

Biometric Identification via Eye Movement Scanpaths in Reading

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Abstract

This paper presents an objective evaluation of various eye movement-based biometric features and their ability to accurately and precisely distinguish unique individuals. Eye movements are uniquely counterfeit resistant due to the complex neurological interactions and the extraocular muscle properties involved in their generation. Considered biometric candidates cover a number of basic eye movements and their aggregated scanpath characteristics, including: fixation count, average fixation duration, average saccade amplitudes, average saccade velocities, average saccade peak velocities, the velocity waveform, scanpath length, scanpath area, regions of interest, scanpath inflections, the amplitude-duration relationship, the main sequence relationship, and the pairwise distance between fixations. As well, an information fusion method for combining these metrics into a single identification algorithm is presented. With limited testing this method was able to identify subjects with an equal error rate of 27%. These results indicate that scanpath-based biometric identification holds promise as a behavioral biometric technique.

1. Introduction

Biometric identification refers to the automated process of extracting, processing, and comparing certain distinctive physical or behavioral characteristics, for the purposes of uniquely identifying a given individual [1]. Biometrics has and continues to maintain a crucial role in the fields of law enforcement, criminal justice, and corporate and personal security. Suspect identification, criminal conviction, access restriction, and personalized interfaces constitute only a small subset of the many and varied applications of biometrics in modern society.

As technology advances, however, biometric traits are becoming easier to reproduce, circumventing the purposes

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of biometric identification techniques and leaving gaps in the efficacy of the systems that use them [2]. To combat this, improvements must continue to be made to existing biometric systems to increase the accuracy and specificity of biometric identification techniques.

There are a wide range of physical and behavioral traits that can be used to identify an individual, often involving the hands [3], face [4], eyes [5], or ears [6]. The eyes in particular offer a variety of physical (iris) and behavioral (eye movements) properties that make them ideal for the purposes of biometric identification, due to their high specificity and the complex mechanical logistics of reproduction [7].

Eye movements are highly counterfeit resistant, as they depend largely on the brain activity and extraocular muscle properties of an individual. As a result, with our current knowledge of the human brain and extraocular muscle structure, it is not possible to accurately replicate eye movements outside of a living human.

While there has been some research into the general applicability of eye movements as a behavioral biometric, the error rates produced by current methods of eye movement analysis [8, 9] and oculomotor plant modeling [10] tend to be much higher than those of accepted biometric systems. For this reason, more research is required to identify eye movement features, and methods of extraction, that are able to provide a higher level of specificity and noise tolerance. In this paper we consider various methods of eye movement pattern (scanpath) analysis and their ability to accurately distinguish between individuals in the context of biometric identification.

2. Background

The term scanpath refers to the spatial path formed by a sequence of fixations and saccades. Fixations occur when the eye is held in a relatively stable position, allowing heightened visual acuity on an object of interest. Saccades occur when the eye rotates quickly (with velocities reaching as high as 700°/s) between points of fixation, with almost no visual acuity maintained during rotation [11].

Scanpath theory is the idea that individuals tend to repeat certain scanpath trajectories during repeated viewings of a

given pattern. This phenomenon was first investigated by Noton and Stark [12], where it was found that the general scanpath displayed by a subject during the first viewing of a pattern was repeated in the initial eye movements of roughly 65% of subsequent viewings.

As well, it has been noted by various sources [12-14] that the scanpaths produced for a given stimulus pattern tend to vary for different subjects. The hypothesized explanation being that these scanpaths are formed in memory during the initial viewing of a pattern.

These inherent properties of scanpaths – subconscious reproduction, variation by subject, variation by stimulus – make them promising candidates as a behavioral biometric. In this paper, we investigate specifically the scanpaths formed during reading.

The reading process presents an instance of high usability, as it is a fairly common activity which should be familiar to most subjects. For an unfamiliar text, reading is also an active cognitive process whose pace and direction are set by the individual subject’s knowledge and experience with similar texts [13, 15]. This cognitive nature of reading forces the subject to concentrate on the material rather than the task, producing more realistic and natural eye movements, and causing distinct differences in the scanpaths exhibited for content of varying difficulty and medium.

