CSE462/562: Database Systems (Spring 24)

Lecture 9: Single-table query processing (Part 1)

4/1/2024
Reminders

• The next lecture on 4/8 will be remote due to the solar eclipse
  • Live streaming from Knox 104
  • Please join through Panopto
    • https://ub.hosted.panopto.com/Panopto/Pages/Viewer.aspx?id=d5b61364-381a-4596-8f26-b0f20148c17a

• Project 3 is due today, 23:59 PM EDT
• Project 4 to be released tomorrow, due on 4/15/2024, 23:59 PM EDT
Single-table queries

• We’ll start with the simplest single-table queries w/o or w/ aggregations
  • How to translate it into a query plan?
  • How to implement each operator?
  • How to measure the cost of each operator?

```sql
SELECT G, SUM(E)
FROM R
WHERE P
GROUP BY G
HAVING P'
ORDER BY S
```

```sql
SELECT E
FROM R
WHERE P
ORDER BY S
```
We’ll start with the simplest single-table queries w/o or w/ aggregations

- How to translate it into a query plan?
- How to implement each operator?
- How to measure the cost of each operator?

```sql
SELECT E
FROM R
WHERE P
ORDER BY S
```

$\text{Sort}_S(\pi_E \sigma_P R)$

```sql
SELECT G, SUM(E)
FROM R
WHERE P
GROUP BY G
HAVING P'
ORDER BY S
```

$\text{Sort}_S(\sigma_{P'} G \text{SUM}(E) \sigma_P R)$
Logical plan -> physical plan

• We’ll start with the simplest single-table queries w/o or w/ aggregations
  • How to translate it into a query plan?
  • How to implement each operator?
  • How to measure the cost of each operator?

• A few basic operators
  • Selection: $\sigma$
  • Projection: $\pi$ (w/ and w/o deduplication)
  • Aggregation: $\gamma$ w/o or w/ group by
  • Set operators: $\cup$, $\cap$
  • Sorting (later lectures)
  • Cartesian product: $\times$ or Join: $\bowtie$ (later lectures)

• Question: what are the alternatives? How to evaluate their efficiency?
Measuring cost

• We’ll start with the simplest single-table queries w/o or w/ aggregations
  • How to translate it into a query plan?
  • How to implement each operator?
  • How to measure the cost of each operator?

• For disk-based systems, we mainly measure the number of I/Os
  • Differences between random I/O and sequential I/O
  • Faster storage -> also need to measure the CPU cost

• A simple cost model
  • \( t_T \): average time to transfer a page of data (data transfer time)
  • \( t_S \): average time to randomly seek data (seek time + rotation delay)
    • For SSD, time overhead for initiating an I/O request
  • Cost = \( B \times t_T + S \times t_S \)
    • \( B \): number of pages read/written; \( S \): number of random I/O

<table>
<thead>
<tr>
<th>Typical ( t_T ) and ( T_S )</th>
<th>HDD*</th>
<th>SSD†</th>
</tr>
</thead>
<tbody>
<tr>
<td>( t_T ) (ms)</td>
<td>0.1</td>
<td>0.01</td>
</tr>
<tr>
<td>( t_S ) (ms)</td>
<td>4</td>
<td>0.09</td>
</tr>
</tbody>
</table>

Data from DB Concept book (Ch. 15.2). Assuming 4KB pages.
* typical HDD with 40 MB/s transfer rate, 15000 rpm disk in 2018
† typical SATA SSD that supports 10K IOPS (QD-1), 400 MB/s sequential read rate
Measuring cost

• Other assumptions
  • Ignoring the buffer effect for random pages
  • Do consider the private workspace size $M$ for the operators
  • Omitting the cost of transferring output to the user/disk
    • Common to any equivalent plan

• Notations: for relation $R$
  • $T_R$: number of records, $N_R$: number of pages in its heap file, $B_R$: (average) number of tuples per page
  • $h_I$: height of a B-tree index $I$ over the file
  • $M$: private workspace size in pages

• Running example
  • $t_S = 4 \text{ ms}, t_T = 0.1 \text{ ms}, 4000$-byte page
  • Student: $R$($sid$: int, name: varchar(19), login: varchar(19), major: char(2), adm_year: int)
    • 50 bytes/tuple, $B_R = 80$, $T_R = 40,000$, $N_R = 500$
  • Enrollment: $E$($sid$: int, semester: char(3), cno: int, grade: double)
    • 20 bytes/tuple, $B_E = 200$, $T_E = 200,000$, $N_E = 1000$
**Selection $\sigma$**

