

# Lecture 7

CSE 331

# HW 1 is out!

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 note @46    ▾

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## Homework 1 is Online

Homework 1 is online at <https://cse.buffalo.edu/~nasrinak/cse331/SP23/hws/hw1/index.html>.

You can also access the homework from the "Homework" drop-down menu in the navigation bar of the [course webpage](#).

**Homework 1 is due Friday, February 17, 8:00pm.**

hw1

# HW0 Grades Released

note @66

stop following **71 views**

Actions

## HW0 Grades Released

HW0 has been graded. The scores and the feedback are now available on Autolab.

Here are the stats (note that the stats are only over the students who submitted and not the entire class):

Q1(a):

Problem	Mean	Median	StdDev	Max	Min
Proof Idea	4.5	2.3	3.9	10.0	0.0

# 1<sup>st</sup> t/f Poll

poll @72

stop following 8 views

Actions

## First T/F Poll

Apologies for getting this started late! The plan is to do a weekly True/false question on piazza. The way it is going to work is that (almost) every Monday (or so) I will post a statement in a poll and ask you all to vote True or False. (Please just vote and do not post your justification yet.) Then after two days, I will give the correct answer, and then I'll ask you to construct the correct justification. Note that this is to give you more practice for the true/false questions on the exams (there will be pretty much no true/false questions on the homeworks). So please try and work on these on your own so that you gain some practice.

Here is the first question. Is the following statement **True** or **False**?

Given  $n$  numbers  $a_1, \dots, a_n$  such that for every  $i \in [n]$  (we will use  $[n]$  to denote the set of integers  $\{1, \dots, n\}$ ) we have  $a_i \in \{0, 1\}$ . That is, we are given  $n$  numbers each of which is a bit. Then we can sort these  $n$  numbers in  $O(n)$  time.

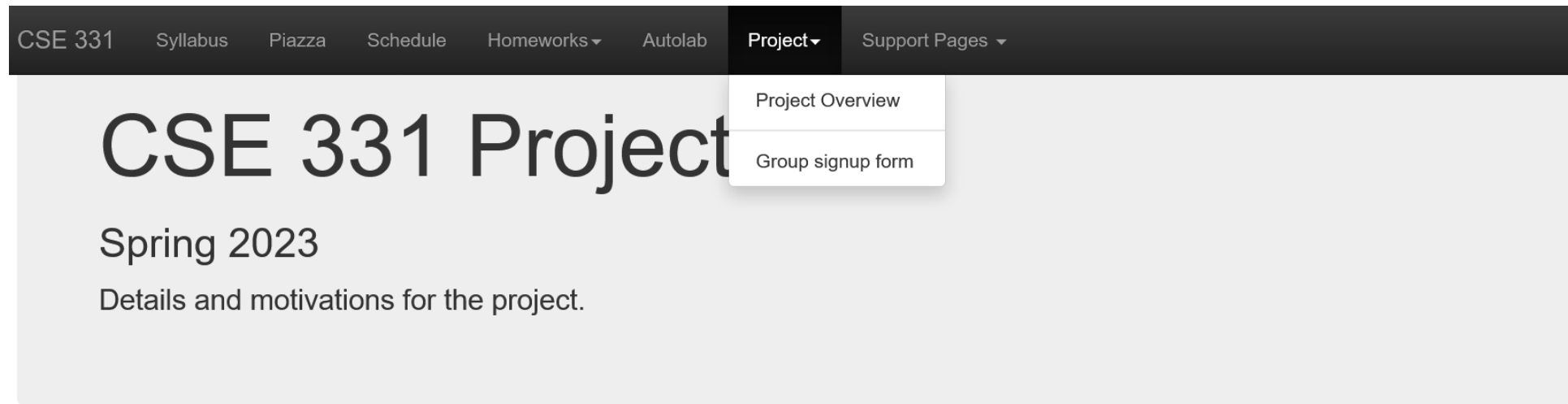
## First T/F Poll closes in 7 day(s)

A total of 4 voter(s) in 0 hours



# Register your project groups

**Deadline: Friday, March 3, 11:59pm**

A screenshot of a web page navigation menu for CSE 331. The menu is dark grey with white text. It includes links for 'CSE 331', 'Syllabus', 'Piazza', 'Schedule', 'Homeworks', 'Autolab', 'Project', and 'Support Pages'. The 'Project' link is highlighted, and a dropdown menu is open, showing 'Project Overview' and 'Group signup form'. Below the navigation menu, the page content is visible, including the title 'CSE 331 Project', the semester 'Spring 2023', and a brief description: 'Details and motivations for the project.'

## Motivation

[CSE 331](#) is primarily concerned with the technical aspects of algorithms: how to design them and then how to analyze their correctness and runtime. However, algorithms are pervasive in our world and are common place in many aspects of society. The main aim of the project is to have you explore in some depth some of the social implications of algorithms.

