

Feb 23

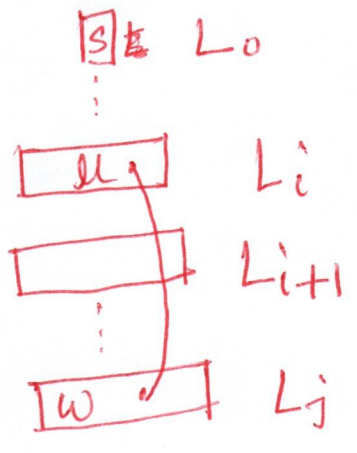
Proposition % let T be a BFS tree for $G = (V, E)$.

IF $(u, w) \in E$ s.t. $u \in L_i, w \in L_j$

$\Rightarrow |i - j| \leq 1 \Leftrightarrow i \in \{j-1, j, j+1\}$

Proof idea: wlog assume $i \leq j$ [if ~~$i > j$~~ , change the roles of i & j]
 ↳ without loss of generality

For contradiction, assume $|i - j| > 1 \Rightarrow j > i + 1 \Rightarrow j \geq i + 2$



Consider the situation when BFS is creating L_{i+1} .

- $\Rightarrow u \in L_i, w \notin L_0, \dots, L_i$
- $\Rightarrow (u, w) \in E$
- $\Rightarrow w$ will be added by BFS to L_{i+1}
- \Rightarrow contradicts $w \in L_j$ for $j \geq i + 2$ \square