- **Scan** is usually the leaf-level of logical plans
  - Represents reading an entire relation -- not really a relational operator
- **Selection $\sigma_P Q$**
  - $P$ is usually conjunctions or disjunctions $Q.\text{attr op value}$
    but can also be User-Defined Functions (UDF)
  - selects records satisfying some predicate from the child
  - Child may be a scan or some other operators

- Many possible implementation of selection depending on
  - the predicate $P$
  - the available file/index for the scan

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**Logical plan for $\sigma_{\text{adm\_year=2021}} R$**

- Scan $R$
- $\sigma_{\text{adm\_year=2021}}$

**op is an operator:** $<, \leq, =, <>, >, \geq, ...$
Simple selection: linear scan

- Consider a simple selection $\sigma_{R.\text{attr op value}}^R$
  - Assume that the child is a relation stored in some disk file/index
- Most straight-forward implementation is linear scan
  - Scan each page and each record on the page
    - emits a record only if the predicate $R.\text{attr op value}$ evaluates to true
  - Applies to any predicate $P$ or file
  - Also works for pipelining -- can do selection on the fly without writing temporary files

- Cost: $t_S + N_R \times t_T$
  - 1 seek to the start of the file and $N_R$ pages to read
  - the “last resort” -- usually the slowest implementation

- cost for $\sigma_{\text{adm\_year=2021}}^R$: $t_S + 500 \times t_T = 54 \text{ ms}$
Simple selection: binary search on sorted file

- If the file on $R$ is sorted on the search key
  - use binary search to locate the first record, then scan the remaining tuples
  - Cost: $\left\lfloor \log_2 N_R \right\rfloor \times (t_S + t_T) + (N - 1) \times t_T$

  \[ N: \text{the number of pages with matching records, which can be approximated as} \]
  \[ N = \left\lfloor sN_R \right\rfloor \]
  - $s$: selectivity, i.e., the percentage of records that satisfy the predicate (discussed later in QO)

- Running example: suppose $R$ is sorted on $adm\_year$ and selectivity is $s = 10\%$
  - cost = $\left\lfloor \log_2 500 \right\rfloor \times (t_S + t_T) + (\left\lfloor 0.1 \times 500 \right\rfloor - 1) \times t_T = 41.8 \text{ ms}$
Simple selection: index scan

- If the file has a B-Tree index $I$ over the search key, assuming alternative 2 for data entries
  - cost varies depending on whether it’s clustered
- Assuming selectivity is $s = 0.1$, the number of matching records is $T$ and the number of pages with matching records is $N$, assume $h = 3$

  cost =
  - $h_I \times (t_T + t_S)$ for finding qualifying data entries +
  - cost for retrieving the heap records
    - clustered: $t_S + N \times t_T \approx t_S + [sN_R] \times t_T$ (total = 12.3 + 9 = 21.3 ms)
    - unclustered: $\left\lceil \frac{T}{F} \right\rceil - 1 \times t_T + T \times (t_T + t_S) = \left\lceil \frac{[sT_R]}{F} \right\rceil - 1 \times t_T + [sT_R] \times (t_T + t_S)$ (total = 12.3 + 16401.3 = 16413.3 ms)
  - can we do better?
Simple selection: index scan (cont’d)

- Refinement for unclustered index scan: bitmap index scan
  1. Initialize a bitmap with one bit for each page in the file (usually fits in mem even for a large file)
  2. Find the first qualifying data entry
  3. Scan all the data entries and mark all the unique pages with the matching records in the bitmap
  4. Scan all the pages with bit 1 (linear scan on page)

- Alternative: collect all RID in memory in step 3, sort and fetch tuples in RID order
  - more expensive unless RIDs fit in memory
  - might make sense for faster storage (thus CPU cost matters)
Cost of bitmap index scan =

- (tree search) $h \times (t_S + t_T) +$
- (scan of data entries) $\left(\left\lceil \frac{T}{F} \right\rceil - 1 \right) \times t_T +$ (assuming leaf level is consecutive from bulk loading)
- (scan of data pages) $N \times (t_S + t_T)$ (when $N$ is small and thus most involve random seeks) or $t_S + N \times t_T$ (when $N$ is close to $N_R$ and it’s close to sequential scan)

Example 1 (large selectivity): $s = 0.9, F = 300, T = [sT_R] = 36000, N = 500$ =>

cost = $4.1 \times 3 + 0.1 \times \left(\left\lceil \frac{36000}{300} \right\rceil - 1 \right) + 4 + 0.1 \times 500 = 78.2$ ms (unclustered)

vs $4.1 \times 3 + 4 + 0.1 \times 500 = 61.3$ ms (clustered)