Just to give some examples for such implications:

Your UB email: [XXX@buffalo.edu](mailto:XXX@buffalo.edu)

Your UBIT ID is **XXX**

**NOT** [XXX@buffalo.edu](mailto:XXX@buffalo.edu)

**NOT** your person number

# Gale-Shapley Algorithm

Initially all men and women are **free**

While there exists a free woman who can propose

Let  $w$  be such a woman and  $m$  be the best man she has not proposed to

$w$  proposes to  $m$

If  $m$  is free

$(m,w)$  get **engaged**

Else  $(m,w')$  are engaged

If  $m$  prefers  $w'$  to  $w$

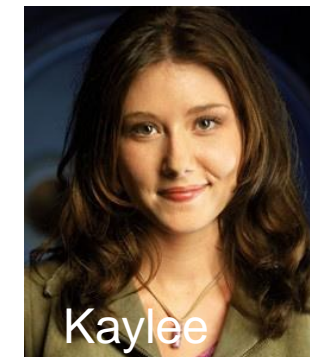
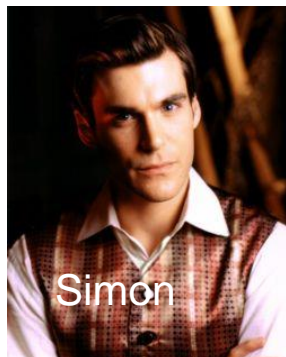
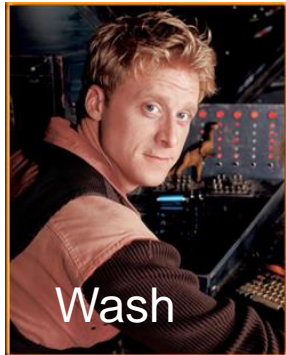
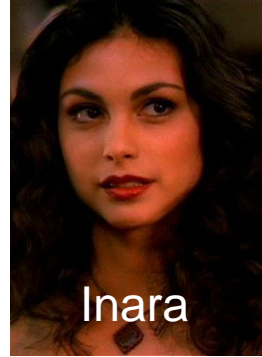
$w$  remains **free**

Else

$(m,w)$  get **engaged** and  $w'$  is **free**

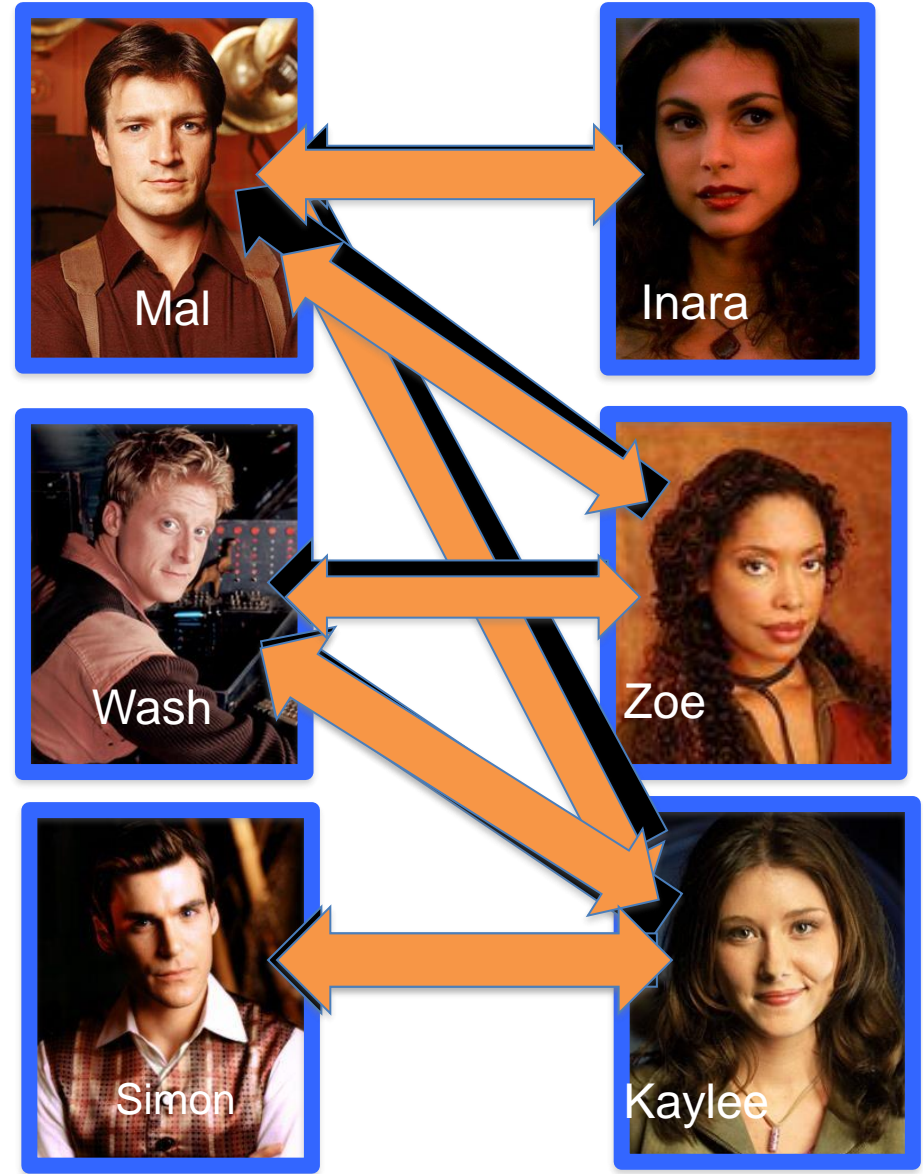
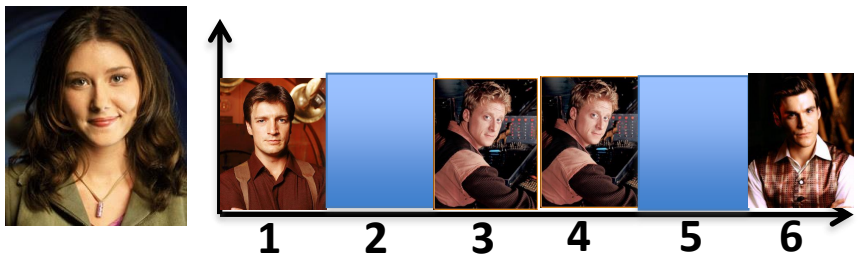
Output the engaged pairs as the final output

