

Which came first: Number or Symbol?

eg:
$$\begin{array}{r} 187 \\ + 236 \\ \hline 423 \end{array}$$

Main Actors = Symbolic

1. Alphabet = a finite set of characters.

Numerical Actors:

Examples:

Integers n, m, k, i, j, \dots

DIG = $\{0, 1, 2, 3, 4, 5, 6, 7, 8, 9\}$

Each integer is represented by a string over DIG. (or BIN)

BIN = $\{0, 1\}$ The name Σ

A-Z = $\{A, \dots, Z\}$ will often default to $\{0, 1\}$ [Sigma]

ASCII = 128 char codes for typewriter + control

Then sets of numbers, eg.

UTF-8 (later padded with 128 more)

PRIMES = $\{2, 3, 5, 7, 11, \dots\}$

UNICODE 16-bit char (or more)

correspond to languages

2. A string is a (finite) list of char
eg $x = "aaaab"$: length $|x| = 5$.

Both views of languages correspond to decision problems such as:

3. A language is a set of strings often infinite

Given $x \in \mathbb{Z}$, is x prime?

4. A class is a set of languages. eg. polynomial time.