

# Lecture 22

CSE 331

Oct 24, 2018

# Grading

Mid-term-1 hopefully by tonight

Mid-term-2 hopefully by Friday

HW 5 hopefully by weekend

# Scheduling to minimize lateness

$n$  jobs:  $i$ th job  $(t_i, d_i)$

start time:  $s$

Schedule the  $n$  jobs:  $i$ th job gets interval  $[s(i), f(i)=s(i)+t_i)$



Algo picks  $s(i)$

GOAL: Minimize MAXIMUM lateness

Lateness of job  $i$ ,  $l_i = \max(0, f(i) - d_i)$

# The Greedy Algorithm

(Assume jobs sorted by deadline:  $d_1 \leq d_2 \leq \dots \leq d_n$ )

$f = s$

For every  $i$  in  $1..n$  do

Schedule job  $i$  from  $s(i) = f$  to  $f(i) = f + t_i$

$f = f + t_i$

# Two definitions for schedules

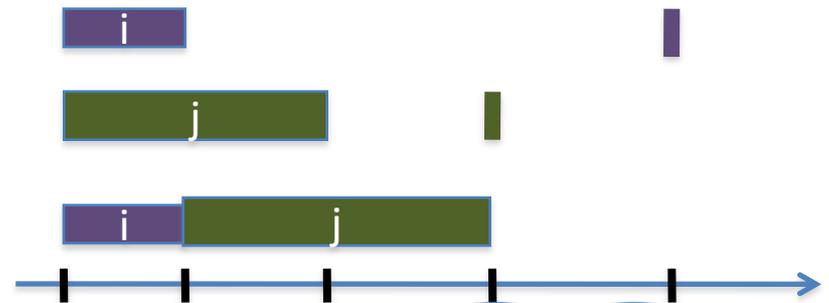
Idle time

Max “gap” between two consecutively scheduled tasks



Inversion

$(i,j)$  is an inversion if  $i$  is scheduled before  $j$  but  $d_i > d_j$



$f=1$

For every  $i$  in  $1..n$  do

Schedule job  $i$  from  $s_i=f$  to  $f_i=f+t_i$

$f=f+t_i$

0 idle time and 0  
inversions for greedy  
schedule

# Proof structure

Any two schedules with 0 idle time and 0 inversions have the same max lateness

Greedy schedule has 0 idle time and 0 inversions

There is an optimal schedule with 0 idle time and 0 inversions

# Today's agenda

“Exchange” argument to convert an optimal solution into a 0 inversion one