3. Biometrics via Scanpath Analysis

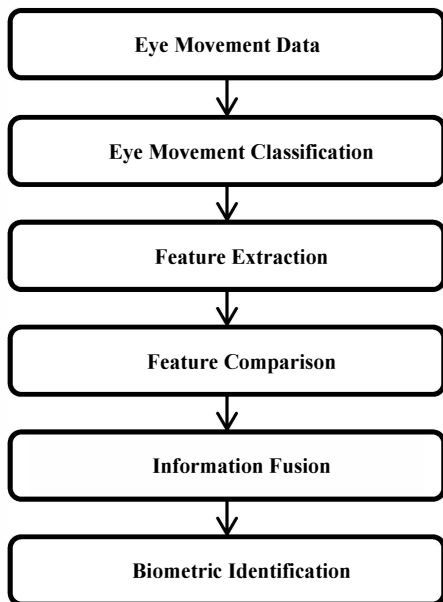


Figure 1: Biometrics via scanpath analysis.

Figure 1 provides an overview of our approach to biometrics via scanpath analysis. The raw Eye Movement Data produced during various recordings is supplied to the Eye Movement Classification module which identifies, filters,

and merges the data points that describe the unique fixations/saccades present in each. Merged fixation and saccade groups are then sent to the Feature Extraction module for analysis, where scanpath features are calculated. In comparing two scanpaths, the scanpath features and fixation groups of each recording are sent to the Feature Comparison module, in which similarity scores are calculated for the various scanpath features, and a pairwise distance comparison is performed on opposing fixation points. The various similarity scores are then supplied to the Information Fusion module to combine them into a single similarity score that can be used for Biometric Identification.

3.1. Eye Movement Classification

The raw eye movement signal, shown in Figure 2, produced by an eye tracker presents a great deal of information, much more in fact than is practically necessary during scanpath analysis. It would be less practical to compare raw eye position data points (as done by Kasprowski and Ober [9]) when the number of fixations/saccades represented by that data is several orders of magnitude smaller. As well, this data often contains extraneous noise caused by blinks and the inherent inaccuracy of the eye tracking system. As a result, this signal must be processed and filtered to provide accurate and useful information.

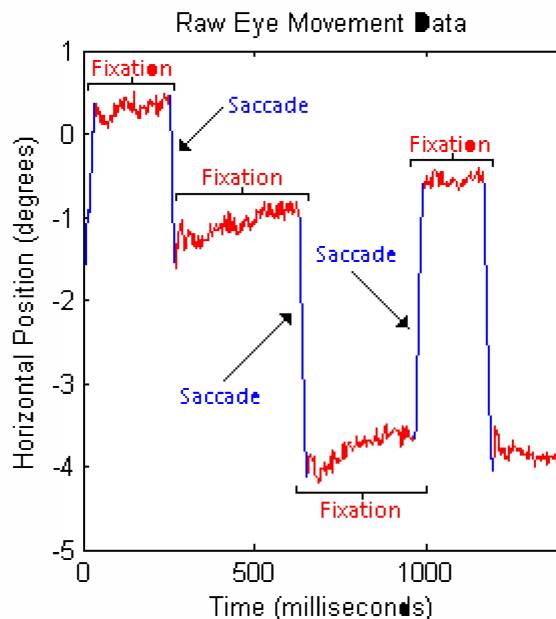


Figure 2: Raw eye movement signal.

To reduce the data set to the basic fixations and saccades that form the scanpath, a velocity threshold algorithm [16] was employed to classify individual points with a velocity

greater than 50°/sec as saccades, where all remaining points were assumed to be fixations. Following the classification process, a micro-saccade filter re-classified saccades with amplitude less than 0.5° as fixations, and a micro-fixation filter re-classified fixations with a duration less than 100 milliseconds as saccades.

Fixation and saccade groups, shown in Figure 3, were then merged. Fixation data included: start time, duration, and positional centroid. Saccade data included: start time, duration, amplitude, velocity, and peak velocity.

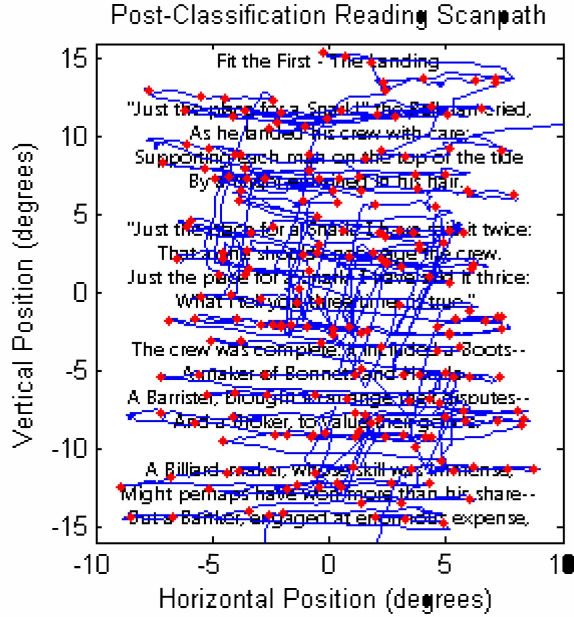


Figure 3: Example reading scanpath.

