Four Data Science Curveballs

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¹Joint work with Tamal Tanu Biswas and with grateful acknowledgment to UB's Center for Computational Research (CCR)

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Key points: Data points have histories, notionally unbiased/ continuous/... need not imply factually unbiased/ continuous/..., and zero-sigma results can be artifacts too.

• X = values of chess moves obtained by analyzing millions of chess positions with chess programs—called *engines*—with names like "Komodo" and "Stockfish" and "Rybka." Now vastly stronger than all human players even running on commodity hardware.

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- Y = performance indicators of (human) players:
 - MM% = how often the player chose the move listed first by the engine in value order.
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 - ASD = the average scaled difference in value between the player's chosen move m_i and the engine's first move m_1 .

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- Z = the players' chess Elo rating: Adult beginner ≈ 600 , club player 1400, master player 2200, human champs 2800, computers 3200+. Based on opponents' Elo ratings and results of the games.

A Predictive Analytic Model

- Domain: A set T of decision-making situations t. Chess game turns
- Inputs: Values v_i for every option at turn t.
 Computer values of moves m_i
- Parameters: s, c, \ldots denoting skills and levels. Trained correspondence $P(s, c, \ldots) \longleftrightarrow$ Elo rating E
- Main Output: Probabilities p_i (= $p_{t,i}$) for P(s, c, ...) to select option i (at turn t).
- **6** The model's Main Equation entails $v_i = v_j \implies p_i = p_j$.
- Outputs:
 - $\bullet~MM\%,~EV\%,~AE$ and other aggregate statistics.
 - Projected confidence intervals for them—via Multinomial Bernoulli Trials plus an adjustment for correlation between consecutive turns.

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• Intrinsic Performance Ratings (IPRs) for the players.

Gathering Data With a GUI (note EV-tie at depths 12 and 13)

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- Besides g, the model picks a function $h(p_i)$ on probabilities.
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• Here $\delta(v_1, v_i)$ scales $v_1 - v_i$ in regard to $|v_1|$.

Any equations in these values will entail

$$v_1 = v_2 \implies p_1 = p_2.$$

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- Taken with multiple Stockfish and Komodo versions using special batch scripts that clear hash between game turns.

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- How about my ESP test??
Conditioned on one of the top two moves being played, if their values (old: Rybka 3, depth 13; new: Stockfish and Komodo, depths 19+) differ by...:

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 - Relation to slime molds and other "semi-Brownian" systems?

History and "Swing" over Increasing Depths



Move	1	2	3	4	5	6	7	8	9	10	11	12	13	14	15	16	17	18	19
Nd2	103	093	087	093	027	028	000	000	056	-007	039	028	037	020	014	017	000	006	000
Bxd7	048	034	-033	-033	-013	-042	-039	-050	-025	-010	001	000	-009	-027	-018	000	000	000	000
Qg8	114	114	-037	-037	-014	-014	-022	-068	-008	-056	-042	-004	-032	000	-014	-025	-045	-045	-050
Nxd4	-056	-056	-113	-071	-071	-145	-020	-006	077	052	066	040	050	051	-181	-181	-181	-213	-213

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• Non-Parapsychological Explanation:



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- Non-Parapsychological Explanation: *Stable* Library Sorting.
- Chess engines sort moves from last depth to schedule next round of search.

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- Will also separate *performance* and *prediction* in the model.

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Single-PV mode maximally retards "late-blooming" moves from jumping ahead in the stable sort.

Surely Y = the frequency of large errors ("blunders") ought to be continuous as a function of X = the value of the position.

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Elo 2600–2850	I	Komod	lo 9.3		Stockfish 7 (modified)				
Value range	#pos	d10	d15	d20	#pos	d10	d15	d20	
-0.30 to -0.21	4,710	9	13	18	4,193	13	10	14	
-0.20 to -0.11	5,048	11	10	13	5,177	6	9	11	
-0.20 to -0.01	4,677	11	13	16	5,552	8	9	16	
0.00 exactly	9,168	24	25	28	9,643	43	40	38	
+0.01 to +0.10	4,283	6	1	2	5,705	8	3	2	
+0.11 to +0.20	5,198	7	5	3	5,495	10	5	3	
+0.21 to +0.30	5,200	7	2	1	4,506	3	4	2	

Reason evidently that 0.00 is a big *basin of attraction* in complex positions that may force one side to give perpetual check or force repetitions to avoid losing.

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Reason evidently that 0.00 is a big basin of attraction in complex positions that may force one side to give perpetual check or force repetitions to avoid losing. Safety net provided $v_1 > 0$ but absent when $v_1 < 0$. Failure to charge adequately for large "notional errors" $= -\infty$

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Human Versus Computer Phenomena



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Eval-Error Curve With Unequal Players



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Computer and Freestyle IPRs

Analyzed Ratings of Computer Engine Grand Tournament (on commodity PCs) and PAL/CSS Freestyle in 2007–08, plus the Thoresen Chess Engines Competition (16-core) Nov–Dec. 2013.

Event	Rating	2σ range	#gm	#moves
CEGT g1,50	3009	2962-3056	42	4,212
CEGT g25,26	2963	2921-3006	42	5,277
PAL/CSS 5ch	3102	3051–3153	45	3,352
PAL/CSS 6ch	3086	3038–3134	45	3,065
PAL/CSS 8ch	3128	3083–3174	39	3,057
TCEC 2013	3083	3062–3105	90	11,024

Computer and Freestyle IPRs—To Move 60

Computer games can go very long in dead drawn positions. TCEC uses a cutoff but CEGT did not. Human-led games tend to climax (well) before Move 60. This comparison halves the difference to CEGT, otherwise similar:

Sample set	Rating	2σ range	#gm	#moves
CEGT all	2985	2954-3016	84	9,489
PAL/CSS all	3106	3078–3133	129	9,474
TCEC 2013	3083	3062-3105	90	11,024
CEGT to60	3056	3023–3088	84	7,010
PAL/CSS to60	3112	3084–3141	129	8,744
TCEC to60	3096	3072-3120	90	8,184

Degrees of Forcing Play



Forcing Index (2500 perspective)

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Add Human-Computer Tandems



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Evidently the humans called the shots.

Add Human-Computer Tandems



Forcing Index (2500 perspective)

Evidently the humans called the shots. But how did they play?

2007–08 Freestyle Performance



Forcing Index (2500 perspective)

Adding 210 Elo was significant. Forcing but good teamwork.

2014 Freestyle Tournament Performance



Tandems had marginally better W-L, but quality not clear...