Example 2 (moderate selectivity): $s = 0.1, F = 300, T = [sT_R] = 4000, E[N] \approx 500$ (think: why?)

cost = $4.1 \times 3 + 0.1 \times \left(\left\lceil \frac{4000}{300} \right\rceil - 1 \right) + 4 + 0.1 \times 500 = 67.6$ ms (unclustered)

vs $4.1 \times 3 + 4 + 0.1 \times 500 = 21.3$ ms (clustered)

Example 3 (small selectivity): $s = 0.0001, F = 300, T = [sT_R] = 4, N = 4$

cost = $4.1 \times 3 + 0.1 \times \left(\left\lceil \frac{4}{300} \right\rceil - 1 \right) + 4.1 \times 4 = 28.7$ ms (unclustered)

vs $4.1 \times 3 + 4 + 0.1 \times \left[0.0001 \times 500\right] = 16.4$ ms (clustered)

Trade-offs:
- Only slightly more expensive than a linear scan when selectivity is close to 1
- Only slightly more expensive than a regular secondary index scan when selectivity is close to 0 (<< linear scan)
- Only works poorly when the selectivity is moderate -- better off with clustered index
  - To show that, let $I_i = 1$ if page $i$ has any matching record (an indicator variable) and assume uniform distribution in search key
  - $E[N] = \sum_{1 \leq i \leq N_R} E[I_i] = \sum_{1 \leq i \leq N_R} \Pr\{I_i = 1\} = N_R(1 - (1 - s)^{BR})$
General selection predicates

• Atom predicate: \textit{attr op value} or UDF

• General predicates:
  • Conjunction \( \land \) (and), disjunction \( \lor \) (or), negation \( \neg \) (not) of atoms or general predicates
  • e.g., \( \sigma_{(adm\_year>=2019 \lor major='CS')} \land sid >= 1000 \)

• Most general cases can always be handled by linear scans
  • Slow!

• Optimization for special cases:
  • Conjunction of simple selection predicates \( \theta_1 \land \theta_2 \land \cdots \land \theta_r \)
    • where \( \theta_i \) is an atom
  • Disjunction of selection predicates \( \theta_1 \lor \theta_2 \lor \cdots \lor \theta_r \)
  • Transforming a predicate \( P \) into \textit{Conjunctive Normal Form (CNF)} or \textit{Disjunction Normal Form (DNF)} for additional optimization opportunities
    • e.g., \( (adm\_year >= 2019 \lor major='CS') \land sid >= 1000 \) \textbf{(CNF)}
      \( \iff (adm\_year >= 2019 \land sid \geq 1000) \lor (major = 'CS' \land sid \geq 1000) \) \textbf{(DNF)}
Conjunctive selection with one index

• $\theta_1 \land \theta_2 \land \cdots \land \theta_r$
  • Choosing one or a prefix of predicates that can be answered using one index
    • Apply the rest of the predicates over the result on the fly
  • For instance, a B-Tree over $(f_1, f_2)$ can select for predicates over a prefix of its index keys
    • $f_1 \ op \ value$ (where $op \in \{<, \leq, =, >, \geq\}$)
    • $f_1 = value \land f_2 \ op \ value$ (where $op \in \{<, \leq, =, >, \geq\}$)
    • If allow using skip scan (jump scan), $f_2 \ op \ value$ or $f_1 \ op \ value \land f_2 \ op \ value$
  • What if there’re multiple choices?
    • Considerations: selectivity, type of indexes, actual cost (access path selection in QO)

• Cost is the same as index scans(bitmap index scans)
Conjunctive selection with multiple indexes

• $\theta_1 \land \theta_2 \land \cdots \land \theta_r$
  • What if the atoms or several conjunctions of atoms can be answered by different indexes?
  • Example: $\sigma_{major='CS'} \land adm\_year=2021 \ R$ when we have two indexes $I_1(major)$ and $I_2(adm\_year)$

• Algorithm:
  1. Collect all the RIDs using both indexes
  2. Compute the intersection of the RIDs
  3. Fetch the heap records of the RIDs in the result set

• Cost: index search + collecting data entries+ sort + intersection + fetching heap records
Partial matches for conjunctive selection