As a side-note, in all recordings produced in the current experiment the number of fixations and saccades was less than the square root of the total number of data points; this information was useful for improving the performance of processing algorithms. For example, an eye movement recording containing 60,000 data points often contained less than 245 fixations and 245 saccades. Note also that this relation is heavily dependent on the frequency of data collection.

3.2. Feature Extraction

The processed fixation and saccade groups essentially describe the scanpath of a recording. By considering the properties of the scanpath and its individual components, we hope to identify scanpath features that hold promise as biometric indicators. To this end, a number of eye movement metrics were calculated for each recording based on the properties of its unique scanpath.

Basic eye movement metrics considered include: fixation count, average fixation duration, average vectorial

saccade amplitude, average horizontal saccade amplitude, average vertical saccade amplitude, average vectorial saccade velocity, average vectorial saccade peak velocity, and the velocity waveform indicator (Q).

More complex metrics, resulting from the aggregated scanpath data, include: scanpath length, scanpath area, regions of interest, inflection count, and slope coefficients of the amplitude-duration and main sequence relationships.

Fixation Count. Fixation count is indicative of the number of objects processed by the subject [17], and was measured simply as the total number of fixations contained within the scanpath.

Average Fixation Duration. Average fixation duration is indicative of the amount of time a subject spends interpreting an object [17], and was measured as the sum of fixation durations over the fixation count.

Average Vectorial Saccade Amplitude. There is a noted tendency for saccades to maintain similar amplitudes during reading [14], average saccade amplitude was considered as a candidate biometric feature under the assumption that differences in amplitude may be apparent between subjects. Average vectorial saccade amplitude was measured as the sum of vectorial saccade amplitudes over the total number of saccades, where the vectorial amplitude of a saccade was defined as the Euclidean norm of the horizontal and vertical amplitudes, according to the equation:

$$\text{Vectorial Average} = \frac{\sum_{i=1}^n \sqrt{x_i^2 + y_i^2}}{n} \quad (1)$$

Average Horizontal Saccade Amplitude. Horizontal saccade amplitude was considered separately as these are more indicative of between-word saccades. Average horizontal saccade amplitude was measured as the sum of horizontal saccade amplitudes greater than 0.5° over the total number of horizontal saccades with amplitude greater than 0.5°.

Average Vertical Saccade Amplitude. Vertical saccade amplitude was considered separately as these are more indicative of between-line saccades. Average vertical saccade amplitude was measured as the sum of vertical saccade amplitudes greater than 0.5° over the total number of vertical saccades with amplitude greater than 0.5°.

Average Vectorial Saccade Velocity. Average vectorial saccade velocity as measured as the sum of vectorial saccade velocities over the total number of saccades, where the vectorial velocity of a saccade was defined as the Euclidean norm of the horizontal and vertical velocities.

Average Vectorial Saccade Peak Velocity. Average vectorial saccade peak velocity was measured as the sum of vectorial saccade peak velocities over the total number of saccades, where the vectorial peak velocity of a saccade was defined as the Euclidean norm of the horizontal and vertical peak velocities.

Velocity Waveform Indicator (Q). We use the term velocity waveform indicator (Q) to refer to the ratio of peak

velocity to average velocity of a given saccade [11]. In normal human saccades this value is roughly constant at 1.6, though it is assumed that this is subject to some amount of variation similar to the amplitude-duration and main sequence relationships. A rough estimate of this value was obtained from the ratio of the average vectorial peak velocity over the average vectorial velocity.

Scanpath Length. Scanpath length is indicative of the efficiency of visual search [17], and was considered as a candidate biometric feature under the assumption that visual search is dependent on the subject's familiarity with similar patterns/content. Scanpath length was measured as the sum of absolute distances between the vectorial centroid of fixation points, where the vectorial centroid was defined as the Euclidean norm of the horizontal and vertical centroid positions, according to the equation:

$$\text{Scanpath Length} = \sum_{i=2}^n \left| \sqrt{x_i^2 + y_i^2} - \sqrt{x_{i-1}^2 + y_{i-1}^2} \right| \quad (2)$$

Scanpath Area. Scanpath area was measured as the area of the convex hull formed by fixation points, as described by Goldberg and Kotval [17]. Scanpath area is similar to scanpath length in its indication of visual search efficiency, but is less sensitive to localized searching. That is, a scanpath may have a large length while only covering a small area.

