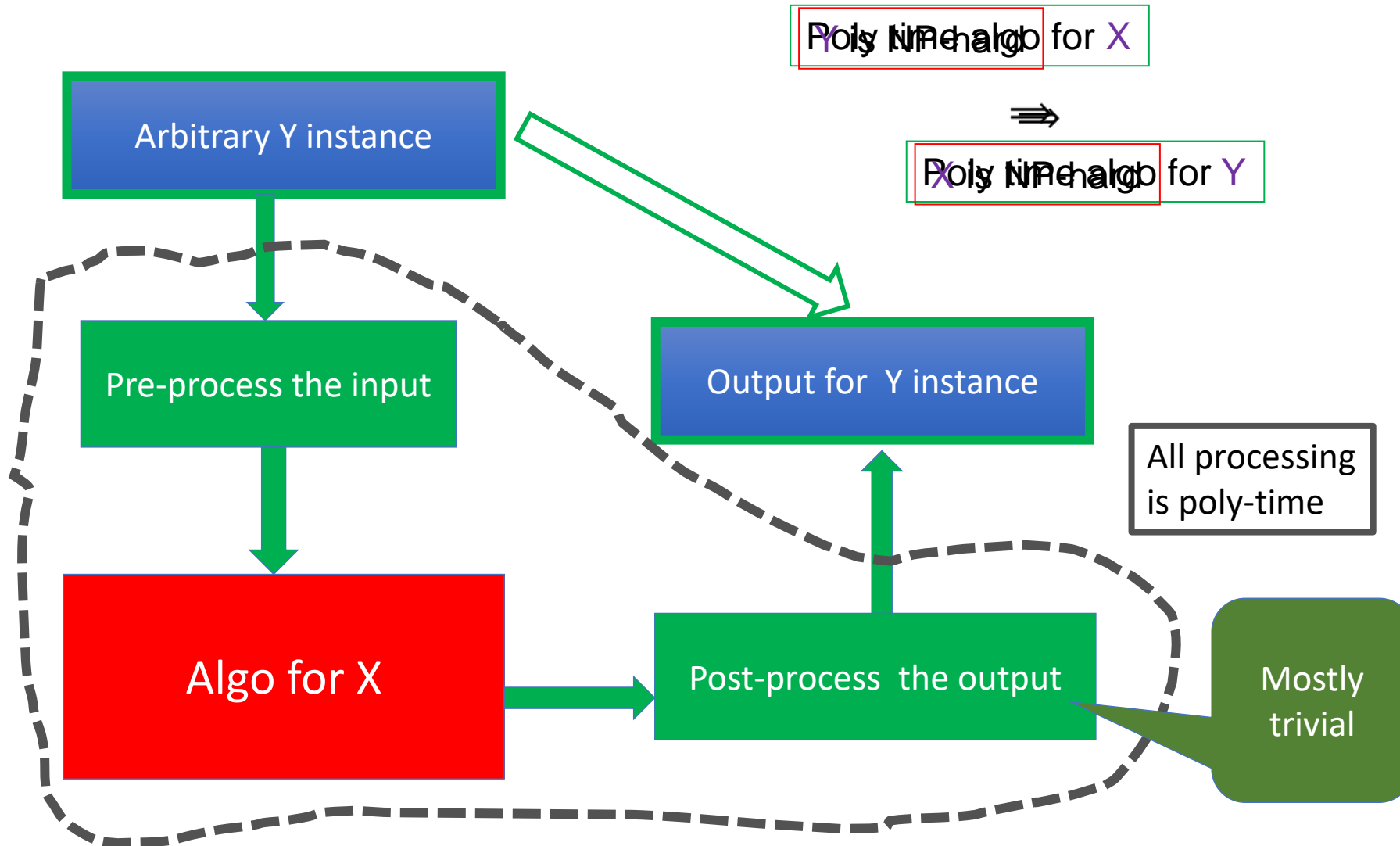
Output for Y instance

Post-process the output

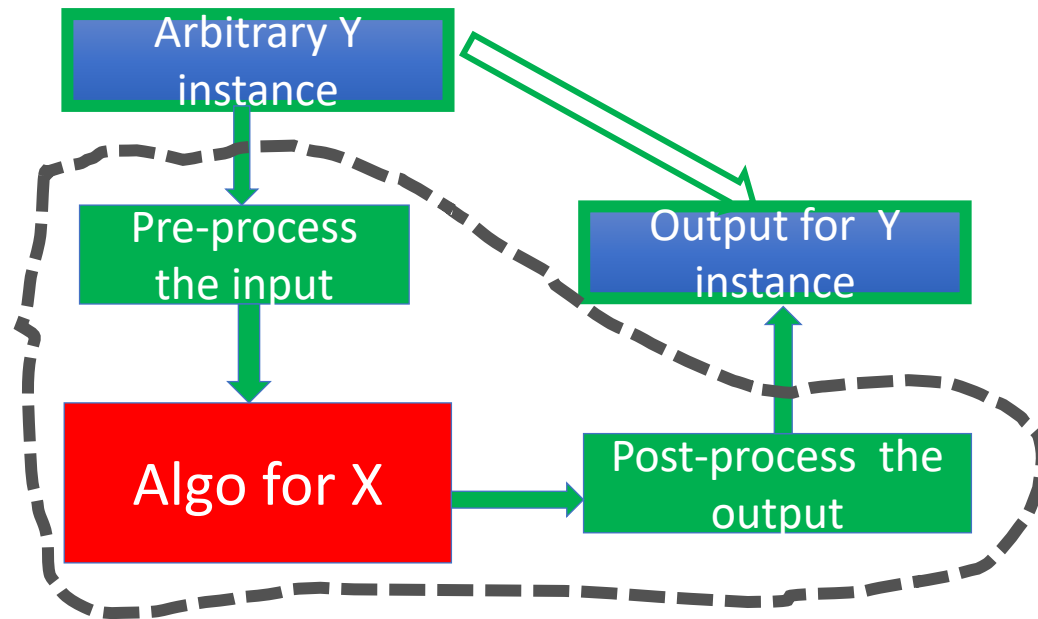
All processing is poly-time



Implications of $Y \leq_p X$



Independent Set \leq_p Vertex Cover



AlgoIS (G, k)

$G' = G$

$k' = n - k$

$b = \text{AlgoVC}(G', k')$

return b



Today's agenda

NP-completeness of k -colorability

Beyond NP-completeness

Anything > NP and < undecidability?