- $\theta_1 \land \theta_2 \land \cdots \land \theta_r$
  - What if only part of the predicates can be optimized with indexes
    - Apply the remaining predicates over the result and discard those that do not satisfy
    - e.g., $\sigma_{\text{major}='CS'} \land \text{adm\_year}=2021$ with a hash index $I(\text{major})$
      - Index Scan for all CS majors using $I(\text{major})$
      - Apply the predicate $\text{adm\_year} = 2021$ over the heap records on the fly

- Note the remaining predicates do not need to be in conjunctive normal form!
  - Can be arbitrary predicates (e.g., UDF)
Disjunction selection with multiple indexes

• $\theta_1 \lor \theta_2 \lor \cdots \lor \theta_r$
  • Only optimizable if all clauses $\theta_i$ can be optimized using some index
  • Otherwise, fall back to linear scan

• Algorithm:
  1. Collect all the RIDs using both indexes
  2. Compute the union of the RIDs
  3. Fetch the heap records of the RIDs in the result set

• Cost: index search + collecting data entries + sort + union + fetching heap records
An excursion: expression evaluation

• So far, we assume **expression evaluation is a black box**
  • Does the predicate evaluate to true in selection?
  • Projection list evaluation?
  • ...

• How does it work?
  • How costly are they?
Expression tree

- A tree that represents an expression
  - Leaf nodes: literals, variables
  - Internal nodes: operators (+, -, *, /, ...), function calls, ...
- Expressions in QP are attached to a plan node
  - Variables refers to columns in the output of some plan node
    - usually output from child, but could be intermediate outputs within certain operators
- Example: predicate $adm\_year \geq 2019 \lor major = 'CS'$

Q: what are the variables in query plan?
A: (short answer) columns in the output

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Expression evaluation

- Interpretation vs Compilation
  - type checking?
- In the course project Taco-DB, we use interpretation (for ease of implementation)
  - recursive evaluation through Eval() calls

\[ \text{rec} = 100, \text{Alice, CS, 2020} \]

\[ = \text{Eval}(\text{rec}) \]

\[ = \text{return result} \]
Projection $\pi$

• Without deduplication
  • evaluate projection list for the records on the fly
  • cost: no additional I/O
  • sometimes baked into other operators (i.e., all operators can be followed by an implicit projection)

• With deduplication
  • Requires materialization (blocking)
  • Hash or Sort
    • Hash -> build a hash table where duplicates are dropped
    • Sort -> emit a record only if it is the first record or it is different from the previous one
  • Result set fits in memory => easy to implement (does not add I/O cost)
  • When result sets exceed configured workspace size $M$,
    • Need to use external hashing and sorting algorithms (next lecture)
    • Optimization opportunities
    • Will come back to this later after we discuss external hashing and sorting
Projection over selection: Index only scan

- For $\pi_{E_1,E_2,...,E_k} \sigma_P R$
  - Let $\text{Var}(E)$ be the set of attributes in the expression $E$
    - e.g., $\text{Var}(R.sid > 100) = \{R.sid\}$
      $$\text{Var}(\text{length}(R.name) + \text{length}(R.login)) = \{R.name, R.login\}$$
  - Suppose there's an index $I$ over $R$ whose index key is $K_I$, such that
    - $\bigcup_{1 \leq i \leq k} \text{Var}(E_i) \cup \text{Var}(P) \subseteq K_I$
    - we can perform an index scan without fetching the heap records (index-only scan)
    - Note: attributes that only appear in the projection list can be non-key columns in index
    - Might be useful even if search key does not match the index key
      - Cheaper than heap scan due to high fan-out

- Cost = tree search cost + cost for scanning all matching data entries
  $$= h \times (t_s + t_T) + \left(\left\lceil \frac{T}{F} \right\rceil - 1\right) \times t_T$$
  (assuming leaf level is consecutive on disk due to bulk loading)
  - Example: $\pi_{\text{adm\_year},\text{sid}} \sigma_{\text{adm\_year}=2021} R$, B-Tree index on $R(\text{adm\_year}, \text{sid})$
    - $h = 3, s = 0.1, T = \lceil sT_R \rceil = 4000, F = 300$
    - cost of index-only scan = $3 \times 4.1 + \left(\left\lceil \frac{4000}{300} \right\rceil - 1\right) \times 0.1 = 13.6$ ms
    vs cost of index scan (clustered) = $3 \times 4.1 + 4 + 0.1 \times [0.1 \times 500] = 21.3$ ms
Summary

• This lecture:
  • Operators for single-table queries
    • Scan, Selection, Projection
    • Expression evaluation

• Next lecture:
  • Aggregation, Sorting, External sorting

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