Regions of Interest. Regions of interest was measured as the total number of spatially unique regions identified after applying a spatial mean shift clustering algorithm [18] to the fixation points of the scanpath, using a sigma value of 2° and convergence resolution of 0.1° .

Inflection Count. Inflections occur when the scanpath changes direction, in reading there are a certain amount of "forced" inflections that are necessary to progress through the text, but general differences in inflection count are indicative of attentional shifts. Inflection count was measured as the number of saccades in which the horizontal and/or vertical velocity changes signs, according to the following algorithm:

1. Inflections = 0
2. $i = 2$
3. While $i < \text{Saccade Count}$:
4. If $\text{sign}(\text{Velocity}_i) \neq \text{sign}(\text{Velocity}_{i-1})$:
5. Inflections = Inflections + 1
6. End if
7. $i = i + 1$
8. End while

Coefficient of the Amplitude-Duration Relationship. The amplitude-duration relationship varies from person to person, and describes the tendency for saccade duration to increase linearly with amplitude [11], according to the equation:

$$\text{Duration} = C \times |\text{Amplitude}| + \text{Duration}_{\min} \quad (3)$$

To calculate the slope coefficient of this relationship, a data set was constructed from the saccade groups such that x-column data contained the larger absolute component (horizontal or vertical) amplitude and y-column data contained the respective saccade duration.

The slope coefficient of the amplitude-duration relationship was obtained from a linear regression of this data set.

Coefficient of the Main Sequence Relationship. The main sequence relationship varies from person to person, and describes the tendency for saccade peak velocity to increase exponentially with amplitude [19], according to the equation:

$$\text{Peak Velocity} = \text{Velocity}_{\max} \left(1 - e^{-\frac{|\text{Amplitude}|}{C}} \right) \quad (4)$$

This relationship has shown to be roughly linear for small saccades in the range of $0-10^\circ$ amplitude. As a result, we have assumed that a linear approximation is acceptable in the current context, as the saccades produced during reading are often on the order of $0-3^\circ$ amplitude, with very few over 10° amplitude.

To calculate the slope coefficient of this relationship, a data set was constructed from the saccade groups such that x-column data contained absolute component (horizontal or vertical) amplitude and y-column data contained the respective absolute component peak velocity.

The slope coefficient of the main sequence relationship was obtained from a linear regression of this data set.

3.3. Feature Comparison

Analysis of Scanpath Components. While the previously discussed metrics proved a means of quantifying certain features of individual scanpaths, additional calculations are necessary to compare the similarity of the metrics produced by different scanpaths.

To determine a relative measure of similarity between metrics, a Gaussian cumulative distribution function (CDF) was applied as follows, where x and μ are the metric values being compared and σ is the metric-specific standard deviation:

$$p = \frac{1}{\sigma\sqrt{2\pi}} \int_{-\infty}^x e^{-\frac{t-\mu}{2\sigma^2}} dt \quad (5)$$

Metric-specific standard deviations were determined empirically, details are given in the Experimental Setup section.

The Gaussian CDF comparison produces a probability value between 0 and 1, where a value of 0.5 indicates an exact match and a value of 0 or 1 indicates no match. This probability is converted into a more intuitive similarity score, where a value of 0 indicates no match and values of 1 indicates an exact match, with the following equation:

$$\text{Similarity} = 1 - |2p - 1| \quad (6)$$

From the similarity score, a simple acceptance threshold

may be used to indicate the level of similarity which constitutes a biometric match.

Pairwise Distance Comparison. In addition to similarity calculations for the various scanpath metrics, a method of scanpath analysis similar to that described by Grindinger et al. [20] was developed to estimate the spatial similarity of two distinct scanpaths.

In comparing two scanpaths, the Euclidean pairwise distance was calculated between the centroid positions of fixations. Following this, a tally was made of the total number of fixation points in each set that could be matched to within 1° of at least one point in the opposing set. The similarity of scanpaths was assessed by the proportion of tallied fixation points to the total number of fixation points, to produce a similarity score similar to those generated for the various eye movement metrics.

3.4. Information Fusion

Information fusion combines the information obtained from different biometric traits to improve the overall accuracy of a biometric system [21].

The previously discussed similarity calculations produce a total of 15 different similarity scores based on varying aspects of scanpath analysis. To consolidate these results into a single representative biometric, we employed the use of a weighted mean formula, to improve the overall accuracy of identification while making allowance for the relative accuracy of individual features:

$$\text{Similarity} = \frac{\sum_{i=1}^n \text{Weight}_i \times \text{Similarity}_i}{\sum_{i=1}^n \text{Weight}_i} \quad (7)$$

Metric-specific weighting values were determined empirically, details are given in the Experimental Setup section.