# Preferences





# GS algorithm: Firefly Edition



# Observation 1

Initially all men and women are **free**

While there exists a free woman who can propose

Let  $w$  be such a woman and  $m$  be the best man she has not proposed to

$w$  proposes to  $m$

If  $m$  is free

$(m,w)$  get **engaged**

Else  $(m,w')$  are engaged

If  $m$  prefers  $w'$  to  $w$

$w$  remains **free**

Else

$(m,w)$  get **engaged** and  $w'$  is **free**

Once a man gets engaged, he remains engaged (to “better” women)

Output the engaged pairs as the final output

# Observation 2

Initially all men and women are **free**

While there exists a free woman who can propose

Let  $w$  be such a woman and  $m$  be the best man she has not proposed to

$w$  proposes to  $m$

If  $m$  is free

$(m,w)$  get **engaged**

Else  $(m,w')$  are engaged

If  $m$  prefers  $w'$  to  $w$

$w$  remains **free**

Else

$(m,w)$  get **engaged** and  $w'$  is **free**

If  $w$  proposes to  $m$  after  $m'$ , then she prefers  $m'$  to  $m$

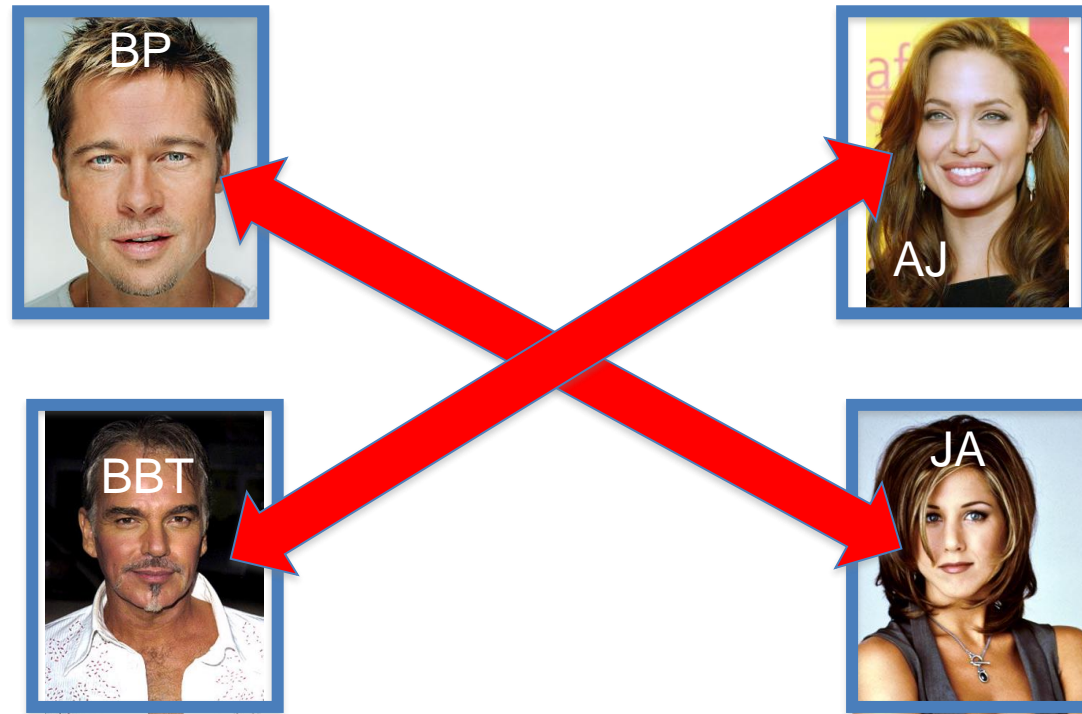
Output the set  $S$  of engaged pairs as the final output

# Why bother proving correctness?

Consider a variant where any free man **or** free woman can propose

Is this variant any different? Can you prove it?

# GS' does not output a stable marriage



# Rest of today's agenda

GS algorithm

Run of GS algorithm on an instance

**Prove correctness of the GS algorithm**