4. Experimental Setup

4.1. Participants

Eye movement data was collected for a total of 32 subjects (26 males / 6 females), ages 18 – 40 with an average age of 23 (SD = 5.4). Mean positional accuracy of the recordings averaged between all calibration points was 0.74° (SD = 0.54°). 29 of the subjects performed 4 recordings each, and 3 of the subjects performed 2 recordings each, generating a total of 122 unique eye movement records.

The first two recordings for each subject were conducted during the same session with a 20 minute break between recordings; the second two recordings were performed a week later, again with a 20 minute break between recordings.

4.2. Apparatus & Software

Eye movements were recorded using an EyeLink II eye tracker [22] running at 1000 Hz. Stimuli were presented on a flat screen monitor positioned at a distance of roughly 685 millimeters from the subject, with screen dimensions of 640×400 millimeters, and resolution of 2560×1600 pixels.

All algorithms and data analysis were implemented and performed in MATLAB, and run using a 3.1 GHz quad-core CPU with 16 GB memory (DDR3 RAM).

4.3. Procedure

Eye movement records were generated for participants' readings of various excerpts from Lewis Carroll's "The Hunting of the Snark." This poem was chosen for its difficult and nonsensical content, forcing readers to progress slowly and carefully through the text.

For each recording, the participant was given 1 minute to read, and text excerpts were chosen to require roughly 1 minute to complete. Participants were given a different excerpt for each of four recording sessions, and excerpts were selected from the "The Hunting of the Snark" to ensure the difficulty of the material was consistent, line lengths were consistent, and that learning effects did not impact subsequent readings.

The raw eye movement records were then processed and classified into the fixations and saccades that describe their unique scanpaths. To determine the metric-specific standard deviation values to be used in similarity calculations, the various eye movement metrics were calculated for each recording, the standard deviation of each metric for recordings produced by each subject were calculated separately, and the average within-subject standard deviation (α) for each metric was calculated. Then, the standard deviation value used for metric-specific similarity calculations was twice the metric-specific average within-subject standard deviation:

$$\sigma = 2\alpha \quad (8)$$

To examine the relative accuracy of individual metrics as biometric features, similarity calculations were run for each metric across all possible combinations of eye movement records. For example, considering 3 eye movement records (A, B, and C) produced by unique subjects, similarity scores were produced for the combinations: A + B, A + C, B + C. For the 122 eye movement records, this resulted in:

$$\binom{122}{2} = 7381 \text{ combinations} \quad (9)$$

From these similarity scores, the receiver operating characteristic (ROC) curves of individual metrics were plotted and equal error rates (EER) were determined to assess their relative accuracies. The ROC and EER of the individual metrics was used as a starting point to order the weighting values of the information fusion technique; spe-

cific weighting values were then modified manually to reduce the EER of the weighted mean:

Weight	Similarity Metric
25	Fixation count
75	Average fixation duration
1	Average vectorial amplitude
10	Average horizontal amplitude
1	Average vertical amplitude
10	Average vectorial velocity
1	Average vectorial peak velocity
1	Velocity waveform indicator
1	Scanpath length
10	Scanpath area
1	Regions of interest
10	Inflection count
1	Amplitude-duration coefficient
1	Main sequence coefficient
1	Pairwise distance comparison

Table 1: Metric-specific weighting values.

The accuracy of the final identification algorithm was calculated similar to metric-specific accuracy, followed by performance assessments of the various stages.

5. Results

5.1. Identification Accuracy

False acceptance rate (FAR) is defined as the percentage of erroneously matched similarity scores, and false rejection rate (FRR) is defined as the percentage of erroneously unmatched similarity scores. The receiver operating characteristic (ROC) curves, shown in Figure 4, plot FRR against FAR at various acceptance thresholds. The equal error rate (EER), shown in Table 2, is the error rate at which FAR and FRR are equal.

EER	Similarity Metric
34%	Fixation count
30%	Average fixation duration
42%	Average vectorial amplitude
36%	Average horizontal amplitude
46%	Average vertical amplitude
37%	Average vectorial velocity
43%	Average vectorial peak velocity
42%	Velocity waveform indicator

43%	Scanpath length
48%	Scanpath area
49%	Regions of interest
38%	Inflection count
45%	Amplitude-duration coefficient
49%	Main sequence coefficient
43%	Pairwise distance comparison
27%	Weighted mean

Table 2: Equal error rates.

Of the considered metrics, average fixation duration (30% EER), fixation count (34% EER), average horizontal saccade amplitude (36% EER), average vectorial saccade velocity (37% EER), and inflection count (38% EER) displayed the most accuracy as biometric indicators.

The main sequence coefficient (49% EER), regions of interest (49% EER), scanpath area (48% EER), and amplitude-duration coefficient (45% EER) provided the least accuracy, often reaching their best half total error rate (HTER) at an acceptance threshold of 1.0, indicating a very poor trade-off of FAR to FRR. It seems likely that this is due in part to the higher level of abstraction inherent in these metrics. While further refinement of thresholds and comparison techniques may yield better results, as presented these metrics do not provide adequate accuracy to justify their use as biometrics.

As well, the weighted mean fusion of scanpath features provides a clear and noticeable benefit in comparison to the individual metrics, as can be seen from the comparative ROC curves, achieving an EER of 27%.

5.2. Identification Performance

Averaged over 10 independent runs, the full process from eye movement classification to biometric identification for comparing the eye movement data supplied by two unique recordings (roughly 3 MB each) took less than 2.30 seconds (SD = 0.01). Of this, eye movement classification took 1.92 seconds (SD = 0.01), feature extraction took 0.35 seconds (SD = 0.01), feature comparison took 0.03 seconds (SD = 0.00), and information fusion took 0.00 seconds (SD = 0.00). Note that eye movement classification may be performed in real time as eye movement data is collected [23], removing this potential bottleneck.

6. Discussion

Previous Work. Silver and Biggs [8] reported an average true positive proportion (TPP) of 65.8% and true negative proportion (TNP) of 98.2% using a neural network for biometric identification based on: the 8 most significant fixations in each recording, the fixation count, average fixation duration, average saccade velocity, average sac-

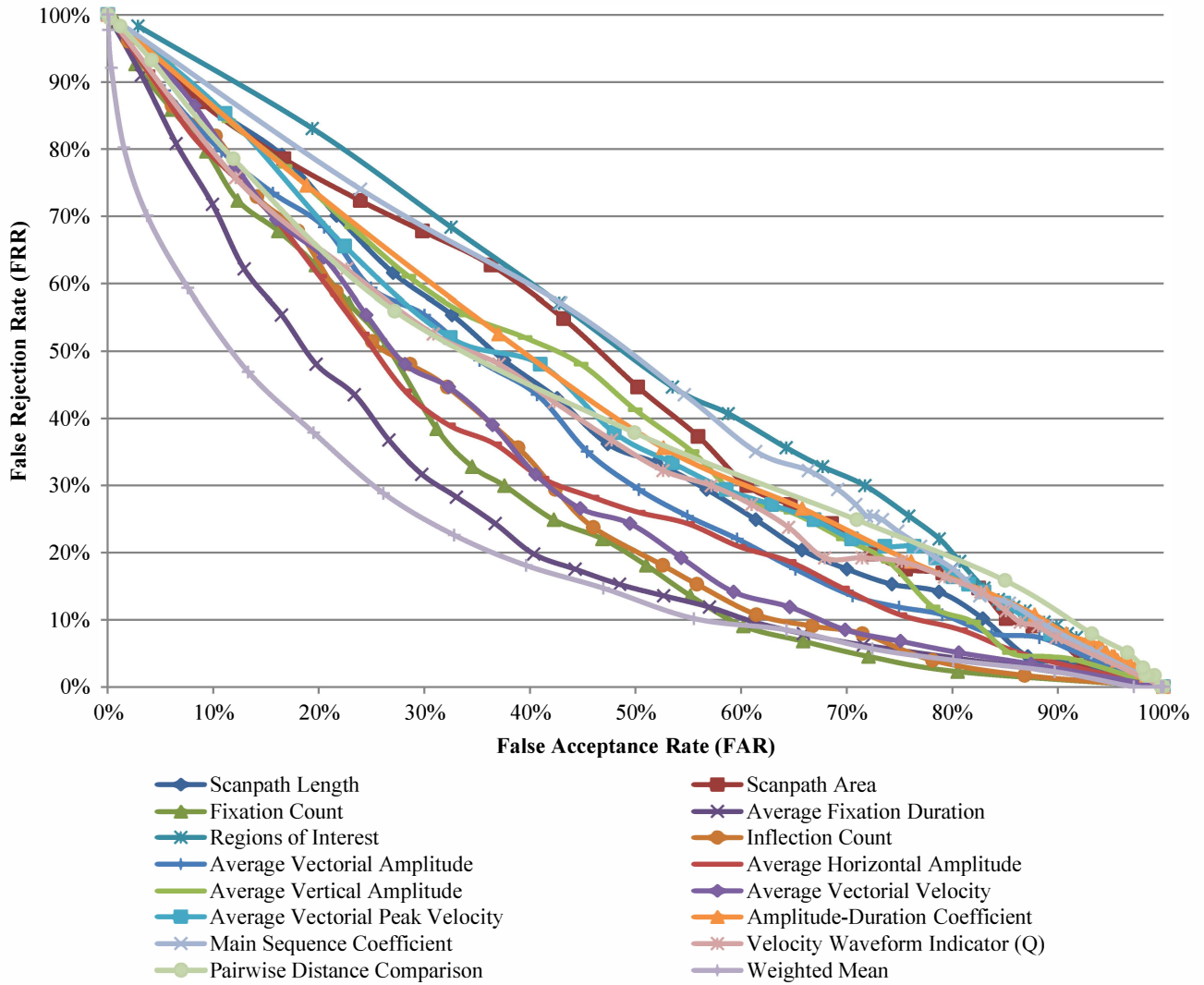


Figure 4: Receiver operating characteristics.

cade duration, and the average vertical position of a user's gaze.

Kasprowski and Ober [9] examined several biometric classification techniques using the cepstral coefficients of the positional signal, and reported accuracy as the average FAR and FRR of each technique: Naïve Bayes obtained an average FAR of 17.5% and FRR of 12.6%, C45 Decision Tree obtained an average FAR of 3.3% and FRR of 35.6%, SVM polynomial obtained an average FAR of 1.6% and FRR of 28.9%, K-Nearest Neighbor ($k = 3$) obtained an average FAR of 1.5% and FRR of 22.6%, and KNN ($k = 7$) obtained an average FAR of 1.4% and FRR of 28.9%.

Neither of these previous works presented the accuracy of individual eye movement characteristics, equal error rates, or ROC curves for the considered techniques. For this reason, it is difficult to compare the results presented in this paper to those provided by previous research; however, we hope these results will establish a baseline performance for

future work.

Limitations. The experiments presented in this paper were conducted under very controlled conditions with the use of high accuracy eye tracking equipment. In practice it would be difficult to replicate such ideal conditions. As well, the relatively small amount of tested subjects and data sets per subject increases the possibility of skewed accuracy results caused by random variation/similarity between recordings.

7. Future Research

There are a number of areas in which the accuracy of these metrics may be improved, including: adjustments to the way analysis is performed, content related analysis, and the implications towards high level brain activity. While we have not addressed these issues in the current paper, focusing instead on the general applicability of scanpath

metrics to biometric identification, they are worth noting as the possible subjects of continued research in this area.

Statistical Analysis Adjustments. Selection of more appropriate standard deviation values and comparison of different probability distributions (e.g. Chi-square, Gamma, etc.) for metric-specific similarity calculations may improve their respective error rates, while a thorough examination of the individual metrics and their relations may allow for increased accuracy through information fusion as the metric-specific weighting values are optimized.

Content Related Analysis. In addition to the considered scanpath metrics, the eye movements produced during reading also exhibit certain traits that are not readily apparent in less structured patterns, allowing further metrics for scanpath comparison [14, 24]. These metrics include: the distribution of fixation positions within a word, which are often Gaussian with a center dependent on the word length; the relative amount of regressions (fixations on previously visited words); and the relative amount of skipped words (words not directly fixated on).

High Level Brain Activity. This work investigated the biometric potential of a set of basic measurements related to individual eye movements and aggregated scanpath characteristics. It is also important to understand if it is possible to categorize the motor control strategies employed by the brain for visual search and learning, and employ such information for identification purposes.

8. Conclusion

As technology advances, biometric traits are becoming easier to reproduce, circumventing the purposes of existing biometric identification techniques and leaving gaps in the efficacy of the systems that use them. Scanpath theory presents a unique solution, as eye movements are uniquely counterfeit resistant due to the complex neurological interactions and extraocular muscle properties involved in their generation.

This paper has presented an objective evaluation of a number of scanpath-based biometric features and their ability to accurately and precisely distinguish unique individuals, with equal error rates ranging from 30%–49%. As well, we have presented an information fusion method which allows for the combination of multiple metrics to produce more stable/accurate identification, which we have shown to be capable of producing an equal error rate of 27% with near real-time performance, allowing for the comparison of two pre-classified eye movement records in less than 0.5 seconds.

9. References

- [1] A. K. Jain, *et al.*, *Handbook of Biometrics*. Secaucus, NJ, USA: Springer-Verlag New York, Inc., 2008.
- [2] C. Roberts, "Biometric attack vectors and defences," *Computers & Security*, vol. 26, pp. 14-25, 2007.
- [3] R. Cappelli, *et al.*, "Performance Evaluation of Fingerprint

- Verification Systems," *IEEE Transactions on Pattern Analysis and Machine Intelligence*, vol. 28, pp. 3-18, 2006.
- [4] J. Lu, *et al.*, "Face Recognition Using LDA Based Algorithms," *IEEE Transactions on Neural Networks*, vol. 14, pp. 195-200, 2003.
- [5] V. Dorairaj, *et al.*, "Performance evaluation of non-ideal iris based recognition system implementing global ICA encoding," presented at the IEEE International Conference on Image Processing, 2005.
- [6] M. Abdel-Mottaleb and J. Zhou, "Human Ear Recognition from Face Profile Images," in *Advances in Biometrics*. vol. 3832, D. Zhang and A. Jain, Eds., ed: Springer Berlin / Heidelberg, 2005, pp. 786-792.
- [7] O. V. Komogortsev and J. I. Khan, "Eye movement prediction by Kalman filter with integrated linear horizontal oculomotor plant mechanical model," presented at the Proceedings of the 2008 symposium on Eye tracking research & applications, Savannah, Georgia, 2008.
- [8] D. L. Silver and A. J. Biggs, "Keystroke and Eye-Tracking Biometrics for User Identification," ed, 2008.
- [9] P. Kasproski and J. Ober, "Eye Movements in Biometrics," in *Biometric Authentication*. vol. 3087, D. Maltoni and A. Jain, Eds., ed: Springer Berlin / Heidelberg, 2004, pp. 248-258.
- [10] O. V. Komogortsev, *et al.*, "Biometric identification via an oculomotor plant mathematical model," in *Proceedings of the 2010 Symposium on Eye-Tracking Research & Applications*, Austin, Texas, 2010, pp. 57-60.
- [11] R. J. Leigh and D. S. Zee, *The Neurology of Eye Movements*, 4 ed.: Oxford University Press, USA, 2006.
- [12] D. Noton and L. Stark, "Scanpaths in Eye Movements during Pattern Perception," *Science*, vol. 171, pp. 308-311, January 22, 1971 1971.
- [13] K. Rayner, "Eye Movements in Reading and Information Processing: 20 Years of Research," *Psychological Bulletin*, vol. 124, pp. 372-422, 1998.
- [14] B. S. Schnitzer and E. Kowler, "Eye movements during multiple readings of the same text," *Vision Research*, vol. 46, pp. 1611-1632, 2006.
- [15] E. J. Paulson, "Viewing Eye Movements During Reading Through the Lens of Chaos Theory: How Reading Is Like the Weather," *Reading Research Quarterly*, vol. 40, pp. 338-358, 2005.
- [16] O. V. Komogortsev, *et al.*, "Standardization of Automated Analyses of Oculomotor Fixation and Saccadic Behaviors," *IEEE Transactions on Biomedical Engineering*, vol. 57, pp. 2635-2645, 2010.
- [17] J. H. Goldberg and X. P. Kotval, "Computer interface evaluation using eye movements: methods and constructs," *International Journal of Industrial Ergonomics*, vol. 24, pp. 631-645, 1999.
- [18] A. Santella and D. DeCarlo, "Robust clustering of eye movement recordings for quantification of visual interest," presented at the Proceedings of the 2004 symposium on Eye tracking research & applications, San Antonio, Texas, 2004.
- [19] A. T. Bahill, *et al.*, "The main sequence, a tool for studying human eye movements," *Mathematical Biosciences*, vol. 24, pp. 191-204, 1975.
- [20] T. Grindinger, *et al.*, "Group-wise similarity and classification of aggregate scanpaths," presented at the Proceedings of the 2010 Symposium on Eye-Tracking Research & Applications, Austin, Texas, 2010.
- [21] A. Ross and A. Jain, "Information fusion in biometrics," *Pattern Recognition Letters*, vol. 24, pp. 2115-2125, 2003.
- [22] S. Research. *EyeLink 1000*. Available: http://www.sr-research.com/EL_1000.html
- [23] D. H. Koh, *et al.*, "Input evaluation of an eye-gaze-guided interface: kalman filter vs. velocity threshold eye movement identification," presented at the Proceedings of the 1st ACM SIGCHI symposium on Engineering interactive computing systems, Pittsburgh, PA, USA, 2009.
- [24] D. J. Schad, *et al.*, "Eye movements during reading of randomly shuffled text," *Vision Research*, vol. 50, pp. 2600-2616, 2010.